

Package ‘shorts’

November 21, 2023

Type Package

Title Short Sprints

Version 2.5.0

Description Create short sprint (<6sec) profiles using the split times or the radar gun data. Mono-exponential equation is used to estimate maximal sprinting speed (MSS), relative acceleration (TAU), and other parameters such us maximal acceleration (MAC) and maximal relative power (PMAX). These parameters can be used to predict kinematic and kinetics variables and to compare individuals. The modeling method utilized in this package is based on the works of Chelly SM, Denis C. (2001) <doi:10.1097/00005768-200102000-00024>, Clark KP, Rieger RH, Bruno RF, Stearne DJ. (2017) <doi:10.1519/JSC.0000000000002081>, Furusawa K, Hill AV, Parkinson JL (1927) <doi:10.1098/rspb.1927.0035>, Greene PR. (1986) <doi:10.1016/0025-5564(86)90063-5>, Samozino P. and Peyrot N., et al (2022) <doi:10.1111/sms.14097>, and Samozino P. (2018) <doi:10.1007/978-3-319-05633-3_11>.

URL <https://mladenjovanovic.github.io/shorts/>

BugReports <https://github.com/mladenjovanovic/shorts/issues>

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coef.shorts_model	<i>S3 method for extracting model parameters from shorts_model object</i>
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Description

S3 method for extracting model parameters from shorts_model object

Usage

```
## S3 method for class 'shorts_model'
coef(object, ...)
```

Arguments

object	shorts_model object
...	Extra arguments. Not used

Examples

```

split_distances <- c(10, 20, 30, 40, 50)
split_times <- create_timing_gates_splits(
  gates = split_distances,
  MSS = 10,
  MAC = 9,
  FD = 0.25,
  TC = 0
)

# Simple model
simple_model <- model_timing_gates(split_distances, split_times)
coef(simple_model)

```

 convert_FV

Convert Force-Velocity profile back to Acceleration-Velocity profile

Description

This function converts back the Force-Velocity (FV) profile to Acceleration-Velocity (AP) profile

Usage

```
convert_FV(F0, V0, bodymass = 75, inertia = 0, resistance = 0, ...)
```

Arguments

F0, V0	Numeric vectors. FV profile parameters
bodymass	Body mass in kg. Used to calculate relative power and forwarded to get_air_resistance
inertia	External inertia in kg (for example a weight vest, or a sled). Not included in the air resistance calculation
resistance	External horizontal resistance in Newtons (for example tether device or a sled friction resistance)
...	Forwarded to get_air_resistance for the purpose of calculation of air resistance and power

Value

A list with calculated MSS and MAC parameters

Examples

```

FVP <- make_FV_profile(7, 8.3, inertia = 10, resistance = 50)

convert_FV(FVP$F0, FVP$V0, inertia = 10, resistance = 50)

```

```
create_timing_gates_splits  
    Create Timing Gates Splits
```

Description

This function is used to generate timing gates splits with predetermined parameters

Usage

```
create_timing_gates_splits(  
  MSS,  
  MAC,  
  gates = c(5, 10, 20, 30, 40),  
  FD = 0,  
  TC = 0,  
  noise = 0  
)
```

Arguments

MSS, MAC	Numeric vectors. Model parameters
gates	Numeric vectors. Distances of the timing gates
FD	Numeric vector. Flying start distance. Default is 0
TC	Numeric vector. Time-correction added to split times (e.g., reaction time). Default is 0
noise	Numeric vector. SD of Gaussian noise added to the split times. Default is 0

Examples

```
create_timing_gates_splits(  
  gates = c(10, 20, 30, 40, 50),  
  MSS = 10,  
  MAC = 9,  
  FD = 0.5,  
  TC = 0  
)
```

find_functions	<i>Find functions</i>
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Description

Family of functions that serve a purpose of finding maximal value and critical distances and times at which power, acceleration or velocity drops below certain threshold.

find_peak_power_distance finds peak power and distance at which peak power occurs

find_peak_power_time finds peak power and time at which peak power occurs

find_velocity_critical_distance finds critical distance at which percent of MSS is achieved

find_velocity_critical_time finds critical time at which percent of MSS is achieved

find_acceleration_critical_distance finds critical distance at which percent of MAC is reached

find_acceleration_critical_time finds critical time at which percent of MAC is reached

find_power_critical_distance finds critical distances at which peak power over percent is achieved

find_power_critical_time finds critical times at which peak power over percent is achieved

Usage

```
find_peak_power_distance(MSS, MAC, inertia = 0, resistance = 0, ...)
```

```
find_peak_power_time(MSS, MAC, inertia = 0, resistance = 0, ...)
```

```
find_velocity_critical_distance(MSS, MAC, percent = 0.9)
```

```
find_velocity_critical_time(MSS, MAC, percent = 0.9)
```

```
find_acceleration_critical_distance(MSS, MAC, percent = 0.9)
```

```
find_acceleration_critical_time(MSS, MAC, percent = 0.9)
```

```
find_power_critical_distance(
  MSS,
  MAC,
  inertia = 0,
  resistance = 0,
  percent = 0.9,
  ...
)
```

```
find_power_critical_time(
  MSS,
  MAC,
  inertia = 0,
```

```

    resistance = 0,
    percent = 0.9,
    ...
)

```

Arguments

MSS, MAC	Numeric vectors. Model parameters
inertia	External inertia in kg (for example a weight vest, or a sled). Not included in the air resistance calculation
resistance	External horizontal resistance in Newtons (for example tether device or a sled friction resistance)
...	Forwarded to predict_power functions for the purpose of calculation of air resistance
percent	Numeric vector. Used to calculate critical distance. Default is 0.9

Value

find_peak_power_distance returns list with two elements: peak_power and distance at which peak power occurs

find_peak_power_time returns list with two elements: peak_power and time at which peak power occurs

References

Haugen TA, Tønnessen E, Seiler SK. 2012. The Difference Is in the Start: Impact of Timing and Start Procedure on Sprint Running Performance: *Journal of Strength and Conditioning Research* 26:473–479. DOI: 10.1519/JSC.0b013e318226030b.

Samozino P. 2018. A Simple Method for Measuring Force, Velocity and Power Capabilities and Mechanical Effectiveness During Sprint Running. In: Morin J-B, Samozino P eds. *Biomechanics of Training and Testing*. Cham: Springer International Publishing, 237–267. DOI: 10.1007/978-3-319-05633-3_11.

Examples

```

dist <- seq(0, 40, length.out = 1000)

velocity <- predict_velocity_at_distance(
  distance = dist,
  MSS = 10,
  MAC = 9
)

acceleration <- predict_acceleration_at_distance(
  distance = dist,
  MSS = 10,
  MAC = 9
)

```

```

# Use ... to forward parameters to the shorts::get_air_resistance
pwr <- predict_power_at_distance(
  distance = dist,
  MSS = 10,
  MAC = 9
  # bodyweight = 100,
  # bodyheight = 1.9,
  # barometric_pressure = 760,
  # air_temperature = 25,
  # wind_velocity = 0
)

# Find critical distance when 90% of MSS is reached
plot(x = dist, y = velocity, type = "l")
abline(h = 10 * 0.9, col = "gray")
abline(v = find_velocity_critical_distance(MSS = 10, MAC = 9), col = "red")

# Find critical distance when 20% of MAC is reached
plot(x = dist, y = acceleration, type = "l")
abline(h = 9 * 0.2, col = "gray")
abline(v = find_acceleration_critical_distance(MSS = 10, MAC = 9, percent = 0.2), col = "red")

# Find peak power and location of peak power
plot(x = dist, y = pwr, type = "l")

peak_pwr <- find_peak_power_distance(
  MSS = 10,
  MAC = 9
  # Use ... to forward parameters to the shorts::get_air_resistance
)
abline(h = peak_pwr$peak_power, col = "gray")
abline(v = peak_pwr$distance, col = "red")

# Find distance in which relative power stays over 75% of PMAX'
plot(x = dist, y = pwr, type = "l")
abline(h = peak_pwr$peak_power * 0.75, col = "gray")
pwr_zone <- find_power_critical_distance(MSS = 10, MAC = 9, percent = 0.75)
abline(v = pwr_zone$lower, col = "blue")
abline(v = pwr_zone$upper, col = "blue")

```

find_optimal_distance *Function that finds the distance at which the sprint, probe, or FV profile is optimal (i.e., equal to 100 perc)*

Description

Function that finds the distance at which the sprint, probe, or FV profile is optimal (i.e., equal to 100 perc)

Usage

```
find_optimal_distance(..., optimal_func = optimal_FV, min = 1, max = 60)
```

Arguments

...	Forwarded to selected optimal_func
optimal_func	Selected profile optimization function. Default is optimal_FV
min, max	Distance over which to find optimal profile distance

Value

Distance

Examples

```
MSS <- 10
MAC <- 8
bodymass <- 75

fv <- make_FV_profile(MSS, MAC, bodymass)

find_optimal_distance(
  F0 = fv$F0,
  V0 = fv$V0,
  bodymass = fv$bodymass,
  optimal_func = optimal_FV,
  method = "max"
)

find_optimal_distance(
  MSS = MSS,
  MAC = MAC,
  optimal_func = optimal_MSS_MAC
)

find_optimal_distance(
  MSS = MSS,
  MAC = MAC,
  optimal_func = probe_MSS_MAC
)
```

fitted.shorts_model *S3 method for returning predictions of shorts_model*

Description

S3 method for returning predictions of shorts_model

Usage

```
## S3 method for class 'shorts_model'
fitted(object, ...)
```

Arguments

```
object      shorts_model object
...         Extra arguments. Not used
```

Examples

```
split_distances <- c(10, 20, 30, 40, 50)
split_times <- create_timing_gates_splits(
  gates = split_distances,
  MSS = 10,
  MAC = 9,
  FD = 0.25,
  TC = 0
)

# Simple model
simple_model <- model_timing_gates(split_distances, split_times)
fitted(simple_model)
```

format_splits

Format Split Data

Description

Function formats split data and calculates split distances, split times and average split velocity

Usage

```
format_splits(distance, time)
```

Arguments

```
distance    Numeric vector
time       Numeric vector
```

Value

Data frame with the following columns:

```
split Split number
split_distance_start Distance at which split starts
split_distance_stop Distance at which split ends
```

split_distance Split distance
split_time_start Time at which distance starts
split_time_stop Time at which distance ends
split_time Split time
split_mean_velocity Mean velocity over split distance
split_mean_acceleration Mean acceleration over split distance

Examples

```

data("split_times")

john_data <- split_times[split_times$athlete == "John", ]

format_splits(john_data$distance, john_data$time)

```

get_air_resistance *Get Air Resistance*

Description

get_air_resistance estimates air resistance in Newtons

Usage

```

get_air_resistance(
  velocity,
  bodymass = 75,
  bodyheight = 1.75,
  barometric_pressure = 760,
  air_temperature = 25,
  wind_velocity = 0
)

```

Arguments

velocity	Instantaneous running velocity in meters per second (m/s)
bodymass	In kilograms (kg)
bodyheight	In meters (m)
barometric_pressure	In Torrs
air_temperature	In Celcius (C)
wind_velocity	In meters per second (m/s). Use negative number as head wind, and positive number as back wind

Value

Air resistance in Newtons (N)

References

Arsac LM, Locatelli E. 2002. Modeling the energetics of 100-m running by using speed curves of world champions. *Journal of Applied Physiology* 92:1781–1788. DOI: 10.1152/japphysiol.00754.2001.

Samozino P, Rabita G, Dorel S, Slawinski J, Peyrot N, Saez de Villarreal E, Morin J-B. 2016. A simple method for measuring power, force, velocity properties, and mechanical effectiveness in sprint running: Simple method to compute sprint mechanics. *Scandinavian Journal of Medicine & Science in Sports* 26:648–658. DOI: 10.1111/sms.12490.

van Ingen Schenau GJ, Jacobs R, de Koning JJ. 1991. Can cycle power predict sprint running performance? *European Journal of Applied Physiology and Occupational Physiology* 63:255–260. DOI: 10.1007/BF00233857.

Examples

```
get_air_resistance(  
  velocity = 5,  
  bodymass = 80,  
  bodyheight = 1.90,  
  barometric_pressure = 760,  
  air_temperature = 16,  
  wind_velocity = -0.5  
)
```

jb_morin

JB Morin Sample Dataset

Description

Sample radar gun data provided by Jean-Benoît Morin on his website. See <https://jbmorin.net/2017/12/13/a-spreadsheet-for-sprint-acceleration-force-velocity-power-profiling/> for more details.

Usage

```
data(jb_morin)
```

Format

Data frame with 2 variables and 232 observations:

time Time in seconds

velocity Velocity in m/s

Details

This dataset represents a sample data provided by Jean-Benoît Morin on a single individual running approximately 35m from a stand still position that is measured with the radar gun. Individual's body mass is 75kg, height is 1.72m. Conditions of the run are the following: air temperature 25C, barometric pressure 760mmHg, wind velocity 0m/s.

The purpose of including this dataset in the package is to check the agreement of the model estimates with Jean-Benoît Morin Microsoft Excel spreadsheet.

Author(s)

Jean-Benoît Morin
 Inter-university Laboratory of Human Movement Biology
 Saint-Étienne, France <https://jbmorin.net/>

References

Morin JB. 2017. A spreadsheet for Sprint acceleration Force-Velocity-Power profiling. Available at <https://jbmorin.net/2017/12/13/a-spreadsheet-for-sprint-acceleration-force-velocity-power-profiling/> (accessed October 27, 2020).

make_FV_profile	<i>Get Force-Velocity Profile</i>
-----------------	-----------------------------------

Description

Provides Force-Velocity (FV) profile modified using ideas by Pierre Samozino and JB-Morin, et al. (2016) and Pierre Samozino and Nicolas Peyror, et al (2021).

Usage

```
make_FV_profile(MSS, MAC, bodymass = 75, inertia = 0, resistance = 0, ...)
```

Arguments

MSS, MAC	Numeric vectors. Model parameters
bodymass	Body mass in kg. Used to calculate relative power and forwarded to get_air_resistance
inertia	External inertia in kg (for example a weight vest, or a sled). Not included in the air resistance calculation
resistance	External horizontal resistance in Newtons (for example tether device or a sled friction resistance)
...	Forwarded to get_air_resistance for the purpose of calculation of air resistance and power

Value

List containing the following elements:

bodymass Returned bodymass used in FV profiling

F0 Horizontal force when velocity=0

F0_rel F0 divided by bodymass

V0 Velocity when horizontal force=0

Pmax Maximal horizontal power

Pmax_rel Pmax divided by bodymass

FV_slope Slope of the FV profile. See References for more info

References

Samozino P, Rabita G, Dorel S, Slawinski J, Peyrot N, Saez de Villarreal E, Morin J-B. 2016. A simple method for measuring power, force, velocity properties, and mechanical effectiveness in sprint running: Simple method to compute sprint mechanics. *Scandinavian Journal of Medicine & Science in Sports* 26:648–658. DOI: 10.1111/sms.12490.

Samozino P, Peyrot N, Edouard P, Nagahara R, Jimenez-Reyes P, Vanwanseele B, Morin J. 2022. Optimal mechanical force-velocity profile for sprint acceleration performance. *Scandinavian Journal of Medicine & Science in Sports* 32:559–575. DOI: 10.1111/sms.14097.

Examples

```
data("jb_morin")

m1 <- model_radar_gun(time = jb_morin$time, velocity = jb_morin$velocity)

fv_profile <- make_FV_profile(
  MSS = m1$parameters$MSS,
  MAC = m1$parameters$MAC,
  bodyheight = 1.72,
  bodymass = 120,
)

fv_profile
```

Description

This function models the sprint instantaneous velocity using mono-exponential equation that estimates maximum sprinting speed (MSS) and relative acceleration (TAU). `velocity` is used as target or outcome variable, and `time` as predictor.

Usage

```

model_radar_gun(
  time,
  velocity,
  weights = 1,
  CV = NULL,
  use_observed_MSS = FALSE,
  control = minpack.lm::nls.lm.control(maxiter = 1000),
  na.rm = FALSE,
  ...
)

```

Arguments

time	Numeric vector
velocity	Numeric vector
weights	Numeric vector. Default is 1
CV	Should cross-validation be used to estimate model fit? Default is NULL. Otherwise use integer indicating number of folds. See Example for more information
use_observed_MSS	Should MSS be estimated from the observed velocity? Default is FALSE
control	Control object forwarded to nlsLM . Default is <code>minpack.lm::nls.lm.control(maxiter = 1000)</code>
na.rm	Logical. Default is FALSE
...	Forwarded to nlsLM function

Value

List object with the following elements:

parameters List with the following estimated parameters: MSS, TAU, MAC, PMAX, and TC

model_fit List with the following components: RSE, R_squared, minErr, maxErr, and RMSE

model Model returned by the [nlsLM](#) function

data Data frame used to estimate the sprint parameters, consisting of time, velocity, weights, and pred_velocity columns

References

Samozino P. 2018. A Simple Method for Measuring Force, Velocity and Power Capabilities and Mechanical Effectiveness During Sprint Running. In: Morin J-B, Samozino P eds. Biomechanics of Training and Testing. Cham: Springer International Publishing, 237–267. DOI: 10.1007/978-3-319-05633-3_11.

Examples

```
instant_velocity <- data.frame(  
  time = c(0, 1, 2, 3, 4, 5, 6),  
  velocity = c(0.00, 4.99, 6.43, 6.84, 6.95, 6.99, 7.00)  
)  
  
sprint_model <- with(  
  instant_velocity,  
  model_radar_gun(time, velocity)  
)  
  
print(sprint_model)  
coef(sprint_model)  
plot(sprint_model)
```

model_tether

Model Using Instantaneous Tether device

Description

This function models the sprint instantaneous velocity using mono-exponential equation that estimates maximum sprinting speed (MSS) and relative acceleration (TAU). velocity is used as target or outcome variable, and distance as predictor.

Usage

```
model_tether(  
  distance,  
  velocity,  
  weights = 1,  
  CV = NULL,  
  use_observed_MSS = FALSE,  
  control = minpack.lm::nls.lm.control(maxiter = 1000),  
  na.rm = FALSE,  
  ...  
)
```

Arguments

distance	Numeric vector
velocity	Numeric vector
weights	Numeric vector. Default is 1
CV	Should cross-validation be used to estimate model fit? Default is NULL. Otherwise use integer indicating number of folds. See Example for more information
use_observed_MSS	Should MSS be estimated from the observed velocity? Default is FALSE

control	Control object forwarded to <code>nlsLM</code> . Default is <code>minpack.lm::nls.lm.control(maxiter = 1000)</code>
na.rm	Logical. Default is FALSE
...	Forwarded to <code>nlsLM</code> function

Value

List object with the following elements:

parameters List with the following estimated parameters: MSS, TAU, MAC, and PMAX

model_fit List with the following components: RSE, R_squared, minErr, maxErr, and RMSE

model Model returned by the `nlsLM` function

data Data frame used to estimate the sprint parameters, consisting of distance, velocity, weights, and pred_velocity columns

Examples

```
distance <- c(5, 10, 20, 30, 40)
velocity <- predict_velocity_at_distance(distance, MSS = 10, MAC = 8)
m1 <- model_tether(distance = distance, velocity = velocity)
m1
plot(m1)
```

model_tether_DC

Model Using Instantaneous Tether device and Distance Correction

Description

This function models the sprint instantaneous velocity using mono-exponential equation that estimates maximum sprinting speed (MSS) and relative acceleration (TAU). velocity is used as target or outcome variable, and distance as predictor. Additional parameter DC, serving the intercept function, is estimated

Usage

```
model_tether_DC(
  distance,
  velocity,
  weights = 1,
  CV = NULL,
  use_observed_MSS = FALSE,
  control = minpack.lm::nls.lm.control(maxiter = 1000),
  na.rm = FALSE,
  ...
)
```


Arguments

distance	Numeric vector
velocity	Numeric vector
weights	Numeric vector. Default is 1
CV	Should cross-validation be used to estimate model fit? Default is NULL. Otherwise use integer indicating number of folds. See Example for more information
use_observed_MSS	Should MSS be estimated from the observed velocity? Default is FALSE
control	Control object forwarded to <code>nlsLM</code> . Default is <code>minpack.lm::nls.lm.control(maxiter = 1000)</code>
na.rm	Logical. Default is FALSE
...	Forwarded to <code>nlsLM</code> function

Value

List object with the following elements:

parameters List with the following estimated parameters: MSS, TAU, MAC, PMAX, and DC

model_fit List with the following components: RSE, R_squared, minErr, maxErr, and RMSE

model Model returned by the `nlsLM` function

data Data frame used to estimate the sprint parameters, consisting of distance, velocity, weights, and pred_velocity columns

Examples

```
distance <- c(5, 10, 20, 30, 40)

velocity <- predict_velocity_at_distance(distance = 0.5, MSS = 10, MAC = 8)

m1 <- model_tether_DC(distance = distance, velocity = velocity)

m1

plot(m1)
```

model_timing_gates *Models Using Timing Gates Split Times*

Description

These functions model the sprint split times using mono-exponential equation, where time is used as target or outcome variable, and distance as predictor.

`model_timing_gates` Provides the simplest model with estimated MSS and MAC parameters

`model_timing_gates_TC` Besides estimating MSS and MAC parameters, this function estimates additional parameter TC or time correction

`model_timing_gates_FD` In addition to estimating MSS and MAC parameters, this function estimates FD or flying distance

`model_timing_gates_FD_TC` Combines the approach of the `model_timing_gates_FD` with that one of `model_timing_gates_TC`. In other words, it add extra parameter TC to be estimated in the `model_timing_gates_FD` model

Usage

```
model_timing_gates(
  distance,
  time,
  weights = 1,
  LOOCV = FALSE,
  control = minpack.lm::nls.lm.control(maxiter = 1000),
  na.rm = FALSE,
  ...
)
```

```
model_timing_gates_TC(
  distance,
  time,
  weights = 1,
  LOOCV = FALSE,
  control = minpack.lm::nls.lm.control(maxiter = 1000),
  na.rm = FALSE,
  ...
)
```

```
model_timing_gates_FD(
  distance,
  time,
  weights = 1,
  FD = NULL,
  LOOCV = FALSE,
  control = minpack.lm::nls.lm.control(maxiter = 1000),
  na.rm = FALSE,
  ...
)
```

```
model_timing_gates_FD_TC(
  distance,
  time,
  weights = 1,
  FD = NULL,
  LOOCV = FALSE,
  control = minpack.lm::nls.lm.control(maxiter = 1000),
```

```

na.rm = FALSE,
...
)

```

Arguments

distance, time Numeric vector. Indicates the position of the timing gates and time measured

weights Numeric vector. Default is vector of 1. This is used to give more weight to particular observations. For example, use `1\distance` to give more weight to observations from shorter distances.

L00CV Should Leave-one-out cross-validation be used to estimate model fit? Default is FALSE

control Control object forwarded to `nlsLM`. Default is `minpack.lm::nls.lm.control(maxiter = 1000)`

na.rm Logical. Default is FALSE

... Extra parameters forwarded to `nlsLM` function

FD Use this parameter if you do not want the FD parameter to be estimated, but rather take the provided value

Value

List object with the following elements:

data Data frame used to estimate the sprint parameters, consisting of `distance`, `time`, `weights`, and `pred_time` columns

model Model returned by the `nlsLM` function

parameters List with the estimated parameters, of which the following are always returned: `MSS`, `TAU`, `MAC`, and `PMAX`

model_fit List with the following components: `RSE`, `R_squared`, `minErr`, `maxErr`, and `RMSE`

References

Haugen TA, Tønnessen E, Seiler SK. 2012. The Difference Is in the Start: Impact of Timing and Start Procedure on Sprint Running Performance: *Journal of Strength and Conditioning Research* 26:473–479. DOI: 10.1519/JSC.0b013e318226030b.

Jovanović, M., & Vescovi, J. 2022. shorts: An R Package for Modeling Short Sprints. *International Journal of Strength and Conditioning*, 2(1). <https://doi.org/10.47206/ijsc.v2i1.74>

Jovanović, M. 2023. Bias in estimated short sprint profiles using timing gates due to the flying start: Simulation study and proposed solutions. *Computer Methods in Biomechanics and Biomedical Engineering*, 1–11. <https://doi.org/10.1080/10255842.2023.2170713>

Examples

```

split_distances <- c(10, 20, 30, 40, 50)
split_times <- create_timing_gates_splits(
  gates = split_distances,
  MSS = 10,

```

```
MAC = 9,  
FD = 0.25,  
TC = 0  
)  
  
# Simple model  
simple_model <- model_timing_gates(split_distances, split_times)  
  
print(simple_model)  
coef(simple_model)  
plot(simple_model)  
  
# Model with correction of 0.3s  
model_with_correction <- model_timing_gates(split_distances, split_times + 0.3)  
  
print(model_with_correction)  
plot(model_with_correction)  
  
# Model with time_correction estimation  
model_with_TC <- model_timing_gates_TC(split_distances, split_times)  
  
print(model_with_TC)  
plot(model_with_TC)  
  
# Model with flying distance estimations  
model_with_FD <- model_timing_gates_FD(split_distances, split_times)  
  
print(model_with_FD)  
plot(model_with_FD)  
  
# Model with flying distance estimations and time correction  
model_with_FD_TC <- model_timing_gates_FD_TC(split_distances, split_times)  
  
print(model_with_FD_TC)  
plot(model_with_FD_TC)
```

optimal_functions *Optimal profile functions*

Description

Family of functions that serve a purpose of finding optimal sprint or force-velocity profile

optimal_FV finds "optimal" F_0 and V_0 where time at distance is minimized, while keeping the power the same

optimal_MSS_MAC finds "optimal" MSS and MAS where time at distance is minimized, while keeping the P_{max} the same

Usage

```

optimal_FV(
  distance,
  F0,
  V0,
  bodymass = 75,
  inertia = 0,
  resistance = 0,
  method = "max",
  ...
)

optimal_MSS_MAC(distance, MSS, MAC)

```

Arguments

distance	Numeric vector
F0, V0	Numeric vectors. FV profile parameters
bodymass	Body mass in kg
inertia	External inertia in kg (for example a weight vest, or a sled). Not included in the air resistance calculation
resistance	External horizontal resistance in Newtons (for example tether device or a sled friction resistance)
method	Method to be utilized. Options are "peak" and "max" (default)
...	Forwarded to get_air_resistance for the purpose of calculation of air resistance
MSS, MAC	Numeric vectors. Model parameters

Value

optimal_FV returns a data frame with the following columns

F0 Original F0
V0 Original V0
bodymass Bodymass
inertia Inertia
resistance Resistance
Pmax Maximal power estimated using $F0 * V0 / 4$
Pmax_rel Relative maximal power
slope FV profile slope
distance Distance
time Time to cover distance
Ppeak Peak power estimated quantitatively

Ppeak_rel Relative peak power
Ppeak_dist Distance at which peak power is manifested
Ppeak_time Time at which peak power is manifested
F0_optim Optimal F0
F0_coef Ratio between F0_optim an F0
V0_optim Optimal V0
V0_coef Ratio between V0_optim an V0
Pmax_optim Optimal maximal power estimated $F0_optim * V0_optim / 4$
Pmax_rel_optim Optimal relative maximal power
slope_optim Optimal FV profile slope
profile_imb Percent ratio between slope and optimal slope
time_optim Time to cover distance when profile is optimal
time_gain Difference in time to cover distance between time_optimal and time
Ppeak_optim Optimal peak power estimated quantitatively
Ppeak_rel_optim Optimal relative peak power
Ppeak_dist_optim Distance at which optimal peak power is manifested
Ppeak_time_optim Time at which optimal peak power is manifested

optimal_MSS_MAC returns a data frame with the following columns

MSS Original MSS
MAC Original MAC
Pmax_rel Relative maximal power estimated using $MSS * MAC / 4$
slope Sprint profile slope
distance Distance
time Time to cover distance
MSS_optim Optimal MSS
MSS_coef Ratio between MSS_optim an MSS
MAC_optim Optimal MAC
MAC_coef Ratio between MAC_optim an MAC
Pmax_rel_optim Optimal relative maximal power estimated using $MSS_optim * MAC_optim / 4$
slope_optim Optimal sprint profile slope
profile_imb Percent ratio between slope and optimal slope
time_optim Time to cover distance when profile is optimal
time_gain Difference in time to cover distance between time_optimal and time

References

Samozino P, Peyrot N, Edouard P, Nagahara R, Jimenez-Reyes P, Vanwanseele B, Morin J. 2022. Optimal mechanical force-velocity profile for sprint acceleration performance. *Scandinavian Journal of Medicine & Science in Sports* 32:559–575. DOI: 10.1111/sms.14097.

Examples

```
MSS <- 10
MAC <- 8
bodymass <- 75

fv <- make_FV_profile(MSS, MAC, bodymass)

dist <- seq(5, 40, by = 5)

opt_MSS_MAC_profile <- optimal_MSS_MAC(
  distance = dist,
  MSS,
  MAC
)[["profile_imb"]]

opt_FV_profile <- optimal_FV(
  distance = dist,
  fv$F0,
  fv$V0,
  fv$bodymass
)[["profile_imb"]]

opt_FV_profile_peak <- optimal_FV(
  distance = dist,
  fv$F0,
  fv$V0,
  fv$bodymass,
  method = "peak"
)[["profile_imb"]]

plot(x = dist, y = opt_MSS_MAC_profile, type = "l", ylab = "Profile imbalance")
lines(x = dist, y = opt_FV_profile, type = "l", col = "blue")
lines(x = dist, y = opt_FV_profile_peak, type = "l", col = "red")
abline(h = 100, col = "gray", lty = 2)
```

plot.shorts_model *S3 method for plotting shorts_model object*

Description

S3 method for plotting shorts_model object

Usage

```
## S3 method for class 'shorts_model'
plot(x, type = NULL, ...)
```

Arguments

x	shorts_model object
type	Not used
...	Not used

Value

ggplot object

Examples

```
split_times <- data.frame(
  distance = c(5, 10, 20, 30, 35),
  time = c(1.20, 1.96, 3.36, 4.71, 5.35)
)

# Simple model with time splits
simple_model <- with(
  split_times,
  model_timing_gates(distance, time)
)

coef(simple_model)
plot(simple_model)

# Simple model with radar gun data
instant_velocity <- data.frame(
  time = c(0, 1, 2, 3, 4, 5, 6),
  velocity = c(0.00, 4.99, 6.43, 6.84, 6.95, 6.99, 7.00)
)

radar_model <- with(
  instant_velocity,
  model_radar_gun(time, velocity)
)

# sprint_model$parameters
coef(radar_model)
plot(radar_model)
```

predict.shorts_model *S3 method for making predictions using shorts_model*

Description

S3 method for making predictions using shorts_model

Usage

```
## S3 method for class 'shorts_model'  
predict(object, ...)
```

Arguments

```
object      shorts_model object  
...        Forwarded to generic predict() function
```

Examples

```
split_distances <- c(10, 20, 30, 40, 50)  
split_times <- create_timing_gates_splits(  
  gates = split_distances,  
  MSS = 10,  
  MAC = 9,  
  FD = 0.25,  
  TC = 0  
)  
  
# Simple model  
simple_model <- model_timing_gates(split_distances, split_times)  
predict(simple_model)
```

predict_kinematics *Kinematics prediction functions*

Description

Predicts kinematic from known MSS and MAC parameters

Usage

```
predict_velocity_at_time(time, MSS, MAC)  
  
predict_distance_at_time(time, MSS, MAC)  
  
predict_acceleration_at_time(time, MSS, MAC)  
  
predict_time_at_distance(distance, MSS, MAC)  
  
predict_time_at_distance_FV(  
  distance,  
  F0,  
  V0,  
  bodymass = 75,  
  inertia = 0,
```

```
    resistance = 0,  
    ...  
)  
  
predict_velocity_at_distance(distance, MSS, MAC)  
  
predict_acceleration_at_distance(distance, MSS, MAC)  
  
predict_acceleration_at_velocity(velocity, MSS, MAC)  
  
predict_air_resistance_at_time(time, MSS, MAC, ...)  
  
predict_air_resistance_at_distance(distance, MSS, MAC, ...)  
  
predict_force_at_velocity(  
    velocity,  
    MSS,  
    MAC,  
    bodymass = 75,  
    inertia = 0,  
    resistance = 0,  
    ...  
)  
  
predict_force_at_time(  
    time,  
    MSS,  
    MAC,  
    bodymass = 75,  
    inertia = 0,  
    resistance = 0,  
    ...  
)  
  
predict_force_at_distance(  
    distance,  
    MSS,  
    MAC,  
    bodymass = 75,  
    inertia = 0,  
    resistance = 0,  
    ...  
)  
  
predict_power_at_distance(  
    distance,  
    MSS,  
    MAC,
```

```
    bodymass = 75,  
    inertia = 0,  
    resistance = 0,  
    ...  
)  
  
predict_power_at_time(  
    time,  
    MSS,  
    MAC,  
    bodymass = 75,  
    inertia = 0,  
    resistance = 0,  
    ...  
)  
  
predict_relative_power_at_distance(  
    distance,  
    MSS,  
    MAC,  
    bodymass = 75,  
    inertia = 0,  
    resistance = 0,  
    ...  
)  
  
predict_relative_power_at_time(  
    time,  
    MSS,  
    MAC,  
    bodymass = 75,  
    inertia = 0,  
    resistance = 0,  
    ...  
)  
  
predict_kinematics(  
    object = NULL,  
    MSS,  
    MAC,  
    max_time = 6,  
    frequency = 100,  
    bodymass = 75,  
    inertia = 0,  
    resistance = 0,  
    add_inertia_to_vertical = TRUE,  
    ...  
)
```

Arguments

time, distance, velocity	Numeric vectors
MSS, MAC	Numeric vectors. Model parameters
F0, V0	Numeric vectors. FV profile parameters
bodymass	Body mass in kg. Used to calculate relative power and forwarded to get_air_resistance
inertia	External inertia in kg (for example a weight vest, or a sled). Not included in the air resistance calculation
resistance	External horizontal resistance in Newtons (for example tether device or a sled friction resistance)
...	Forwarded to get_air_resistance for the purpose of calculation of air resistance and power
object	If <code>shorts_model</code> object is provided, estimated parameters will be used. Otherwise provide MSS and MAC parameters
max_time	Predict from 0 to max_time. Default is 6seconds
frequency	Number of samples within one second. Default is 100Hz
add_inertia_to_vertical	Should inertia be added to bodymass when calculating vertical force? Use TRUE (Default) when using weight vest, and FALSE when dragging sled

Value

Numeric vector
Data frame with kinetic and kinematic variables

References

Haugen TA, Tønnessen E, Seiler SK. 2012. The Difference Is in the Start: Impact of Timing and Start Procedure on Sprint Running Performance: *Journal of Strength and Conditioning Research* 26:473–479. DOI: 10.1519/JSC.0b013e318226030b.

Jovanović, M., Vescovi, J.D. (2020). `shorts`: An R Package for Modeling Short Sprints. Preprint available at SportRxiv. <https://doi.org/10.31236/osf.io/4jw62>

Samozino P. 2018. A Simple Method for Measuring Force, Velocity and Power Capabilities and Mechanical Effectiveness During Sprint Running. In: Morin J-B, Samozino P eds. *Biomechanics of Training and Testing*. Cham: Springer International Publishing, 237–267. DOI: 10.1007/978-3-319-05633-3_11.

Examples

```
MSS <- 8
MAC <- 9

time_seq <- seq(0, 6, length.out = 10)

df <- data.frame(
```

```

    time = time_seq,
    distance_at_time = predict_distance_at_time(time_seq, MSS, MAC),
    velocity_at_time = predict_velocity_at_time(time_seq, MSS, MAC),
    acceleration_at_time = predict_acceleration_at_time(time_seq, MSS, MAC)
  )

df$time_at_distance <- predict_time_at_distance(df$distance_at_time, MSS, MAC)
df$velocity_at_distance <- predict_velocity_at_distance(df$distance_at_time, MSS, MAC)
df$acceleration_at_distance <- predict_acceleration_at_distance(df$distance_at_time, MSS, MAC)
df$acceleration_at_velocity <- predict_acceleration_at_velocity(df$velocity_at_time, MSS, MAC)

# Power calculation uses shorts::get_air_resistance function and its defaults
# values to calculate power. Use the ... to setup your own parameters for power
# calculations
df$power_at_time <- predict_power_at_time(
  time = df$time, MSS = MSS, MAC = MAC,
  # Check shorts::get_air_resistance for available params
  bodymass = 100, bodyheight = 1.85
)

df

# Example for predict_kinematics
split_times <- data.frame(
  distance = c(5, 10, 20, 30, 35),
  time = c(1.20, 1.96, 3.36, 4.71, 5.35)
)

# Simple model
simple_model <- with(
  split_times,
  model_timing_gates(distance, time)
)

predict_kinematics(simple_model)

```

print.shorts_model *S3 method for printing shorts_model object*

Description

S3 method for printing shorts_model object

Usage

```
## S3 method for class 'shorts_model'
print(x, ...)
```

Arguments

x shorts_model object
 ... Not used

Examples

```
split_distances <- c(10, 20, 30, 40, 50)
split_times <- create_timing_gates_splits(
  gates = split_distances,
  MSS = 10,
  MAC = 9,
  FD = 0.25,
  TC = 0
)

# Simple model
simple_model <- model_timing_gates(split_distances, split_times)
simple_model
```

 probe_functions

Probe profile functions

Description

Family of functions that serve a purpose of probing sprint or force-velocity profile. This is done by increasing individual sprint parameter for a percentage and calculating which parameter improvement yield biggest deduction in sprint tim

probe_FV "probes" F_0 and V_0 and calculates which one improves sprint time for a defined distance

probe_MSS_MAC "probes" MSS and MAC and calculates which one improves sprint time for a defined distance

Usage

```
probe_FV(
  distance,
  F0,
  V0,
  bodymass = 75,
  inertia = 0,
  resistance = 0,
  perc = 2.5,
  ...
)

probe_MSS_MAC(distance, MSS, MAC, perc = 2.5)
```

Arguments

distance	Numeric vector
F0, V0	Numeric vectors. FV profile parameters
bodymass	Body mass in kg
inertia	External inertia in kg (for example a weight vest, or a sled). Not included in the air resistance calculation
resistance	External horizontal resistance in Newtons (for example tether device or a sled friction resistance)
perc	Numeric vector. Probing percentage. Default is 2.5 percent
...	Forwarded to predict_power_at_distance for the purpose of calculation of air resistance
MSS, MAC	Numeric vectors. Model parameters

Value

probe_FV returns a data frame with the following columns

F0 Original F0

V0 Original V0

bodymass Bodymass

inertia Inertia

resistance Resistance

Pmax Maximal power estimated using $F0 * V0 / 4$

Pmax_rel Relative maximal power

slope FV profile slope

distance Distance

time Time to cover distance

probe_perc Probe percentage

F0_probe Probing F0

F0_probe_time Predicted time for distance when F0 is probed

F0_probe_time_gain Difference in time to cover distance between time_optimal and time

V0_probe Probing V0

V0_probe_time Predicted time for distance when V0 is probed

V0_probe_time_gain Difference in time to cover distance between time_optimal and time

profile_imb Percent ratio between V0_probe_time_gain and F0_probe_time_gain

probe_MSS_MAC returns a data frame with the following columns

MSS Original MSS

MAC Original MAC

Pmax_rel Relative maximal power estimated using $MSS * MAC / 4$

slope Sprint profile slope
distance Distance
time Time to cover distance
probe_perc Probe percentage
MSS_probe Probing MSS
MSS_probe_time Predicted time for distance when MSS is probed
MSS_probe_time_gain Difference in time to cover distance between probe time and time
MAC_probe Probing MAC
MAC_probe_time Predicted time for distance when MAC is probed
MAC_probe_time_gain Difference in time to cover distance between probing time and time
profile_imb Percent ratio between MSS_probe_time_gain and MAC_probe_time_gain

Examples

```

MSS <- 10
MAC <- 8
bodymass <- 75

fv <- make_FV_profile(MSS, MAC, bodymass)

dist <- seq(5, 40, by = 5)

probe_MSS_MAC_profile <- probe_MSS_MAC(
  distance = dist,
  MSS,
  MAC
)[["profile_imb"]]

probe_FV_profile <- probe_FV(
  distance = dist,
  fv$F0,
  fv$V0,
  fv$bodymass
)[["profile_imb"]]

plot(x = dist, y = probe_MSS_MAC_profile, type = "l", ylab = "Profile imbalance")
lines(x = dist, y = probe_FV_profile, type = "l", col = "blue")
abline(h = 100, col = "gray", lty = 2)

```

radar_gun_data

Radar Gun Data

Description

Data generated from known MSS and TAU and measurement error for N=5 athletes using radar gun with sampling frequency of 100Hz over 6 seconds.

Usage

```
data(radar_gun_data)
```

Format

Data frame with 4 variables and 3000 observations:

athlete Character string

bodyweight Bodyweight in kilograms

time Time reported by the radar gun in seconds

velocity Velocity reported by the radar gun in m/s

```
residuals.shorts_model
```

S3 method for providing residuals for the shorts_model object

Description

S3 method for providing residuals for the shorts_model object

Usage

```
## S3 method for class 'shorts_model'  
residuals(object, ...)
```

Arguments

object	shorts_model object
...	Not used

Examples

```
split_distances <- c(10, 20, 30, 40, 50)  
split_times <- create_timing_gates_splits(  
  gates = split_distances,  
  MSS = 10,  
  MAC = 9,  
  FD = 0.25,  
  TC = 0  
)  
  
# Simple model  
simple_model <- model_timing_gates(split_distances, split_times)  
residuals(simple_model)
```

split_times	<i>Split Testing Data</i>
-------------	---------------------------

Description

Data generated from known MSS and TAU and measurement error for N=5 athletes using 6 timing gates: 5m, 10m, 15m, 20m, 30m, 40m

Usage

```
data(split_times)
```

Format

Data frame with 4 variables and 30 observations:

athlete Character string

bodyweight Bodyweight in kilograms

distance Distance of the timing gates from the sprint start in meters

time Time reported by the timing gate

summary.shortcuts_model	<i>S3 method for providing summary for the shortcuts_model object</i>
-------------------------	---

Description

S3 method for providing summary for the shortcuts_model object

Usage

```
## S3 method for class 'shortcuts_model'
summary(object, ...)
```

Arguments

object	shortcuts_model object
...	Not used

Examples

```

split_distances <- c(10, 20, 30, 40, 50)
split_times <- create_timing_gates_splits(
  gates = split_distances,
  MSS = 10,
  MAC = 9,
  FD = 0.25,
  TC = 0
)

# Simple model
simple_model <- model_timing_gates(split_distances, split_times)
summary(simple_model)

```

vescovi

*Vescovi Timing Gates Sprint Times***Description**

Timing gates sprint times involving 52 female athletes. Timing gates were located at 5m, 10m, 20m, 30m, and 35m. See **Details** for more information.

Usage

```
data(vescovi)
```

Format

Data frame with 17 variables and 52 observations:

Team Team or sport. Contains the following levels: 'W Soccer' (Women Soccer), 'FH Sr' (Field Hockey Seniors), 'FH U21' (Field Hockey Under 21), and 'FH U17' (Field Hockey Under 17)

Surface Type of testing surface. Contains the following levels: 'Hard Cours' and 'Natural Grass'

Athlete Athlete ID

Age Athlete age in years

Height Body height in cm

Bodyweight Body weight in kg

BMI Body Mass Index

BSA Body Surface Area. Calculated using Mosteller equation $\sqrt{(\text{height}/\text{weight})/3600}$

5m Time in seconds at 5m gate

10m Time in seconds at 10m gate

20m Time in seconds at 20m gate

30m Time in seconds at 30m gate

35m Time in seconds at 35m gate

10m-5m split Split time in seconds between 10m and 5m gate

20m-10m split Split time in seconds between 20m and 10m gate

30m-20m split Split time in seconds between 30m and 20m gate

35m-30m split Split time in seconds between 35m and 30m gate

Details

This data-set represents sub-set of data from a total of 220 high-level female athletes (151 soccer players and 69 field hockey players). Using a random number generator, a total of 52 players (35 soccer and 17 field hockey) were selected for this data-set. Soccer players were older (24.6 ± 3.6 vs. 18.9 ± 2.7 yr, $p < 0.001$), however there were no differences for height (167.3 ± 5.9 vs. 167.0 ± 5.7 cm, $p = 0.886$), body mass (62.5 ± 5.9 vs. 64.0 ± 9.4 kg, $p = 0.500$) or any sprint interval time ($p > 0.650$).

The protocol for assessing linear sprint speed has been described previously (Vescovi 2014, 2016, 2012) and was identical for each cohort. Briefly, all athletes performed a standardized warm-up that included general exercises such as jogging, shuffling, multi-directional movements, and dynamic stretching exercises. Infrared timing gates (Brower Timing, Utah) were positioned at the start line and at 5, 10, 20, and 35 meters at a height of approximately 1.0 meter. Participants stood with their lead foot positioned approximately 5 cm behind the initial infrared beam (i.e., start line). Only forward movement was permitted (no leaning or rocking backwards) and timing started when the laser of the starting gate was triggered. The best 35 m time, and all associated split times were kept for analysis. The assessment of linear sprints using infrared timing gates does not require familiarization (Moir, Button, Glaister, and Stone 2004).

Author(s)

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Vescovi JD (2016). "Locomotor, Heart-Rate, and Metabolic Power Characteristics of Youth Women's Field Hockey: Female Athletes in Motion (FAiM) Study." *Research Quarterly for Exercise and Sport*, 87(1), 68-77. ISSN 0270-1367, 2168-3824. doi:10.1080/02701367.2015.1124972.

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