Series 2

1. A Plantscientist wants to test the effect of a new herbicide on lentils. He considers the following treatments:

| 1. | Control (without weeding, no fertilizer) | $\mathtt{TR} = 1$ |
|----|---|-------------------|
| 2. | weeding by hand | $\mathtt{TR}=2$ |
| 3. | spraying with herbicide before | $\mathtt{TR} = 3$ |
| 4. | spraying with herbicide after | $\mathtt{TR}=4$ |
| 5. | weeding by hand + fertilizer | $\mathtt{TR} = 5$ |
| 6. | spraying with herbicide before + fertilizer | $\mathtt{TR}=6$ |
| 7. | spraying with herbicide after + fertilizer | $\mathtt{TR} = 7$ |

The experiment was arranged as a block design experiment with 3 blocks (variable BLOCK) and one treatment factor (variable TR). The harvesting weight (variable Y) was used as response. The data is given in the file lentil.dat. (d.len <- read.table("http://stat.ethz.ch/ Teaching/Datasets/WBL/lentil.

a) Check with an analysis of variance if there are differences between treatments.

R hints:

• Reading data in:

```
t.url <- "http://stat.ethz.ch/Teaching/Datasets/WBL/lentil.dat"
d.len <- read.table(t.url,header=T)
d.len$BLOCK <- factor(d.len$BLOCK)
d.len$TR <- factor(d.len$TR)</pre>
```

• Plotting the data:

Use the function

```
> plot(as.numeric(d.len$TR),...)
```

to plot the data (TR on the x-axis and Y on th y-axis).

For a more informative plot use the following combination of R functions to create an empty plot first and then fill it with text:

```
> plot(...,...,type="n",xlab="TR",ylab="Y")
> text(...,...,labels=d.len$BLOCK)
```

b) In order to detect existing differences between treatments, we consider the following contrasts:

| | Treatment | | | | | | |
|----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| Contrast | λ_1 | λ_2 | λ_3 | λ_4 | λ_5 | λ_6 | λ_7 |
| L1 | -6 | +1 | +1 | +1 | +1 | +1 | +1 |
| L2 | 0 | -1 | -1 | -1 | +1 | +1 | +1 |
| L3 | 0 | +2 | -1 | -1 | +2 | -1 | -1 |
| L4 | 0 | 0 | -1 | +1 | 0 | -1 | +1 |
| L5 | 0 | -2 | +1 | +1 | +2 | -1 | -1 |
| L6 | 0 | 0 | +1 | -1 | 0 | -1 | +1 |

Are these contrasts orthogonal? What question can be answered by testing them?

 ${f c}$) Test the contrasts.

R hints:

• <u>Contrasts</u>: Generate a matrix len.contr with the contrasts L1 to L6 in the columns (either use cbind or matrix). Then use the following R code:

```
> contrasts(d.lentil$TR) <- len.contr
> r.len <- aov(...)
> summary.lm(r.len)
# assign contrasts
```

- ANOVA tables for contrasts: R code:
 - > summary(r.len,split=list(Factorname=list(L1=1,...)))
- d) Write down the design matrix. (Source: R.G. Peterson, Agricultural Field experiments Design and Analysis, 1994, p. 113)
- 2. The response time (in milleseconds) was determined for three types of electrical circuits. The results

| Type 1 | 9 | 12 | 10 | 8 | 15 |
|--------|----|----|----|----|----|
| Type 2 | 20 | 21 | 23 | 17 | 30 |
| Type 3 | 6 | 5 | 8 | 16 | 7 |

a) Test the hypothesis, that all types have the same response time.

R hints:

• Creating the data set:

We want separate columns for the factor and for the values.

```
> y <- c(9,12,10,8,15,20,21,23,17,30,6,5,8,16,7)
```

- > Ty <- c(...)
- > circ <- data.frame(Type=Ty,Y=y)</pre>
- > circ\$Type <- as.factor(circ\$Type)</pre>
- ANOVA table:

use the functions

- > circ.fit <- aov(...)
- > summary(circ.fit)
- b) Use Tukey's method to compare pairs of treatment means.

R hints:

- Tukey's method:
 - > TukeyHSD(circ.fit, "Type", conf.level=...)
- c) Construct a set of orthogonal contrasts, assuming that circuit type 2 was different from the other two.

R hints:

- Contrasts: see exercise 1.
- d) Test the contrasts.

R hints:

• Analysis of contrasts:

use the argument "split" to show the contrasts of the fitted data.

- > summary(...,split=list(Type=list(L1=1,L2=2)))
- 3. An experiment was run to compare three different methods to measure air pollution. Two different technicians did the measurements, which are given in ppm (parts per million). To control the influence of the technicians a block design was used.

| | Treatment | | |
|------------|-----------|----|--------------|
| Technician | A | В | \mathbf{C} |
| 1 | 7 | 36 | 2 |
| 2 | 13 | 44 | 18 |

- a) Calculate the overall mean, treatment and block means. Make a 2×3 contingency table with the residuals.
- **b)** Write down the complete anova table. How large is $\hat{\sigma}$?

R hints:

- First create a vector for each factor and a vector for the measurements (i.e. 3 vectors of length 6)
- then create a data frame (do not forget as.factor(...) for the factors).
- You can now use the function > aov(Y~techn+treatment,...)
- 4. A scientist is interested in how genotype of a strawberry plant affects fruit yield. There are three levels of genotype (AA, AB, BB) and ten plots of land, three plants per plot. Each of the three genotypes is present in each plot. The data is in file strawb.dat.

```
st<-read.table("http://stat.ethz.ch/Teaching/Datasets/strawb.dat",header=TRUE)
```

- a) Plot the data.
- **b)** Do an analysis of variance on the data.
- c) Do an analysis of variance without taking into account land effects.

R hints:

- ullet > aov(formula=yield \sim gtype-land,...)
- d) Compare the results in b) and c). Why are the degrees of freedom different? Which result would you use?

Preliminary discussion: 24.10.2011.

Deadline: 31.10.2011.