

## Kapitel 8: Die wichtigsten Verteilungen III

| Verteilung                | $p(k)$ bzw. $f(x)$                                                                                              | $\mathcal{W}(X)$       | $E[X]$                   | $\text{Var}[X]$            |
|---------------------------|-----------------------------------------------------------------------------------------------------------------|------------------------|--------------------------|----------------------------|
| Binomial $(n, p)$         | $\binom{n}{k} p^k (1-p)^{n-k}$                                                                                  | $k = 0, 1, \dots, n$   | $np$                     | $np(1-p)$                  |
| Geometrisch $(p)$         | $p(1-p)^{k-1}$                                                                                                  | $k = 1, 2, \dots$      | $\frac{1}{p}$            | $\frac{1-p}{p^2}$          |
| Poisson $(\lambda)$       | $e^{-\lambda} \frac{\lambda^k}{k!}$                                                                             | $k = 0, 1, 2, \dots$   | $\lambda$                | $\lambda$                  |
| Uniform $(a, b)$          | $\frac{1}{b-a}$                                                                                                 | $a \leq x \leq b$      | $\frac{a+b}{2}$          | $\frac{(b-a)^2}{12}$       |
| Exponential $(\lambda)$   | $\lambda e^{-\lambda x}$                                                                                        | $x > 0$                | $\frac{1}{\lambda}$      | $\frac{1}{\lambda^2}$      |
| Gamma $(\alpha, \lambda)$ | $\frac{\lambda^\alpha}{\Gamma(\alpha)} x^{\alpha-1} e^{-\lambda x}$                                             | $x > 0$                | $\frac{\alpha}{\lambda}$ | $\frac{\alpha}{\lambda^2}$ |
| Normal $(\mu, \sigma^2)$  | $\frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$                                     | $-\infty < x < \infty$ | $\mu$                    | $\sigma^2$                 |
| $\chi_n^2$                | $\frac{1}{2^{\frac{n}{2}} \Gamma(\frac{n}{2})} x^{\frac{n}{2}-1} e^{-\frac{1}{2}x}$                             | $x > 0$                | $n$                      | $2n$                       |
| $t_n$                     | $\frac{\Gamma(\frac{n+1}{2})}{\sqrt{n\pi} \Gamma(\frac{n}{2})} \left(1 + \frac{x^2}{n}\right)^{-\frac{n+1}{2}}$ | $-\infty < x < \infty$ | $0 \ (n > 1)$            | $\frac{n}{n-2} \ (n > 2)$  |

