ETH
Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich

Lineare Regression: Tests

Statistik (Biol./Pharm.) – Herbst 2012

t-Test in der Linearen Regression: 1/2

1. **Modell:**

$$Y_i = \beta_0 + \beta_1 x_i + E_i,\ E_1, \ldots, E_n \ iid \ \mathcal{N}(0, \sigma^2).$$

2. **Nullhypothese:** $H_0 : \ \beta_1 = 0$
   Alternative: $H_A : \ \beta_1 \neq 0$ (Es wird hier üblicherweise ein zwei-seitiger Test durchgeführt)

3. **Teststatistik:**

$$T = \frac{\text{beobachtet} - \text{erwartet}}{\text{geschätzter Standardfehler}} = \frac{\hat{\beta}_1 - 0}{\widehat{\text{s.e.}}(\hat{\beta}_1)}.$$

   Dabei ist der geschätzte Standardfehler

$$\widehat{\text{s.e.}}(\hat{\beta}_1) = \sqrt{\widehat{Var}(\hat{\beta}_1)} = \frac{\hat{\sigma}}{\sqrt{\sum_{i=1}^{n}(x_i - \bar{x}_n)^2}}.$$

   Verteilung der Teststatistik unter H_0**:** $T \sim t_{n-2}$

t-Test in der Linearen Regression: 2/2

4. **Signifikanzniveau:** α

5. **Verwerfungsbereich fr die Teststatistik:**

$$K = \quad (-\infty, -t_{n-2;1-\frac{\alpha}{2}}] \cup [t_{n-2;1-\frac{\alpha}{2}}, \infty)$$

6. **Testentscheid:** Überprüfe, ob der beobachtete Wert der Teststatistik im Verwerfungsbereich liegt.

Ersatz: Cooper & Shuttle

- 12-Minuten Test nach Cooper (1968)
- 20m-Shuttle-Test nach Leger (1982)

Eur J Appl Physiol (1982) 49: 1–12

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A Maximal Multistage 20-m Shuttle Run Test to Predict $\dot{V}O_2$ max*

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Lineare Regression in R

Modell: $Y_i = \beta_0 + \beta_1 x_i + E_i,\ E_i \sim N(0, \sigma^2)\ i.i.d$

Modell: $Y_i = -19.46 + 5.86 x_i + E_i,\ E_i \sim N(0, 5.43^2)\ i.i.d$

Standardfehler von $\widehat{\beta_1}$

Mit etwa 95% Wa. liegt β_1 im Bereich $5.86 \pm 2 * 0.41$

Beobachtete Teststatistik im Test $H_0: \beta_1 = 0$ vs. $H_A: \beta_1 \neq 0$

P-Wert:

Angenommen $\beta_1 = 0$; wie wa. ist Beobachtung oder etwas extremeres?

```
> fitShuttle <- lm(vo2max ~ vmax, data = dat)
> summary(fitShuttle)

Call:
lm(formula = vo2max ~ vmax, data = dat)

Residuals:
     Min       1Q   Median       3Q      Max
-10.2230  -4.3976  -0.2016   4.7026  12.0348

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -19.4582     4.7239  -4.119  8.5e-05 ***
vmax          5.8566     0.4082  14.347  < 2e-16 ***
---
Signif. codes:  0 ‘***’ 0.001 ‘**’ 0.01 ‘*’ 0.05 ‘.’ 0.1 ‘ ’ 1

Residual standard error: 5.433 on 89 degrees of freedom
Multiple R-squared: 0.6981, Adjusted R-squared: 0.6948
F-statistic: 205.8 on 1 and 89 DF,  p-value: < 2.2e-16
```

Freiheitsgrade: n – (Anz. β’s) = 91 – 2 = 89

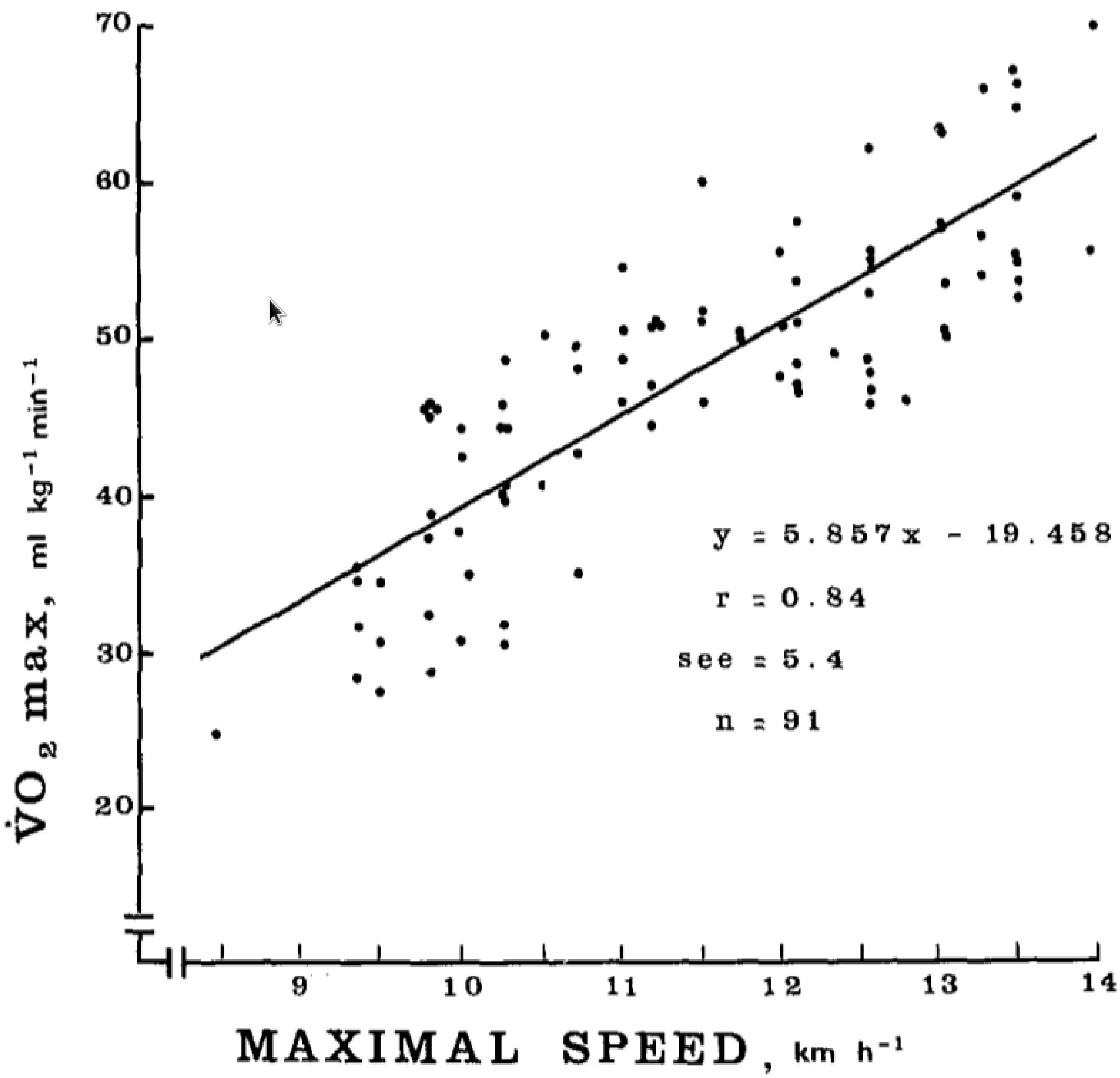
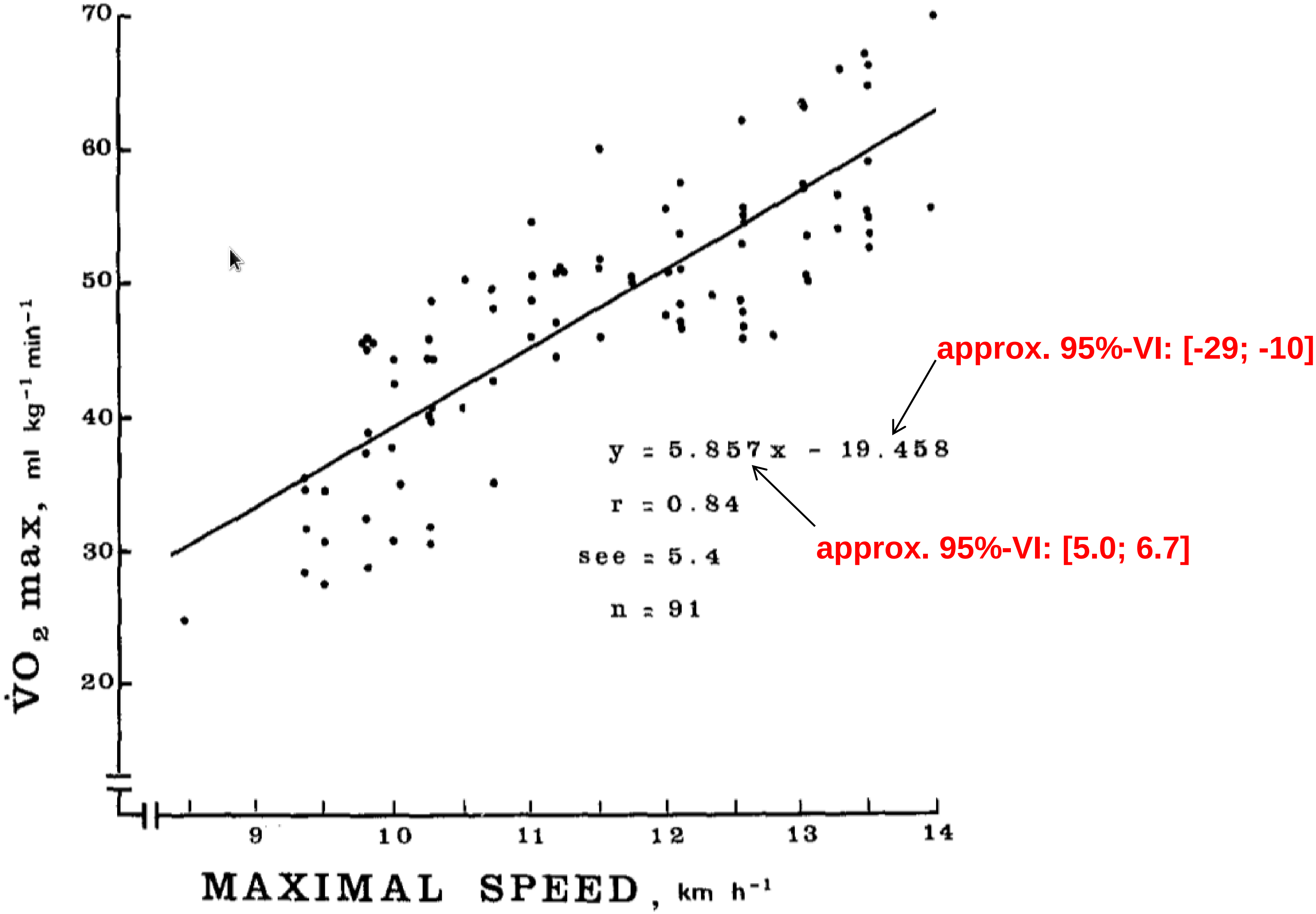


Fig. 2. $\dot{V}O_2$ max as a function of the maximal speed achieved in the 20-m shuttle run test for a total sample of 91 adult subjects. Each point in this figure represents maximal effort



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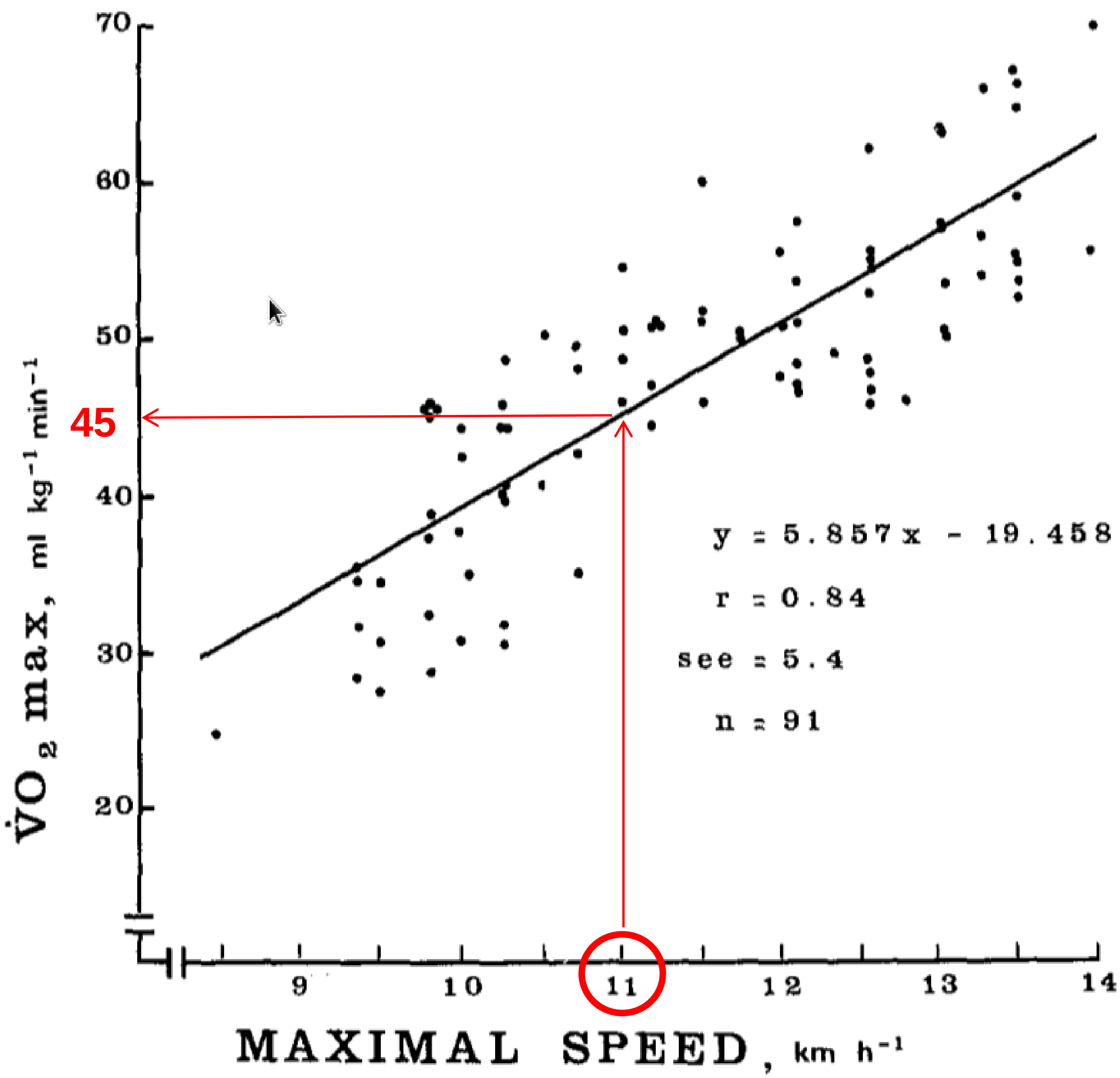

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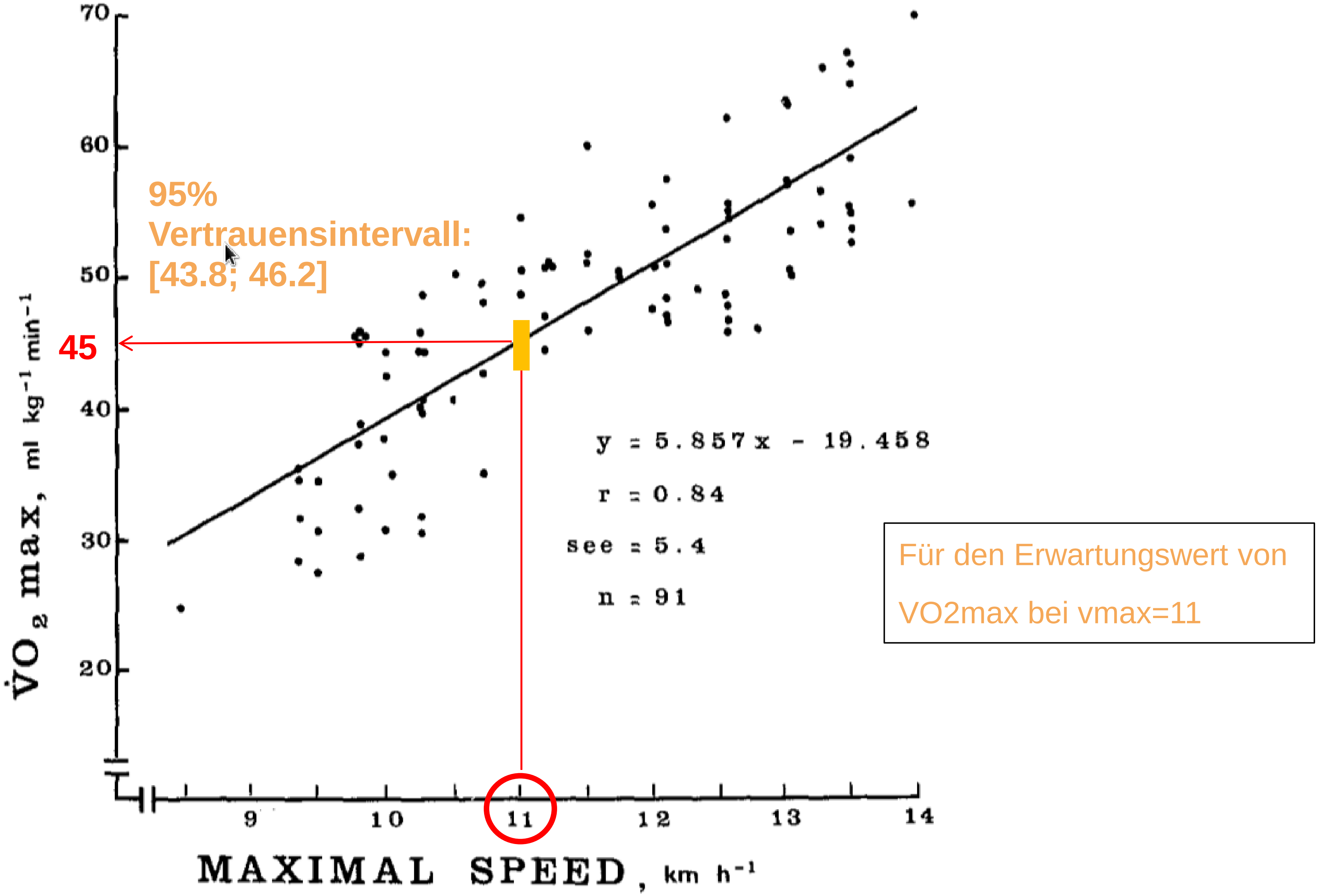

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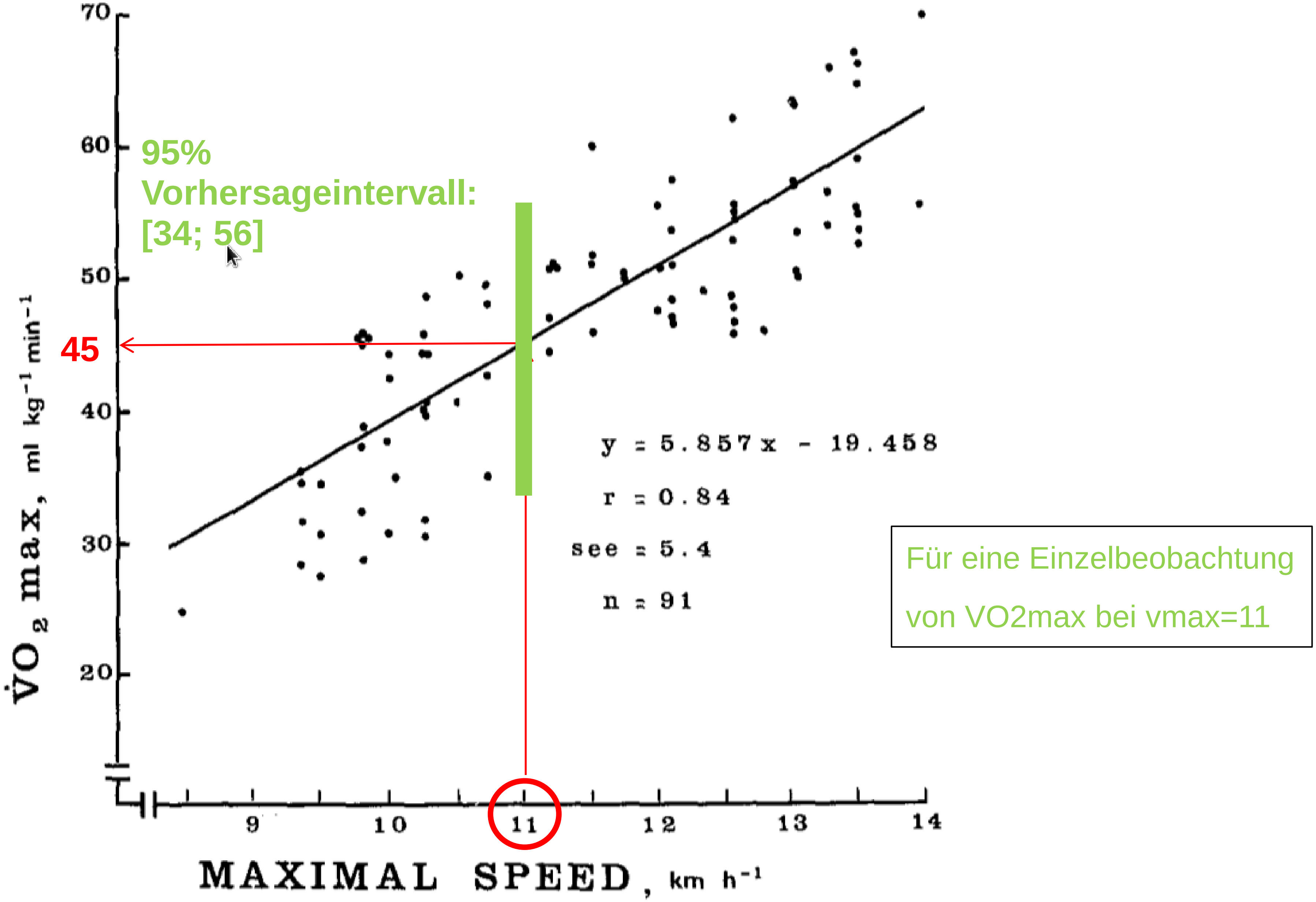

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