1. Chances
Most natural laws are based on multiplication, division, and powers. This leads to the experience that the distribution which most often describes observed or measured data well is the log-normal or multiplicative normal distribution, which therefore deserves the name of "the normal distribution", rather than the established, "additive" Gaussian or normal distribution. Using this fact as a starting point in data analysis bears great chances. This is true for a variety of applications across plant protection and most sciences.

2. Nature multiplies
Multiplication of cells
1-2-4-8-16-…
More general, growth, of plants, capital etc:
$s_t = s_0 \cdot k^t$
Life is chemistry, e.g., reaction velocity, $v = k \cdot [A] \cdot [B]$
mass action, $A+B \rightarrow^{\rightarrow} C+D$: $K_c = ([A] \cdot [B]) / ([C] \cdot [D])$
and physics, e.g., osmosis, gas laws $p \cdot v = n \cdot R \cdot T$
Finally, Einstein’s form assumed to be the most well known is based on multiplication, too:
$E = m \cdot c^2$

3. Log- or multiplicative normal distributions
Moreover, the multiplicative version of the well known Central Limit Theorem gives a reason for the basic role of the multiplicative normal distribution: If a number of relatively small variations of single variables in the formulas are combined by multiplications or divisions, this leads to an approximate multiplicative normal distribution.

In addition to the natural laws indicated, a number of phenomena such as health risk (Hattis et al., 1999 cf²) permeability and solute mobility (e.g. Baur, 1997, cf¹) or many further mechanisms (Koch 1966, cf¹) lead to log-normal distributions of data.

In line with this, examples fitting log-normal distributions are ubiquitously found across the sciences. In plant protection, they relate to various aspects and interactions within the disease triangle composed of plants, pests and pathogens, and the environment.


4. The normal distribution is the log-normal distribution. Starting from the impressive anthem and monument W.J. Youden designed in honor of the normal distribution, we changed some words in the beginning only to adapt it to the log-normal. - The shape corresponds to a shape parameter $s^*$ of 1.5. Then, 68% of the data are in the range from the multiplicative mean $xbar^*$ times/divide ($^\times /$) 1.5, with 95% in the range $^\times / 1.5^2$. Interestingly, this $s^*$ is quite typical for latent periods of infectious diseases. – Now, how would be ranges for further interactions and $s^*$’s?

5. According to this insight, analyses should be based on the multiplicative normal distribution in order to improve the quality and efficiency of results. If humans or animals are involved, this even is an ethical imperative. For further results see our poster on “Reconsidering the normal distribution – benefits from replacing ± by $^\times /$”.

*Present Address: ELI-o-Research, Scheuchzerstr. 210, CH-8057 Zürich; +41-76-369 2132 (handy): eckhard.limpert@bluewin.ch

References

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