

Dear all,

I'm new in R and I'm trying to estimate the covariance matrix of a bivariate normal distribution by maximizing the log-likelihood. The maximization **really has to be** performed with the non-linear minimization routine (**nlm**). The 2 means of the distribution are known and equal to 1.

I've already tried 2 different ways to compute this covariance but for each of them I obtained a lot of warnings and illogical values for the covariance matrix.

In the first one, I defined the bivariate normal distribution with the command **dmvnorm**:

```
x<-rnorm(6000, 2.4, 0.6)
x <- matrix(c(x), ncol=1)
y<-rlnorm(6000, 1.3,0.1)
y <- matrix(c(y), ncol=1)
XY <- cbind(x,y)

L<- function(par,x,y) {
  return (-sum(log(par[4]*dmvnorm(XY, mean=c(1,1), sigma= matrix(c(par[1],
  par[1]*par[2]*par[3],par[1]*par[2]*par[3], par[2] ),nrow=2, ncol=2))      )))
}
par.start<- c(0.5, 0.5 ,0.5 ,0.5)
result<-nlm(L,par.start,y=y,x=x, hessian=TRUE)
par.hat <- result$estimate
```

par.hatll y a eu 32 avis (utilisez **warnings()** pour les visionner)

```
> par.hat <- result$estimate
> par.hat
[1] 5.149919e+01 2.520721e+02 8.734212e-03 3.996771e+02
> warnings()
```

Messages d'avis :

- 1: In **log(eigen(sigma, symmetric = TRUE, only.values = TRUE)\$values)** :
production de NaN
- 2: In **nlm(L, par.start, y = y, x = x, hessian = TRUE)** :
NA/Inf replaced by maximum positive value
- 3: In **log(eigen(sigma, symmetric = TRUE, only.values = TRUE)\$values)** :
production de NaN
- 4: In **nlm(L, par.start, y = y, x = x, hessian = TRUE)** :
NA/Inf replaced by maximum positive value
- 5: In **log(eigen(sigma, symmetric = TRUE, only.values = TRUE)\$values)** :
production de NaN
- 6: In **nlm(L, par.start, y = y, x = x, hessian = TRUE)** :
NA/Inf replaced by maximum positive value
- 7: In **log(eigen(sigma, symmetric = TRUE, only.values = TRUE)\$values)** :
production de NaN
- 8: In **nlm(L, par.start, y = y, x = x, hessian = TRUE)** :
NA/Inf replaced by maximum positive value
- 9: In **log(eigen(sigma, symmetric = TRUE, only.values = TRUE)\$values)** :
production de NaN
- 10: In **nlm(L, par.start, y = y, x = x, hessian = TRUE)** :
NA/Inf replaced by maximum positive value

.... Until 24th warning

In the second one, I wrote step by step the bivariate normal distribution in order to have each parameter separately (not in a matrix) but it didn't work as well:

```
x<-rnorm(6000, 2.4, 0.6)
y<-rlnorm(6000, 1.3,0.1)
L <- function(par,x,y) {
  return (-sum(log((1-par[4])*((1/(2*pi*par[1]*par[2])*sqrt(1-par[3])))*exp( (-1/2*(1-par[3]^2))* ((y-
  1)/par[2])^2 +((x-1)/par[1])^2 - 2*(y-1)*(x-1)/(par[2]*par[1])  ))))
}
#par [1]= sigma_x , par [2]= sigma_y par [3]= rho_xy par[4] is a mixing parameter. The final step of my
calculation will be to have a mixture of bivariate normal and log-normal distributions.
par.start<- c(0.5, 0.5 ,0.5 ,0.5)
result<-nls(L,par.start,y=y,x=x, hessian=T)
par.hat <- result$estimate
par.ha
```

When I run this script, I get always 50 advices like those below:

Messages d'avis :

```
1: In sqrt(1 - par[3]) : production de NaN
2: In nls(L, par.start, y = y, x = x, hessian = T) :
  NA/Inf replaced by maximum positive value
3: In sqrt(1 - par[3]) : production de NaN
4: In nls(L, par.start, y = y, x = x, hessian = T) :
  NA/Inf replaced by maximum positive value
5: In sqrt(1 - par[3]) : production de NaN
6: In nls(L, par.start, y = y, x = x, hessian = T) :
  NA/Inf replaced by maximum positive value
7: In log((1 - par[4]) * ((1/(2 * pi * par[1] * par[2] * ... : production de NaN
8: In nls(L, par.start, y = y, x = x, hessian = T) :
  NA/Inf replaced by maximum positive value
9: In log((1 - par[4]) * ((1/(2 * pi * par[1] * par[2] * ... : production de NaN
10: In nls(L, par.start, y = y, x = x, hessian = T) :
  NA/Inf replaced by maximum positive value
..... until 50th warning
```

Does one of you know how to use the nlm method to estimate the covariance matrix (and mixing parameter) of a bivariate normal distribution?

Thank you in advance for your help and answers.

Best regards,

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