

Spatial modeling using the sommer package

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The sommer package was developed to provide R users with a powerful and reliable multivariate mixed model solver for different genetic (in diploid and polyploid organisms) and non-genetic analyses. This package allows the user to estimate variance components in a mixed model with the advantages of specifying the variance-covariance structure of the random effects, specifying heterogeneous variances, and obtaining other parameters such as BLUPs, BLUEs, residuals, fitted values, variances for fixed and random effects, etc. The core algorithms of the package are coded in C++ using the Armadillo library to optimize dense matrix operations common in the direct-inversion algorithms.

This vignette is focused on showing the capabilities of sommer to fit spatial models using the two dimensional splines models.

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SECTION 1: Introduction

Backgrounds in tensor products

TBD

SECTION 2: Spatial models

1) Two dimensional splines (multiple spatial components)

In this example we show how to obtain the same results than using the SpATS package. This is achieved by using the `spl2Db` function which is a wrapper of the `tpsmb` function.

```
library(sommer)
data(DT_yatesoats)
DT <- DT_yatesoats
DT$row <- as.numeric(as.character(DT$row))
DT$col <- as.numeric(as.character(DT$col))
DT$R <- as.factor(DT$row)
DT$C <- as.factor(DT$col)
```

```
# SPATS MODEL
# m1.SpATS <- SpATS(response = "Y",
```

```

#           spatial = ~ PSANOVA(col, row, nseg = c(14,21), degree = 3, pord = 2),
#           genotype = "V", fixed = ~ 1,
#           random = ~ R + C, data = DT,
#           control = list(tolerance = 1e-04))
#
# summary(m1.SpATS, which = "variances")
#
# Spatial analysis of trials with splines
#
# Response:                Y
# Genotypes (as fixed):    V
# Spatial:                 ~PSANOVA(col, row, nseg = c(14, 21), degree = 3, pord = 2)
# Fixed:                   ~1
# Random:                  ~R + C
#
#
# Number of observations:   72
# Number of missing data:  0
# Effective dimension:     17.09
# Deviance:                483.405
#
# Variance components:
#
#           Variance          SD      log10(lambda)
# R           1.277e+02    1.130e+01    0.49450
# C           2.673e-05    5.170e-03    7.17366
# f(col)      4.018e-15    6.339e-08    16.99668
# f(row)      2.291e-10    1.514e-05    12.24059
# f(col):row  1.025e-04    1.012e-02    6.59013
# col:f(row)  8.789e+01    9.375e+00    0.65674
# f(col):f(row) 8.036e-04    2.835e-02    5.69565
#
# Residual      3.987e+02    1.997e+01
#
# SOMMER MODEL
m1.sommer <- mmer(Y~1+V+
                 spl2Db(col,row, nsegments = c(14,21), degree = c(3,3),
                       penaltyord = c(2,2), what = "base"),
                 random = ~R+C+
                 spl2Db(col,row, nsegments = c(14,21), degree = c(3,3),
                       penaltyord = c(2,2), what="bits"),
                 data=DT, tolParConv = 1e-6, verbose = FALSE)

```

Warning: fixed-effect model matrix is rank deficient so dropping 8 columns / coefficients

```
summary(m1.sommer)$varcomp
```

##	VarComp	VarCompSE	Zratio	Constraint
## R.Y-Y	125.928235	89.77330	1.4027360	Positive
## C.Y-Y	-7.789528	24.29529	-0.3206189	Positive
## A:fC.Y-Y	0.000000	19.09624	0.0000000	Positive
## A:fR.Y-Y	0.000000	15.87659	0.0000000	Positive
## A:fC.R.Y-Y	0.000000	21.42763	0.0000000	Positive
## A:C.fR.Y-Y	82.177296	92.28630	0.8904604	Positive
## A:fC.fR.Y-Y	0.000000	25.46390	0.0000000	Positive

```
## units.Y-Y 405.900386 90.48195 4.4859820 Positive
# get the fitted values for the spatial kernel and plot
# ff <- fitted.mmer(m1.sommer)
# DT$fit <- as.matrix(Reduce("+",ff$Zu[-c(1:2)]))
# lattice::levelplot(fit~row*col,data=DT)
```

2) Two dimensional splines (single spatial component)

To reduce the computational burden of fitting multiple spatial kernels `sommer` provides a single spatial kernel method through the `spl2Da` function. This as will be shown, can produce similar results to the more flexible model. Use the one that fits better your needs.

```
# SOMMER MODEL
m2.sommer <- mmer(Y~1+V,
  random = ~R+C+spl2Da(col,row, nsegments = c(14,21), degree = c(3,3), penaltyord = c(2,2),
  data=DT, tolParConv = 1e-6, verbose = FALSE)
summary(m1.sommer)$varcomp
```

##	VarComp	VarCompSE	Zratio	Constraint
## R.Y-Y	125.928235	89.77330	1.4027360	Positive
## C.Y-Y	-7.789528	24.29529	-0.3206189	Positive
## A:fC.Y-Y	0.000000	19.09624	0.0000000	Positive
## A:fR.Y-Y	0.000000	15.87659	0.0000000	Positive
## A:fC.R.Y-Y	0.000000	21.42763	0.0000000	Positive
## A:C.fR.Y-Y	82.177296	92.28630	0.8904604	Positive
## A:fC.fR.Y-Y	0.000000	25.46390	0.0000000	Positive
## units.Y-Y	405.900386	90.48195	4.4859820	Positive

```
# get the fitted values for the spatial kernel and plot
# ff <- fitted.mmer(m2.sommer)
# DT$fit <- as.matrix(Reduce("+",ff$Zu[-c(1:2)]))
# lattice::levelplot(fit~row*col,data=DT)
```

3) Spatial models in multiple trials at once

Sometimes we want to fit heterogeneous variance components when e.g., have multiple trials or different locations. The spatial models can also be fitted that way using the `at.var` and `at.levels` arguments. The first argument expects a variable that will define the levels at which the variance components will be fitted. The second argument is a way for the user to specify the levels at which the spatial kernels should be fitted if the user doesn't want to fit it for all levels (e.g., trials or fields).

```
DT2 <- rbind(DT,DT)
DT2$Y <- DT2$Y + rnorm(length(DT2$Y))
DT2$trial <- c(rep("A",nrow(DT)),rep("B",nrow(DT)))
head(DT2)
```

##	row	col	Y	N	V	B	MP	R	C	trial
##	1	1	91.79843	0.2	Victory	B2	Victory	1	1	A
##	2	1	61.85086	0	Victory	B2	Victory	2	1	A
##	3	1	120.55643	0.4	Marvellous	B2	Marvellous	3	1	A
##	4	1	143.55323	0.6	Marvellous	B2	Marvellous	4	1	A
##	5	1	149.01331	0.6	GoldenRain	B2	GoldenRain	5	1	A
##	6	1	106.56385	0.2	GoldenRain	B2	GoldenRain	6	1	A

```

# SOMMER MODEL
m3.sommer <- mmer(Y~1+V,
                 random = ~vsr(dsr(trial),R)+vsr(dsr(trial),C)+
                 spl2Da(col,row, nsegments = c(14,21), degree = c(3,3),
                 penaltyord = c(2,2), at.var = trial),
                 rcov = ~vsr(dsr(trial),units),
                 data=DT2, tolParConv = 1e-6, verbose = FALSE)
summary(m3.sommer)$varcomp

```

##	VarComp	VarCompSE	Zratio	Constraint
## A:R.Y-Y	107.48007	82.12826	1.3086855	Positive
## B:R.Y-Y	98.26652	80.47655	1.2210578	Positive
## A:C.Y-Y	144.95281	138.74448	1.0447465	Positive
## B:C.Y-Y	138.91292	134.98994	1.0290613	Positive
## A:all.Y-Y	403.81707	879.19318	0.4593041	Positive
## B:all.Y-Y	418.54730	901.30369	0.4643799	Positive
## A:units.Y-Y	385.64550	202.89149	1.9007475	Positive
## B:units.Y-Y	396.86541	208.15464	1.9065893	Positive

```

# get the fitted values for the spatial kernel and plot
# ff <- fitted.mmer(m3.sommer)
# DT2$fit <- as.matrix(Reduce("+",ff$Zu[-c(1:4)]))
# lattice::levelplot(fit~row*col|trial,data=DT2)

```

Literature

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