# Package 'XDNUTS'

January 20, 2025

Type Package

Length Version 1.5.5 Date 2024-12-22 **Description** Hamiltonian Monte Carlo for both continuous and discontinuous posterior distributions with customisable trajectory length termination criterion. See Nishimura et al. (2020) <doi:10.1093/biomet/asz083> for the original Discontinuous Hamiltonian Monte Carlo, Hoffman et al. (2014) <doi:10.48550/arXiv.1111.4246> and Betancourt (2016) <doi:10.48550/arXiv.1601.00225> for the definition of possible Hamiltonian Monte Carlo termination criteria. License MIT + file LICENSE Imports base, coda, ggplot2, graphics, grDevices, gridExtra, parallel, purrr, Rcpp (>= 1.0.12), Rdpack, stats **RdMacros** Rdpack LinkingTo Rcpp, RcppArmadillo RoxygenNote 7.3.1 Suggests knitr, rmarkdown, KernSmooth VignetteBuilder knitr **Depends** R (>= 2.10) LazyData true NeedsCompilation yes **Author** Paolo Manildo [aut, cre] (<a href="https://orcid.org/0009-0006-7056-7012">https://orcid.org/0009-0006-7056-7012</a>) Maintainer Paolo Manildo <paolo.manildo@studenti.unipd.it> Repository CRAN **Date/Publication** 2024-12-22 11:40:01 UTC

Title Discontinuous Hamiltonian Monte Carlo with Varying Trajectory

2 XDNUTS-package

# **Contents**

XDNU <sup>*</sup>	TS-package	Disc Leng	tinı	10	us	Н	am	ilt	on	ia	n	M	on	te	C	Car	rlo	ν	vit	h	Va	ar	yin	ıg	Τ	ra	je	ct	or <sub>.</sub>	y
Index																														19
	xdtransform		 										•																•	17
	xdnuts																													
	xdextract																													
	summary.XDNUTS viscosity																													
	set_parameters																													
	print.XDNUTS		 																											9
	print.summary.XDN																													
	plot.XDNUTS																													
	XDNUTS-package main_function																													

# Description

Hamiltonian Monte Carlo for both continuous and discontinuous posterior distributions with customisable trajectory length termination criterion. See Nishimura et al. (2020) <doi:10.1093/biomet/asz083> for the original Discontinuous Hamiltonian Monte Carlo, Hoffman et al. (2014) <doi:10.48550/arXiv.1111.4246> and Betancourt (2016) <doi:10.48550/arXiv.1601.00225> for the definition of possible Hamiltonian Monte Carlo termination criteria.

#### **Details**

#### The DESCRIPTION file:

Package: XDNUTS Type: Package

Title: Discontinuous Hamiltonian Monte Carlo with Varying Trajectory Length

Version: 1.5.5

Date: 2024 12.23

Date: 2024-12-22
Authors@R: person("Paolo", "Manildo", email = "paolo.manildo@studenti.unipd.it", role = c("aut", "cre"), comment =

License: MIT + file LICENSE

Imports: base, coda, ggplot2, graphics, grDevices, gridExtra, parallel, purrr, Rcpp (>= 1.0.12), Rdpack, stats

Hamiltonian Monte Carlo for both continuous and discontinuous posterior distributions with customisable

RdMacros: Rdpack

LinkingTo: Rcpp, RcppArmadillo

RoxygenNote: 7.3.1

Description:

Suggests: knitr, rmarkdown, KernSmooth

VignetteBuilder: knitr
Depends: R (>= 2.10)
LazyData: true

XDNUTS-package 3

Author: Paolo Manildo [aut, cre] (<a href="https://orcid.org/0009-0006-7056-7012">https://orcid.org/0009-0006-7056-7012</a>)

Maintainer: Paolo Manildo <paolo.manildo@studenti.unipd.it>

# Index of help topics:

XDNUTS-package Discontinuous Hamiltonian Monte Carlo with

Varying Trajectory Length

main\_function Function to generate a Markov chain for both

continuous and discontinuous posterior

distributions.

plot.XDNUTS Function to view the draws from the posterior

distribution.

print.XDNUTS Function for printing an object of class XDNUTS

print.summary.XDNUTS Function for printing an object of class

summary.XDNUTS

set\_parameters Function that regulates the specifications of

the xdnuts function.

summary.XDNUTS Function to print the summary of an XDNUTS

model.

viscosity Blood viscosity data

xdextract Function to extract samples from the output of

an XDNUTS model.

xdnuts Discontinuous Hamiltonian Monte Carlo using

both manual and automatic termination criteria.

xdtransform Function to apply a transformation to the

samples from the output of an XDNUTS model.

The package allows to use a more efficient version of the Discontinuous Hamiltonian Monte Carlo proposed in (Nishimura et al. 2020), thanks to the use of recycled samples from each trajectory (Nishimura and Dunson 2020) and a termination criterion for identyfing the optimal discrete integration time of each trajectory (Betancourt 2016). No models are at disposal, so the user must specify one through the definition of the function nlp. This function must evaluate the negative log posterior of the model and its gradient with respect to the first d-k parameters. d is the model dimension, while k is the number of parameters for which the sampling scheme will be based on the method described in (Nishimura et al. 2020). This method was born for treating discontinuous components but it is applicable to continuous one too. nlp must be a function with 3 arguments:

- the vector of parameters, current state of the chain/trajectory, for which the negative log posterior or its gradient must be evaluated.
- a list object that contains the necessary argouments, namely data and hyperparameters.
- a boolean value, TRUE to evaluate only the negative log posterior of the models, FALSE to evaluate its gradient with respect to the continuous components of the posterior.

The available algorithms are the following

**NUTS** No U-Turn Sampler of (Hoffman et al. 2014).

**XHMC** Hamiltonian Monte Carlo with a termination criterion based on the exhustion of the virial (Betancourt 2016) which require the specification of a threshold.

4 main\_function

**HMC** Hamiltonian Monte Carlo with trajectory length varying uniformly inside a user specified interval. Instead of proposing the last value of each trajectories a sample is drawn uniformly from them. Reference can be found in (Betancourt 2017).

All of them are embedded into the framework described in (Nishimura et al. 2020) which allows the use of Hamiltonian Monte Carlo with discontinuous posterior and hence to discrete parameter space by the definition of a step function shape density.

#### Author(s)

Paolo Manildo [aut, cre] (<a href="https://orcid.org/0009-0006-7056-7012">https://orcid.org/0009-0006-7056-7012</a>)

Maintainer: Paolo Manildo <paolo.manildo@studenti.unipd.it>

#### References

Hoffman MD, Gelman A, others (2014). "The No-U-Turn sampler: adaptively setting path lengths in Hamiltonian Monte Carlo." *J. Mach. Learn. Res.*, **15**(1), 1593–1623.

Betancourt M (2016). "Identifying the optimal integration time in Hamiltonian Monte Carlo." *arXiv* preprint arXiv:1601.00225.

Betancourt M (2017). "A conceptual introduction to Hamiltonian Monte Carlo." arXiv preprint arXiv:1701.02434.

Nishimura A, Dunson DB, Lu J (2020). "Discontinuous Hamiltonian Monte Carlo for discrete parameters and discontinuous likelihoods." *Biometrika*, **107**(2), 365–380.

Nishimura A, Dunson D (2020). "Recycling Intermediate Steps to Improve Hamiltonian Monte Carlo." *Bayesian Analysis*, **15**(4). ISSN 1936-0975, doi:10.1214/19ba1171, http://dx.doi.org/10.1214/19-BA1171.

main_function	Function to generate a Markov chain for both continuous and discon-
	tinuous posterior distributions.

#### Description

The function allows to generate a single Markov Chain for sampling from both continuous and discontinuous posterior distributions using a plethora of algorithms. Classic Hamiltonian Monte Carlo (Duane et al. 1987), NUTS (Hoffman et al. 2014) and XHMC (Betancourt 2016) are embedded into the framework described in (Nishimura et al. 2020), which allows to deal with such posteriors. Furthermore, for each method, it is possible to recycle samples from the trajectories using the method proposed by (Nishimura and Dunson 2020). This is used to improve the estimation of the mass matrix during the warm-up phase without requiring significant additional computational costs. This function should not be used directly, but only through the user interface provided by xdnuts.

main\_function 5

#### Usage

```
main_function(
   theta0,
   nlp,
   args,
   k,
   N,
   K,
   tau,
   L,
   thin,
   chain_id,
   verbose,
   control
)
```

#### **Arguments**

theta0 a vector of length-d containing the starting point of the chain.

nlp a function object that takes three arguments:

 $\mathbf{par}$  a vector of length-d containing the value of the parameters.

**args** a list object that contains the necessary arguments, namely data and hyperparameters.

eval\_nlp a boolean value, TRUE for evaluating only the model\'s negative log posterior, FALSE to evaluate the gradient with respect to the continuous components of the posterior.

args the necessary arguments to evaluate the negative log posterior and its gradient.

k the number of parameters that induce a discontinuity in the posterior distribu-

tion.

N integer containing the number of post warm-up samples to evaluate.

K integer containing the number of recycled samples from each trajectory during

the warm-up phase or beyond.

tau the threshold for the exhaustion termination criterion described in (Betancourt

2016).

L the desired length of the trajectory of classic Hamiltonian Monte Carlo algo-

rithm.

thin integer containing the number of samples to discard in order to produce a final

iteration of the chain.

chain\_id the identification number of the chain.

verbose a boolean value that controls whether to print all the information regarding the

sampling process.

control an object of class control\_xdnuts containing the specifications for the algo-

rithm. See the set\_parameters function for detail.

6 main\_function

#### Value

a named list containing:

values a  $N \times d$  matrix containing the sample from the target distribution (if convergence has been reached).

**energy** a vector of length-N containing the Markov Chain of the energy level sets.

**step\_size** a vector of length-N containing the sampled step size used for each iteration.

**step\_length** a vector of length-N containing the length of each trajectory of the chain.

**alpha** a vector of length-k+1 containing the estimate of the Metropolis acceptance probabilities. The first element of the vector is the estimated global acceptance probability. The remaining k elements are the estimate rate of reflection for each parameters which travels coordinate-wise through some discontinuity.

**warm\_up** a  $N_{adapt} \times d$  matrix containing the sample of the chain coming from the warm-up phase. If keep\_warm\_up = FALSE inside the control argument, nothing is returned.

**div\_trans** a  $M \times d$  matrix containing the locations where a divergence has been encountered during the integration of Hamilton equation. Hopefully  $M \ll N$ , and even better if M = 0.

**M\_cont** the Mass Matrix of the continuous components estimated during the warm-up phase. Based on the M\_type value of the control arguments, this could be an empty object, a vector or a matrix.

M\_disc the Mass Matrix of the discontinuous components estimated during the warm-up phase. Based on the M\_type value of the control arguments, this could be an empty object or a vector.

#### References

Betancourt M (2016). "Identifying the optimal integration time in Hamiltonian Monte Carlo." *arXiv* preprint arXiv:1601.00225.

Duane S, Kennedy AD, Pendleton BJ, Roweth D (1987). "Hybrid monte carlo." *Physics letters B*, **195**(2), 216–222.

Hoffman MD, Gelman A, others (2014). "The No-U-Turn sampler: adaptively setting path lengths in Hamiltonian Monte Carlo." *J. Mach. Learn. Res.*, **15**(1), 1593–1623.

Nishimura A, Dunson D (2020). "Recycling Intermediate Steps to Improve Hamiltonian Monte Carlo." *Bayesian Analysis*, **15**(4). ISSN 1936-0975, doi:10.1214/19ba1171, http://dx.doi.org/10.1214/19-BA1171.

Nishimura A, Dunson DB, Lu J (2020). "Discontinuous Hamiltonian Monte Carlo for discrete parameters and discontinuous likelihoods." *Biometrika*, **107**(2), 365–380.

plot.XDNUTS 7

plot.XDNUTS

Function to view the draws from the posterior distribution.

#### **Description**

Function to view the draws from the posterior distribution.

## Usage

```
## S3 method for class 'XDNUTS'
plot(
    x,
    type = 1,
    which = NULL,
    warm_up = FALSE,
    plot.new = FALSE,
    which_chains = NULL,
    colors = NULL,
    gg = TRUE,
    scale = 1,
    ...
)
```

#### **Arguments**

Х an object of class XDNUTS. the type of plot to display. type type = 1 marginal chains, one for each desired dimension. type = 2 bivariate plot. type = 3 time series plot of the energy level sets. Good for a quick diagnostic of big models. type = 4 stickplot of the step-length of each iteration. type = 5 Histograms of the centered marginal energy in gray and of the first differences of energy in red. type = 6 Autoregressive function plot of the parameters. type = 7 Matplot of the empirical acceptance rate and refraction rates. either a numerical vector indicating the index of the parameters of interest or a which string which = 'continuous' for plotting the first d - k parameters. which = 'discontinuous' for plotting the last k parameters. where both d and k are elements contained in the output of the xdnuts function. If type = 7, it refers to the rates index instead. When which = 'continuous', only the global acceptance rate is displayed. In contrast, when which = 'discontinuous', the refraction rates are shown.

warm_up	a boolean value indicating whether the plot should be made using the warm-up samples.
plot.new	a boolean value indicating whether a new graphical window should be opened. This is advised if the parameters space is big.
which_chains	a numerical vector indicating the index of the chains of interest.
colors	a numerical vector containing the colors for each chain specified in which_chains or for each rate specified in which when type = 7.
gg	A boolean value indicating whether the plot should utilize the grammar of graphics features. Default value is set to TRUE.
scale	A numeric value for scaling the appearance of plots.
	additional arguments to customize plots. In reality, these do nothing.

#### Value

A graphical object if gg = TRUE, otherwise nothing is returned.

print.summary.XDNUTS Function for printing an object of class summary.XDNUTS

# Description

Print to console the statistics about the MCMC samples obtained with a call to the function summary.XDNUTS. See that for details.

## Usage

```
## S3 method for class 'summary.XDNUTS'
print(x, ..., digits = 3)
```

## **Arguments**

x an object of class summary.XDNUTS
 ... additional values to pass. These currently do nothing.
 digits number of digits for rounding the output. Default value is 3.

#### Value

No return value.

print.XDNUTS 9

		VDA		
prir	١Ť.	.XI)I	AL J	1.5

Function for printing an object of class XDNUTS

## **Description**

Print to console the specific of the algorithm used to generate an XDNUTS object.

## Usage

```
## S3 method for class 'XDNUTS'
print(x, ..., digits = 3, show_all = FALSE)
```

#### **Arguments**

```
x an object of class XDNUTS.... additional arguments to pass. These currently do nothing.
```

digits a numeric scalar indicating the number of digits to show. Default value is 3.

show\_all logical scalar indicating where to print all the summary statistics even if these

are more than 10.

#### Value

Return a graphical object.

set\_parameters

Function that regulates the specifications of the xdnuts function.

## **Description**

Function that regulates the specifications of the xdnuts function.

# Usage

```
set_parameters(
  N_init1 = 50L,
  N_adapt = 200L,
  N_init2 = 75L,
  burn_adapt_ratio = 0.1,
  keep_warm_up = FALSE,
  recycle_only_init = TRUE,
  max_treedepth = 10L,
  eps_jitter = 0.1,
  L_jitter = 3L,
  gamma = 0.05,
  kappa = 0.75,
```

10 set\_parameters

```
delta = NULL,
t0 = 10L,
M_type = "dense",
refresh = 0.1,
l_eps_init = NA_real_,
different_stepsize = FALSE,
mu = NA_real_,
M_cont = NULL,
M_disc = NULL
```

#### **Arguments**

N\_init1 an integer that regulates the number of samples used to adapt the step size.

N\_adapt an integer that regulates the number of samples used to estimate the Mass Matrix

with fixed step size.

N\_init2 an integer that regulates the number of samples used to adapt the step size after

the estimation of the Mass Matrix.

burn\_adapt\_ratio

a numeric scalar  $\in (0,1]$  indicating the ratio of warm-up samples to discard in

order to estimate the covariance matrix of the parameters.

keep\_warm\_up a logical scalar that determines whether the warm-up samples should be re-

turned.

recycle\_only\_init

a logical value which disables the recycling of the samples from each trajectory

once the warm-up phase has terminated.

max\_treedepth an integer that regulates the maximum depth of the binary tree used to approxi-

mate Hamilton equation for the exploration of each energy level set of the phase

space.

eps\_jitter a numeric scalar which regulates the amount of jittering used to perturb the value

of the step size for each iteration of the chain after the warm-up phase.

L\_jitter an integer scalar that regulates the amount of jittering used to perturb the value

of the trajectory length if this is specified to be constant. This occurs when the classic Hamiltonian Monte Carlo algorithm is used through the method = "HMC" option in the xdnuts function. If L\_jitter  $\geq 1$  each trajectory length is sampled

uniformly inside the interval [L - L\_jitter, L + L\_jitter].

gamma a numeric value that, in the Nesterov Dual Averaging algorithm, regulates the

sensitivity of the step size updating scheme to fluctuations in the estimate of the

mean Metropolis acceptance probability.

kappa a numeric value that regulates the vanishing of Nesterov Dual Averaging algo-

rithm for the estimation of the step size.

delta a vector containing the Metropolis acceptance probabilities, including both the

global and those related to potential differences. Default values are (0.8,0.6). If the second element of the vector is set to NA, then the step size calibration is

conducted solely through the global acceptance probabilities.

summary.XDNUTS 11

an integer value that makes Nesterov Dual Averaging algorithm for the estimation of the step size less sensitive to early iterations.

M\_type a character value specifying the type of Mass Matrix to estimate:

- "identity" no Mass Matrix estimation is done.
- "diagonal" a diagonal Mass Matrix is estimated during the warm-up phase.
- "dense" a full dense Mass Matrix is estimated during the warm-up phase.

refresh a numeric scalar bounded in (0,1) which regulates the update frequency of the

displayed sampling process state. Default values is 0.1, meaning every 10% of

the total samples.

1\_eps\_init a numeric scalar containing the logarithm of the initial value for the step size

used to approximate Hamilton differential equation for phase space exploration.

different\_stepsize

a boolean value indicating where the adaptation scheme should adapt different step size. If TRUE, a global step size is adapted via Nesterov Dual Averaging algorithm. At the same time, for each empirical reflection rate of each component treated as discontinuous the same algorithm is exploited and the difference between these is obtained through the updating of the discontinuous components

Mass Matrix. Default value is FALSE.

mu a numeric scalar containing the value to which the step size is shrunken during

the warm-up phase.

M\_cont a vector of length-d-k if M\_type = "diagonal" or a  $(d-k) \times (d-k)$  ma-

trix if M\_type = "dense" containing an initial estimate for the Mass Matrix (the inverse of the parameters covariance matrix). If you want to keep it fixed, they

should specify  $N_adapt = 0$ .

M\_disc a vector of length-k if M\_type = "diagonal" or M\_type = "dense" containing

an initial estimate for the Mass Matrix (the inverse of the parameters covari-

ances). If one wants to keep it fixed, they should specify N\_adapt = 0.

#### Value

an object of class control\_xdnuts containing a named list with all the above parameters.

summary.XDNUTS

Function to print the summary of an XDNUTS model.

#### **Description**

Function to print the summary of an XDNUTS model.

12 summary.XDNUTS

#### Usage

```
## S3 method for class 'XDNUTS'
summary(
   object,
     ...,
   q.val = c(0.05, 0.25, 0.5, 0.75, 0.95),
   which = NULL,
   which_chains = NULL
)
```

#### **Arguments**

object	an object of class XDNUTS.
	additional arguments to customize the summary.
q.val	desired quantiles of the posterior distribution for each coordinate. Default values are 0.05,0.25,0.5,0.75,0.95.
which	either a numerical vector indicating the index of the parameters of interest or a string
	which = 'continuous' for plotting the first $d-k$ parameters.
	which = 'discontinuous' for plotting the last $\boldsymbol{k}$ parameters.
	where both $d$ and $k$ are elements contained in the output of the function $\operatorname{xdnuts}$ .
which_chains	a numerical vector indicating the index of the chains of interest.

# Value

a list containing a data frame named stats with the following columns:

mean the mean of the posterior distribution.

sd the standard deviation of the posterior distribution.

**q.val** the desired quantiles of the posterior distribution.

**ESS** the Effective Sample Size for each marginal distribution.

**R\_hat** the Potential Scale Reduction Factor of Gelman (Gelman and Rubin 1992), only if multiple chains are available.

**R\_hat\_upper\_CI** the upper confidence interval for the latter, only if multiple chains are available.

Other quantities returned are:

**Gelman.Test** the value of the multivariate Potential Scale Reduction Factor test (Gelman and Rubin 1992).

**BFMI** the value of the empirical Bayesian Fraction of Information Criteria (Betancourt 2016). A value below 0.2 indicates a bad random walk behavior in the energy Markov Chain, mostly due to a suboptimal specification of the momentum parameters probability density.

**n\_div** the total number of trajectory ended with a divergent transition.

**n\_premature** the total number of trajectory with a premature termination.

viscosity 13

#### References

Betancourt M (2016). "Diagnosing suboptimal cotangent disintegrations in Hamiltonian Monte Carlo." *arXiv preprint arXiv:1604.00695*.

Gelman A, Rubin DB (1992). "Inference from iterative simulation using multiple sequences." *Statistical science*, **7**(4), 457–472.

viscosity

Blood viscosity data

## **Description**

Contains blood viscosity measurements of 6 subjects. Each individual was measured 7 times.

## Usage

viscosity

#### **Format**

A data frame with 6 rows and 8 variables:

id subject identifier.

Time.1 viscosity measurements for the first time.,

Time.2 viscosity measurements for the second time.,

**Time.3** viscosity measurements for the third time.,

**Time.4** viscosity measurements for the fourth time.,

Time.5 viscosity measurements for the fifth time.,

**Time.6** viscosity measurements for the sixth time.,

**Time.7** viscosity measurements for the seventh time.

#### Source

Master\'s Degree course at the University of Padua

## **Examples**

data(viscosity)

14 xdextract

xdextract

Function to extract samples from the output of an XDNUTS model.

# Description

Function to extract samples from the output of an XDNUTS model.

# Usage

```
xdextract(
   X,
   which = NULL,
   which_chains = NULL,
   collapse = FALSE,
   thin = NULL,
   burn = NULL
)
```

# Arguments

Χ	an object of class XDNUTS.
which	either a numerical vector indicating the index of the parameters of interest or a string
	which = 'continuous' for plotting the first $d-k$ parameters.
	which = 'discontinuous' for plotting the last $\boldsymbol{k}$ parameters.
	where both $\boldsymbol{d}$ and $\boldsymbol{k}$ are elements contained in the output of the function xdnuts.
which_chains	a vector of indices containing the chains to extract. By default, all chains are considered.
collapse	a boolean value. If TRUE, all samples from every chain are collapsed into one. The default value is FALSE.
thin	an integer value indicating how many samples should be discarded before returning an iteration of the chain.
burn	an integer value indicating how many initial samples for each chain to burn.

# Value

an  $N \times d$  matrix or an  $N \times d \times C$  array, where C is the number of chains, containing the MCMC samples.

xdnuts 15

xdnuts

Discontinuous Hamiltonian Monte Carlo using both manual and automatic termination criteria.

#### **Description**

The function allows generating multiple Markov Chains for sampling from both continuous and discontinuous posterior distributions using a variety of algorithms. Classic Hamiltonian Monte Carlo (Duane et al. 1987), NUTS (Hoffman et al. 2014), and XHMC (Betancourt 2016) are embedded into the framework described in (Nishimura et al. 2020), which allows dealing with such posteriors. Furthermore, for each method, it is possible to recycle samples from the trajectories using the method proposed by (Nishimura and Dunson 2020). This is used to improve the estimate of the Mass Matrix during the warm-up phase without requiring a relevant additional computational cost.

#### Usage

```
xdnuts(
  theta0,
  nlp,
  args,
  k,
 N = 1000,
 K = 3,
 method = "NUTS",
  tau = NULL,
  L = NULL
  thin = 1,
  control = set_parameters(),
  parallel = FALSE,
  loadLibraries = NULL,
  loadRObject = NULL,
  verbose = FALSE,
  hide = FALSE
)
```

#### **Arguments**

theta0

a list containing the starting values for each chain. These starting values are vectors of length-d. The last  $k \in [0,d]$  elements refer to parameters which determine a discontinuity in the posterior distribution.

nlp

a function which evaluates the negative log posterior and its gradient with respect to parameters that do not induce any discontinuity in the posterior distribution (more generally, the first d-k parameters). This function must take 3 arguments:

par a vector of length-d containing the parameter values.

**args** a list object that contains the necessary arguments, namely data and hyperparameters.

16 xdnuts

	eval_nlp a boolean value, TRUE to evaluate only the negative log posterior of the models, FALSE to evaluate its gradient with respect to the continuous components of the posterior.
args	a list containing the inputs for the negative posterior function.
k	an integer value that states the number of parameters that determines a discontinuity in the posterior distribution. Actually, since the algorithm proposed in (Nishimura et al. 2020) also works for the full continuous case, k is the number of parameters specified by the user for which this algorithm is used.
N	the number of draws from the posterior distribution, after warm-up, for each chain. Default value is $1000$ .
K	the number of recycled samples per iteration used by default during the warm-up phase. Default value is 3. To recycle in the sampling phase too, specify recycle_only_init = FALSE in the control argument above.
method	a character value which defines the type of algorithm to exploit:
	"NUTS" applies the No U-Turn Sampler of (Hoffman et al. 2014).
	"XHMC" applies the Exhaustion Hamiltonian Monte Carlo of (Betancourt 2016).  "HMC" applies one of the classic version of Hamiltonian Monte Carlo algorithm, in particular the one described in (Betancourt 2017), which samples from the trajectory instead of always returning the last value.
tau	the threshold for the virial termination criterion (Betancourt 2016).
L	the desired length of the trajectory of classic Hamiltonian Monte Carlo algorithm.
thin	the number of necessary and discarded samples to obtain a final iteration of one chain.
control	an object of class control_xdnuts, output of the function set_parameters.
parallel	a boolean value specifying whether the chains must be run in parallel. Default value is $\ensuremath{FALSE}.$
loadLibraries	A character vector indicating the names of the packages to load on each cluster if parallel is set to TRUE.
loadRObject	A character vector indicating the names of the R objects to load on each cluster if parallel is set to TRUE.
verbose	a boolean value for printing all the information regarding the sampling process.
hide	a boolean value that omits the printing to the console if set to TRUE.

## Value

a list of class XDNUTS containing

chains a list of the same length of theta0, each element containing the output from the function main\_function.

 ${\bf d}$  the dimension of the parameter space.

**k** the number of parameters that lead to a discontinuous posterior distribution. Or, more generally, for which the algorithm of (Nishimura et al. 2020) is exploited.

xdtransform 17

**K** the number of recycled samples for each iteration during the sampling phase.

N the number of posterior draws for each chain.

method the MCMC method used. This could be either "NUTS", "XHMC", or "HMC".

**tau** the threshold for the virial termination criterion (Betancourt 2016). Only if method = "XHMC" this value is different from zero.

L the desired length of the trajectory of classic Hamiltonian Monte Carlo algorithm specified by the user. This argument is necessary if method = "HMC".

thin the number of discarded samples for every final iteration, specified by the user.

**control** an object of class control\_xdnuts, output of the function set\_parameters with arguments specified by the user.

**verbose** the boolean value specified by the user regarding the printing of the sampling process information.

parallel the boolean value specified by the user regarding parallel processing.

#### References

Betancourt M (2016). "Identifying the optimal integration time in Hamiltonian Monte Carlo." *arXiv* preprint arXiv:1601.00225.

Betancourt M (2017). "A conceptual introduction to Hamiltonian Monte Carlo." arXiv preprint arXiv:1701.02434.

Duane S, Kennedy AD, Pendleton BJ, Roweth D (1987). "Hybrid monte carlo." *Physics letters B*, **195**(2), 216–222.

Hoffman MD, Gelman A, others (2014). "The No-U-Turn sampler: adaptively setting path lengths in Hamiltonian Monte Carlo." *J. Mach. Learn. Res.*, **15**(1), 1593–1623.

Nishimura A, Dunson D (2020). "Recycling Intermediate Steps to Improve Hamiltonian Monte Carlo." *Bayesian Analysis*, **15**(4). ISSN 1936-0975, doi:10.1214/19ba1171, http://dx.doi.org/10.1214/19-BA1171.

Nishimura A, Dunson DB, Lu J (2020). "Discontinuous Hamiltonian Monte Carlo for discrete parameters and discontinuous likelihoods." *Biometrika*, **107**(2), 365–380.

xdtransform Function to apply a transformation to the samples from the output of an XDNUTS model.	xdtransform	Function to apply a transformation to the samples from the output of an XDNUTS model.
---	-------------	---

#### Description

Function to apply a transformation to the samples from the output of an XDNUTS model.

18 xdtransform

# Usage

```
xdtransform(
   X,
   which = NULL,
   FUN = NULL,
   ...,
   new.names = NULL,
   thin = NULL,
   burn = NULL
)
```

#### **Arguments**

X an object of class XDNUTS.

which a vector of indices indicating which parameter the transformation should be ap-

plied to. If NULL, the function is applied to all of them.

FUN a function object which takes one or more components of an MCMC iteration

and any other possible arguments.

... optional arguments for FUN.

new.names a character vector containing the parameter names in the new parameterization.

If only one value is provided, but the transformation involves more, the name is

iterated with an increasing index.

thin an integer value indicating how many samples should be discarded before re-

turning an iteration of the chain.

burn an integer value indicating how many initial samples for each chain to discard.

#### Value

an object of class XDNUTS with the specified transformation applied to each chain.

# **Index**

```
* datasets
viscosity, 13

main_function, 4, 16

plot.XDNUTS, 7
print.summary.XDNUTS, 8
print.XDNUTS, 9

set_parameters, 5, 9, 16, 17
summary.XDNUTS, 8, 11

viscosity, 13

xdextract, 14
XDNUTS (XDNUTS-package), 2
xdnuts, 4, 7, 9, 10, 12, 14, 15
XDNUTS-package, 2
xdtransform, 17
```