## Using asremlPlus, in conjunction with asreml, to do the analysis of a wheat experiment that includes choosing a local spatial variation model using AICs

## Chris Brien

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This vignette shows how to use asremlPlus (Brien, 2024), in conjunction with asreml (Butler et al., 2023), to select the terms to be included in a mixed model for an experiment that involves spatial variation by comparing of information criteria. It also illustrates diagnostic checking and prediction production and presentation for this experiment. Here, asremlPlus and asreml are packages for the R Statistical Computing environment (R Core Team, 2024).

It is divided into the following main sections:

- 1. Set up the initial model for this experiment
- 2. Compare a series of information criteria to select a linear mixed model for the data
- 3. Diagnostic checking using residual plots and variofaces
- 4. Prediction production and presentation

## 1. Set up the initial model for this experiment

```
library(asreml, quietly=TRUE)
```

## Offline License checked out Thu Apr 11 09:26:08 2024

## Loading ASReml-R version 4.2

```
library(asremlPlus)
library(parallel)
library(doParallel)
```

## Loading required package: foreach

## Loading required package: iterators

```
library(foreach)
suppressMessages(library(qqplotr, quietly=TRUE))
options(width = 100)
```

### Get data available in asremlPlus

The data are from a 1976 spring wheat experiment and are taken from Gilmour et al. (1995). An analysis is presented in the asreml manual by Butler et al. (2023, Section 7.6), although they suggest that it is a barley experiment.

data(Wheat.dat)

### Add row and column covariates for the spatial modelling

## Fit an initial model - Row and column random

In the following, an initial model is fitted that has the terms that would be included for a balanced lattice. In addition, a term WithinColPairs has been included to allow for extraneous variation arising between pairs of adjacent lanes.

##	ASReml	Version 4.2	11/04/2024 09:	26:09	
##		LogLik	Sigma2	DF	wall
##	1	-702.7015	26232.20	119	09:26:09
##	2	-700.4838	24394.12	119	09:26:09
##	3	-698.4908	22487.75	119	09:26:09
##	4	-697.5842	21242.11	119	09:26:09
##	5	-697.3673	20590.05	119	09:26:09
##	6	-697.3595	20477.28	119	09:26:09

### Intialize a model sequence by loading the current fit into an asrtests object

In creating the asrtests object, IClikelihood is set to full so that the full Restricted Maximum Likelihood (full REML) of Verbyla, 2019 is incorporated into the tests.summary of the asrtests object.

## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, :
## Log-likelihood not converged

Check for and remove any boundary terms and print a summary of the fit in the asrtests object

```
current.asrt <- rmboundary(current.asrt)</pre>
print(current.asrt)
##
##
## #### Summary of the fitted variance parameters
##
##
                component std.error z.ratio bound %ch
                 5943.898 3815.514 1.557824
                                                 P 0.0
## Row
                12380.527 6323.542 1.957847
                                                 P 0.3
## Column
## Row:Column!R 20477.280 2896.642 7.069316
                                                 P 0.0
##
##
## #### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: yield
##
##
                  Df denDF
                             F.inc
                                       Pr
                   1 14.9 1390.00 0.0000
## (Intercept)
## Rep
                   5 25.3
                              6.04 0.0008
                              0.49 0.4998
## WithinColPairs 1 10.4
## Variety
                  24 104.8
                              4.71 0.0000
##
##
## #### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
             terms DF denDF p
##
                                             BIC
                                    AIC
                                                          action
## 1 Initial model 31
                          3 NA 1720.891 1823.253 Starting model
```

The test.summary output shows that no changes have been made to the model loaded using as.asrtests. The pseudo-anova table shows that Varieties are highly significant (p < 0.001)

# 2. Compare a series of information criteria to select a linear mixed model for the data

In this section, models are compared using Akaike Information Criterion (AICs) based on the full REML.

Check the need for the term for within Column pairs (a post hoc factor)

## ASReml Version 4.2 11/04/2024 09:26:10 ## LogLik Sigma2 DF wall ## 1 -697.359520472.09 119 09:26:10 ## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : ## Log-likelihood not converged print(current.asrt) ## ## ## #### Summary of the fitted variance parameters ## ## component std.error z.ratio bound %ch ## Row 5941.153 3813.586 1.557891 Ρ 0 11165.335 5583.267 1.999785 Ρ 0 ## Column Row:Column!R 20472.402 Ρ 0 ## 2895.582 7.070219 ## ## #### Pseudo-anova table for fixed terms ## ## ## ## Wald tests for fixed effects. ## Response: yield ## ## Df denDF F.inc Pr ## (Intercept) 1 15.3 1466.00 0e+00 ## Rep 5 26.7 6.11 7e-04 ## Variety 24 105.3 4.73 0e+00 ## ## Sequence of model investigations ## #### ## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers) ## ## ## terms DF denDF AIC BIC action р ## 1 Initial model 31 3 NA 1720.89134 1823.252944 Starting model ## 2 Try dropping withinColPairs -1 O NA -2.28193-5.292565 Swapped

It is clear in the call to changeModelOnIC that the model is being changed by dropping the withinColPairs term, which could also be achieved using update.asreml. However, an asremlPlus model-changing function operates on an asrtests object, that includes an asreml object, and, except for changeTerms.asrtests, results in an asrtests object that may contain the changed model or the supplied model depending on the results of hypothesis tests or comparisons of information criteria. In addition, the result of the test or comparison will be added to a test.summary data.frame stored in the new asrtests object and, if the model was changed, the wald.tab in the new asrtests object will have been updated for the new model.

In this case, as can be seen from the summary of current.asrt after the call, the model without withinColPairs had a smaller AIC and so now the model stored in current.asrt does not include withinColPAirs. The wald.tab has been updated for the new model.

#### Choose a model for local spatial variation from several potential models

This example has been analyzed using a model for the local spatial variation based on a separable autocorrelation process of order one (Butler et al., 2023). The need for this model can be assessed using the function addSpatialModelOnIC from asremlPlus that uses a forward selection strategy for fitting a correlation model (see output below). For this function, the spatial model to be fitted, the centred covariates for the two dimensions of the grid, and the factors corresponding to the covariates must be specified. Also, IClikelihood is set to full so that the likelihood will be based on the full REML. Because the model that incorporates the spatial model has a smaller AIC, it is the model returned in spatial.ar1.asrt.

The print of spatial.ar1.asrt shows that an ar1 model for Row was tried first and was found to reduce the AIC by 11.898 and so became the current model. Next a model that incorporates an ar1 function for Column was similarly tried and became the current model. This model includes a nugget variance, unless either the variance for Row:Column term or the Residual is bound or fixed. The Residual is the nugget term and represents non-spatial variance, such as measurement error. An appraisal of the need for a nugget term was made by comparing the fits with the residual variance unfixed and fixed at one. The model with the unfixed residual variance was chosen and is the model to be returned. That is, this model includes a term for nugget variance.

## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some ## components changed by more than 1% on the last iteration ## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some ## components changed by more than 1% on the last iteration ## Warning in infoCriteria.asreml(asreml.obj, IClikelihood = ic.lik, bound.exclusions = bound.exclusion ## Column ## Warning in infoCriteria.asreml(asreml.obj, IClikelihood = ic.lik): The following bound terms were di ## Column ## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Warning : ## Oscillating parameter(s) reset to average value (iteration 7) ## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Warning : ## Oscillating parameter(s) reset to average value (iteration 7) ## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : ## Log-likelihood not converged ## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some ## components changed by more than 1% on the last iteration ## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Warning : ## Oscillating parameter(s) reset to average value (iteration 7) ## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Warning : ## Oscillating parameter(s) reset to average value (iteration 7)

```
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, :
## Log-likelihood not converged
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration
## Warning in newfit.asreml(asreml.obj, random. = mod.ran, trace = trace, update = update, :
## Warning in changeTerms.asrtests(asrtests.obj, dropFixed = dropFixed, addFixed = addFixed, : In
## analysing yield, boundary terms removed
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration
## Warning in infoCriteria.asreml(asreml.obj, IClikelihood = ic.lik, bound.exclusions = bound.exclusion
## Row:Column!R
## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, IClikelihood = ic.lik, : The following b
## Row:Column!R
spatial.ar1.asrt <- rmboundary(spatial.ar1.asrt)</pre>
infoCriteria(list(nonspatial = current.asrt$asreml.obj,
                  ar1 = spatial.ar1.asrt$asreml.obj))
##
              fixedDF varDF NBound
                                        AIC
                                                 BIC
                                                        loglik
## nonspatial
                    0
                          3
                                 0 1409.023 1417.386 -701.5117
## ar1
                    0
                          5
                                 0 1353.762 1367.700 -671.8811
print(spatial.ar1.asrt)
##
##
## #### Summary of the fitted variance parameters
```

```
##
                                                      z.ratio bound %ch
##
                            component
                                         std.error
## Row
                         2.202326e+03 8.222412e+03 0.2678443
                                                                  P 0.3
## Row:Column
                         5.181864e+04 3.381226e+04 1.5325399
                                                                  P 0.0
## Row:Column!Row!cor
                         7.121302e-01 9.570910e-02 7.4405694
                                                                  U 0.0
## Row:Column!Column!cor 8.599232e-01 1.103950e-01 7.7895102
                                                                  U 0.0
## Row:Column!R
                         4.821622e+03 1.717158e+03 2.8079077
                                                                  P 0.0
##
##
## #### Pseudo-anova table for fixed terms
##
##
```

## Wald tests for fixed effects. ## Response: yield ## ## F.inc Pr Df denDF ## (Intercept) 1 1.8 194.600 0.0076 5 21.9 Rep 0.559 0.7303 ## ## Varietv 24 74.2 10.560 0.0000 ## ## ## #### Sequence of model investigations ## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers) ## ## terms DF denDF ## р AIC BIC action ## 1 3 NA 1720.891344 1823.252944 Starting model Initial model 31 ## 2 Try dropping withinColPairs -1 O NA -2.281930 -5.292565 Swapped ## 3 2 NA Try ar1(Row) 0 -11.897710 -5.876439 Swapped ## 4 Try ar1(Column) 0 O NA -55.371326 -55.371326 Swapped ## 5 Column 1 NA NA 1651.310695 1756.682931 Boundary ## 6 Try fixed nugget (residual) variance 0 -1 NA 1.802928 -1.207707Unswapped

However, the spatial models that are available in asremlPlus also include those based on two-dimensional tensor-product natural cubic smoothing splines (TPNCSS), as described by Verbyla et al. (2018), and on two-dimensional tensor-product P-splines (TPPS), as described by Rodriguez-Alvarez et al. (2018) and Piepho, Boer and Williams (2022). The P-splines have been implemented using functions from the R package TPSbits authored by Sue Welham (2022)

The asremlPlus function chooseSpatialModelOnIC allows one to select the best model from amongst these spatial correlation models using the AIC or the BIC, the AIC being the default. The four models from which it selects are (i) a separable autocorrelation model on both row and column dimensions (corr), (ii) a two-dimensional tensor-product natural cubic smoothing spline (TPNCSS), (ii) a two-dimensional tensor-product cubic P-spline with second-difference penalties (TPPSC2), and (iii) a tensor-product two-dimensional linear P-spline with first-difference penalties (TPPSL1). By default all four are fitted and compared, but the trySpatial argument can be used to specify a subset of them.

The call to chooseSpatialModelOnIC, in addition to the arguments specifying covariates and factors, has further arguments: (i) dropFixed and dropRandom that are relevant to fitting P-splines and are used here to remove the random, overall Row and Column terms that were included in the original model so that the fitted P-spline model will be compared to a model including them and because the code for fitting P-splines also automatically includes these terms so that they would be included twice in the model to be fitted resulting in model singularities, (ii) rotateX and ngridangles so that the angles in both row and column directions for rotating the eigenvectors of the penalty matrix for the linear component of the P-splines is optimized (setting ngridangles to NULL causes the R function nloptr::bobyqa to be invoked for finding the optimal angles), (iii) an asreml.option argument to specify that the grp method be used in fitting the P-spline terms, this being safer because the data.frame needed for any post-fitting computation is available in the asreml object, and (iv) return.asrts to specify which asrtests objects are to be returned. Here we specify all so that asrtests objects for the best fits between the model supplied in the current.asrt and each of the spatial models is returned for all four spatial models. In this case, neither the checkboundaryonly nor the IClikelihood arguments were set because their defaults for chooseSpatialModelOnIC are appropriate.

```
suppressWarnings(
```

```
spatial.asrts <- chooseSpatialModelOnIC(current.asrt,</pre>
```

```
row.covar = "cRow", col.covar = "cColumn",
row.factor = "Row", col.factor = "Column",
dropRandom = "Row + Column",
```

rotateX = TRUE, ngridangles = NULL, asreml.option = "grp", return.asrts = "all"))

## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .001400 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .001400 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .001400 have been merged ## Notice : Spline design points closer than .001400 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .001400 have been merged ## Notice : Spline design points closer than .000900 have been merged ## elapsed time for bobyqa: 15.62 seconds ## ## #### Optimal thetas: 20.2026926907242, 64.9728898361927 with criterion 1659.433 ## ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .001400 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .001400 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .001400 have been merged ## Notice : Spline design points closer than .000900 have been merged ## Notice : Spline design points closer than .001400 have been merged ## Notice : Spline design points closer than .000900 have been merged

### Output the results

print(spatial.asrts\$spatial.IC)

##	fixedDF	varDF	AIC	BIC	loglik
## nonspatial	30	3	1718.609	1817.960	-826.3047
## corr	30	5	1651.317	1756.689	-790.6583
## TPNCSS	33	6	1639.489	1756.904	-780.7445
## TPPSC2	33	7	1642.838	1763.263	-781.4190
## TPPSL1	30	3	1708.443	1807.794	-821.2214

print(R2adj(spatial.asrts\$asrts\$TPNCSS\$asreml.obj, include.which.random = ~ .))

## ASReml Version 4.2 11/04/2024 09:27:03 ## LogLik Sigma2 DF wall ## 1 -662.1988 7657.986 117 09:27:03 -662.1988 7657.984 09:27:03 ## 2 117 ## 3 -662.1988 7657.977 117 09:27:03 ## 4 -662.1988 7657.975 117 09:27:03 ## 5 -662.1988 7657.975 09:27:03 117 -662.1988 ## 6 7657.974 09:27:03 117 -662.1988 7657.974 117 09:27:03 ## 7 ## Notice : Spline design points closer than .001400 have been merged ## Notice : Spline design points closer than .000900 have been merged ## [1] 93.3036 ## attr(,"fixed") ## ~. ## <environment: 0x0000014e4f076718> ## attr(,"random") ## ~. print(spatial.asrts\$best.spatial.mod) ## [1] "TPNCSS" print(spatial.asrts\$asrts\$TPNCSS) ## ## ## #### Summary of the fitted variance parameters ## ## component std.error z.ratio bound %ch ## spl(cRow):cColumn 523.2004 372.8016 1.403429 Ρ 0 ## dev(cRow) 7664.0211 4442.0646 1.725329 Ρ 0 ## spl(cColumn) 13338.7348 9236.0511 1.444203 Ρ 0 ## spl(cColumn):cRow 366.7707 322.7484 1.136399 Ρ 0 ## spl(cRow):spl(cColumn) 3630.2187 2186.1497 1.660554 Ρ 0 ## Row:Column!R 7658.0113 1312.2026 5.835998 Ρ 0 ## ## ## #### Pseudo-anova table for fixed terms ## ## ## Wald tests for fixed effects. **##** Response: yield ## ## Df denDF F.inc Pr ## (Intercept) 1 6.8 2645.00 0.0000 5 41.3 20.45 0.0000 ## Rep ## Variety 24 86.5 10.15 0.0000 0.07 0.7954 7.0 ## cRow 1 ## cColumn 1 30.1 20.30 0.0001

## cRow:cColumn 1 64.3 22.00 0.0000 ## ## Sequence of model investigations ## #### ## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers) ## ## ## terms DF denDF p AIC BIC action ## 1 Initial model 31 3 NA 1720.89134 1823.252944 Starting model ## 2 Try dropping withinColPairs -1 O NA -2.28193-5.292565 Swapped ## 3 Try tensor NCS splines 3 NA -79.12043 -61.056614 Swapped 3 dev(cColumn) ## 4 1 NA NA 1639.48896 1756.903736 Boundary ## 5 spl(cRow) 1 NA NA 1639.48901 1756.903788 Boundary printFormulae(spatial.asrts\$asrts\$TPNCSS\$asreml.obj) ## ## ## #### Formulae from asreml object ## ## fixed: yield ~ Rep + Variety + cRow + cColumn + cRow:cColumn ## random: ~ spl(cColumn) + dev(cRow) + spl(cRow):cColumn + spl(cColumn):cRow + spl(cRow):spl(cColumn) ## residual: ~ Row:Column

The output shows that the TPNCSS model has the lowest AIC and so is selected as the best model. The adjusted  $R^2$  value shows that the fixed and random terms in the fitted model account for 93% of the total variation in the yield. The model fitted for the TPNCSS model has been printed using printFormulae.asreml. The fitted model includes the term dev(cRow) that is equivalent to a random Row term and measures the deviations of the Row trend from a linear trend, the spl(cRow) term having been dropped because it was estimated to be zero. The Wald *F*-statistic for Variety is now 10.15 with 86.5 denominator degrees of freedom, as compared to 10.56 and 74.3 for the correlation model and 4.71 and 105.3 for the initial nonspatial model.

## 3. Diagnosting checking using residual plots and variofaces

Get current fitted asreml object and update to include standardized residuals

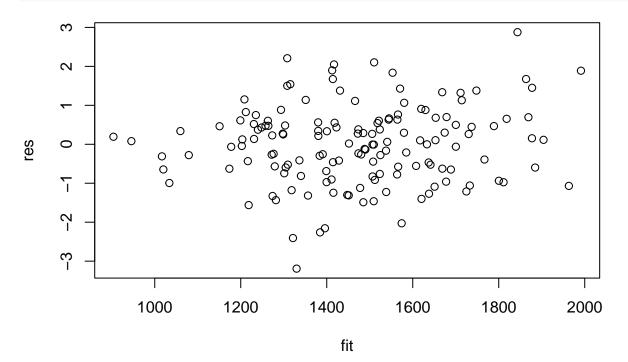
```
current.asr <- spatial.asrts$asrts$TPNCSS$asreml.obj</pre>
current.asr <- update(current.asr, aom=TRUE)</pre>
## ASReml Version 4.2 11/04/2024 09:27:04
##
             LogLik
                            Sigma2
                                        DF
                                                wall
          -662.1988
                          7657.986
                                              09:27:04
##
    1
                                       117
##
    2
          -662.1988
                          7657.984
                                       117
                                              09:27:04
##
    3
          -662.1988
                          7657.977
                                       117
                                              09:27:04
    4
          -662.1988
                          7657.975
##
                                       117
                                              09:27:04
##
    5
          -662.1988
                          7657.975
                                       117
                                              09:27:04
    6
          -662.1988
                          7657.974
                                       117
                                              09:27:04
##
##
   7
          -662.1988
                          7657.974
                                       117
                                              09:27:04
## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged
```

```
Wheat.dat$res <- residuals(current.asr, type = "stdCond")
Wheat.dat$fit <- fitted(current.asr)</pre>
```

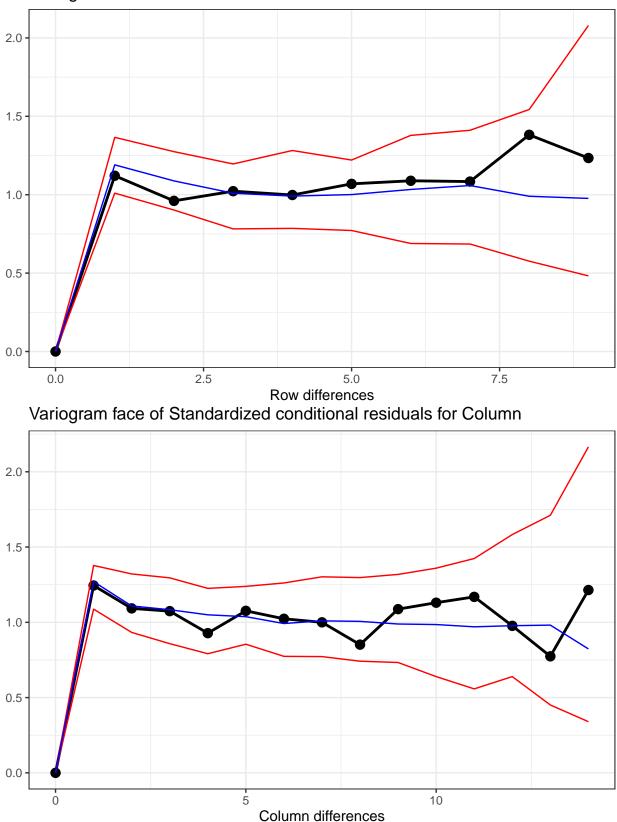
Do diagnostic checking

Do residuals-versus-fitted values plot

```
with(Wheat.dat, plot(fit, res))
```



Plot variofaces



Variogram face of Standardized conditional residuals for Row

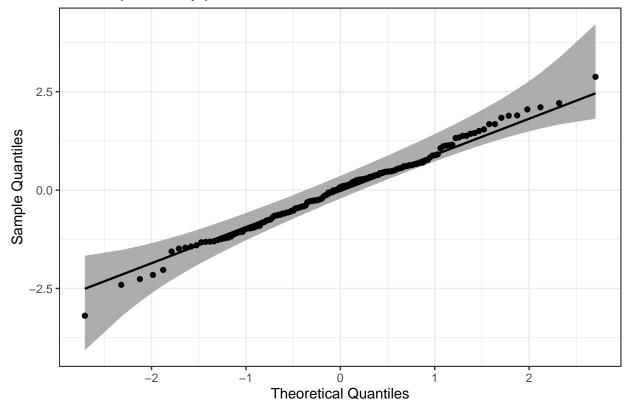
The variofaces are the lag 1 plots of the sample semivariogram with simulated confidence envelopes (Stefanova

et al., 2009).

## Plot normal quantile plot

The plot is obtained using the ggplot function with extensions available from the qqplotr package (Almeida et al., 2023).

```
ggplot(data = Wheat.dat, mapping = aes(sample = res)) +
stat_qq_band(bandType = "ts") + stat_qq_line() + stat_qq_point() +
labs(x = "Theoretical Quantiles", y = "Sample Quantiles",
        title = "Normal probability plot") +
theme(plot.title = element_text(size = 12, face = "bold")) + theme_bw()
```



Normal probability plot

## 4. Prediction production and presentation

Get Variety predictions and all pairwise prediction differences and p-values

## Notice : Spline design points closer than .001400 have been merged ## Notice : Spline design points closer than .000900 have been merged ## ## ## #### Predictions for yield from Variety ## ## ## Notes: ## - The predictions are obtained by averaging across the hypertable ## calculated from model terms constructed solely from factors in ## the averaging and classify sets. ## - Use 'average' to move ignored factors into the averaging set. ## - spl(cRow) evaluated at average value of 0.00000 ## - spl(cColumn) evaluated at average value of 0.00000 ## - The simple averaging set: Rep ## ## Variety predicted.value standard.error upper.halfLeastSignificant.limit ## 1 10 1196.214 64.11316 1255.028 ## 2 9 1266.442 69.62176 1325.255 ## 3 16 1268.206 74.01873 1327.020 ## 4 1 1273.794 69.30592 1332.608 ## 5 14 1310.806 70.75661 1369.620 ## 6 1387.928 23 1329.114 73.70238 ## 7 11 1340.668 75.07426 1399.481 76.83336 ## 8 4 1406.408 1465.222 ## 9 3 1408.543 71.85868 1467.356 ## 10 7 1414.471 72.23082 1473.284 ## 11 12 1423.303 71.18629 1482.117 ## 12 8 75.37805 1445.533 1504.347 ## 13 5 1480.687 70.31499 1539.500 ## 14 15 1485.249 74.28025 1544.063 ## 15 17 1495.212 71.09930 1554.026 ## 16 21 1512.767 72.53109 1571.580 ## 17 6 1520.841 72.50721 1579.654 ## 18 24 1563.649 65.33308 1622.463 ## 19 18 71.06200 1627.700 1568.887 ## 20 25 1579.929 70.52509 1638.743 ## 21 2 74.96623 1644.211 1585.398 ## 22 22 1633.080 71.38265 1691.894 ## 23 13 1637.119 66.24775 1695.932 19 ## 24 1651.533 74.93686 1710.347 ## 25 20 1657.612 1716.426 68.65452 ## lower.halfLeastSignificant.limit est.status ## 1 1137.400 Estimable ## 2 1207.628 Estimable ## 3 1209.393 Estimable ## 4 1214.980 Estimable ## 5 1251.993 Estimable ## 6 1270.300 Estimable ## 7 1281.854 Estimable ## 8 Estimable 1347.594 ## 9 1349.729 Estimable ## 10 1355.657 Estimable ## 11 1364.490 Estimable

##	12	1386.720	Estimable
##	13	1421.873	Estimable
##	14	1426.435	Estimable
##	15	1436.399	Estimable
##	16	1453.953	Estimable
##	17	1462.027	Estimable
##	18	1504.836	Estimable
##	19	1510.073	Estimable
##	20	1521.115	Estimable
##	21	1526.584	Estimable
##	22	1574.266	Estimable
##	23	1578.305	Estimable
##	24	1592.719	Estimable
##	25	1598.798	Estimable
##			
##			
##	LSD values		
##			
##	minimum LSD = 109.6008		
##			
##	mean LSD = 117.6273		
##			
##	maximum LSD = 126.3422		
##			
##	(sed range / mean sed =	0.142 )	

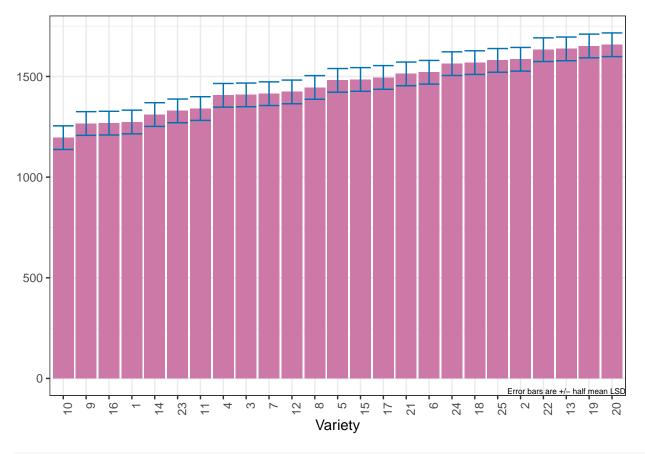
We have set error.intervals to halfLeast so that the limits for each prediction  $\pm (0.5 \text{ LSD})$  are calculated. When these are plotted overlapping error bars indicate predictions that are not significant, while those that do not overlap are significantly different (Snee, 1981).

Also set was sortFactor, so that the results would be ordered for the values of the predictions for Variety. The function **predictPlus** returns an **alldiffs** object, a list consisting of the following components:

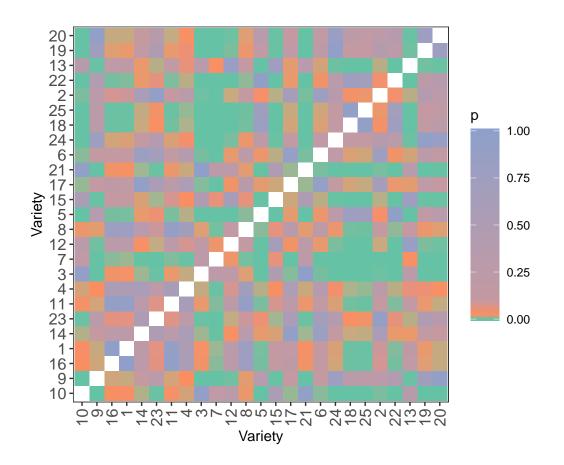
- predictions: the predictions, their standard errors and error intervals;
- vcov: the variance matrix of the predictions;
- differences: all pairwise differences between the predictions,
- p.differences: p-values for all pairwise differences between the predictions;
- sed: the standard errors of all pairwise differences between the predictions;
- LSD: the mean, minimum and maximum of the LSDs.

## Plot the Variety predictions, with halfLSD intervals, and the p-values

```
plotPredictions(Var.diffs$predictions,
                classify = "Variety", y = "predicted.value",
                error.intervals = "half")
```



plotPvalues(Var.diffs)



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