

Package ‘MVar’

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Title Multivariate Analysis

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MVar-package

Multivariate Analysis.

Description

Multivariate analysis, having functions that perform simple correspondence analysis (CA) and multiple correspondence analysis (MCA), principal components analysis (PCA), canonical correlation analysis (CCA), factorial analysis (FA), multidimensional scaling (MDS), linear (LDA) and quadratic discriminant analysis (QDA), hierarchical and non-hierarchical cluster analysis, simple and multiple linear regression, multiple factor analysis (MFA) for quantitative, qualitative, frequency (MFACT) and mixed data, biplot, scatter plot, projection pursuit (PP), grant tour method and other useful functions for the multivariate analysis.

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Author(s)

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 Biplot

Biplot graph.

Description

Plots the Biplot graph.

Usage

```
Biplot(data, alpha = 0.5, title = NA, xlabel = NA, ylabel = NA,
       size = 1.1, grid = TRUE, color = TRUE, var = TRUE,
       obs = TRUE, linlab = NA, class = NA, classcolor = NA,
       posleg = 2, boxleg = TRUE, axes = TRUE, savptc = FALSE,
       width = 3236, height = 2000, res = 300)
```

Arguments

data	Data for plotting.
alpha	Representativeness of the individuals (alpha), representativeness of the variables (1 - alpha), being 0.5 the default.
title	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
var	Adds the variable projections to graph (default = TRUE).
obs	Adds the observations to graph (default = TRUE).
linlab	Vector with the labels for the observations.
class	Vector with names of data classes.
classcolor	Vector with the colors of the classes.
posleg	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
boxleg	Puts the frame in the caption (default = TRUE).
axes	Plots the X and Y axes (default = TRUE).
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (default = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).

Value

Biplot	Biplot graph.
Md	Matrix eigenvalues.
Mu	Matrix U (eigenvectors).
Mv	Matrix V (eigenvectors).
coorI	Coordinates of the individuals.
coorV	Coordinates of the variables.
pvar	Proportion of the principal components.

Author(s)

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References

Rencher, A. C. *Methods of multivariate analysis*. 2th. ed. New York: J.Wiley, 2002. 708 p.

Examples

```
data(iris) # dataset

data <- iris[,1:4]

Biplot(data)

cls <- iris[,5]
res <- Biplot(data, alpha = 0.6, title = "Biplot of data valuing individuals",
              class = cls, classcolor = c("goldenrod3", "gray56", "red"),
              posleg = 2, boxleg = FALSE, axes = TRUE, savptc = FALSE,
              width = 3236, height = 2000, res = 300)
print(res$pvar)

res <- Biplot(data, alpha = 0.4, title = "Graph valuing the variables",
              xlabel = "", ylabel = "", color = FALSE, obs = FALSE,
              savptc = FALSE, width = 3236, height = 2000, res = 300)
print(res$pvar)
```

CA

*Correspondence Analysis (CA).***Description**

Performs simple correspondence analysis (CA) and multiple (MCA) in a data set.

Usage

```
CA(data, typdata = "f", typmatrix = "I")
```

Arguments

<code>data</code>	Data to be analyzed (contingency table).
<code>typdata</code>	"f" for frequency data (default), "c" for qualitative data.
<code>typmatrix</code>	Matrix used for calculations when <code>typdata = "c"</code> . "I" for indicator matrix (default), "B" for Burt's matrix.

Value

<code>depdata</code>	Verify if the rows and columns are dependent, or independent by the chi-square test, at the 5% significance level.
<code>typdata</code>	Data type: "F" frequency or "C" qualitative.
<code>numcod</code>	Number of principal components.
<code>mtxP</code>	Matrix of the relative frequency.
<code>vtrR</code>	Vector with sums of the rows.
<code>vtrC</code>	Vector with sums of the columns.
<code>mtxPR</code>	Matrix with profile of the rows.
<code>mtxPC</code>	Matrix with profile of the columns.
<code>mtxZ</code>	Matrix Z.
<code>mtxU</code>	Matrix with the eigenvectors U.
<code>mtxV</code>	Matrix with the eigenvectors V.
<code>mtxL</code>	Matrix with eigenvalues.
<code>mtxX</code>	Matrix with the principal coordinates of the rows.
<code>mtxY</code>	Matrix with the principal coordinates of the columns.
<code>mtxAutv1r</code>	Matrix of the inertias (variances), with the proportions and proportions accumulated.

Author(s)

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References

Mingoti, S. A. *Analise de dados atraves de metodos de estatistica multivariada: uma abordagem aplicada*. Belo Horizonte: UFMG, 2005. 297 p.

Rencher, A. C. *Methods of multivariate analysis*. 2th. ed. New York: J.Wiley, 2002. 708 p.

See Also

[Plot.CA](#)

Examples

```
data(DataFreq) # frequency data set

data <- DataFreq[,2:ncol(DataFreq)]

rownames(data) <- as.character(t(DataFreq[1:nrow(DataFreq),1]))

res <- CA(data = data, "f") # performs CA

print("Is there dependency between rows and columns?"); res$depdata

print("Number of principal coordinates:"); res$numcoord

print("Principal coordinates of the rows:"); round(res$mtxX,2)

print("Principal coordinates of the columns:"); round(res$mtxY,2)

print("Inertia of the principal components:"); round(res$mtxAutvlr,2)
```

CCA

Canonical Correlation Analysis(CCA).

Description

Perform Canonical Correlation Analysis (CCA) on a data set.

Usage

```
CCA(X = NULL, Y = NULL, type = 1, test = "Bartlett", sign = 0.05)
```

Arguments

X	First group of variables of a data set.
Y	Second group of variables of a data set.
type	1 for analysis using the covariance matrix (default), 2 for analysis using the correlation matrix.
test	Test of significance of the relationship between the group X and Y: "Bartlett" (default) or "Rao".
sign	Test significance level (default 5%).

Value

Cxx	Covariance matrix or correlation Cxx.
Cyy	Covariance matrix or correlation Cyy.
Cxy	Covariance matrix or correlation Cxy.
Cyx	Covariance matrix or correlation Cyx.
var.UV	Matrix with eigenvalues (variances) of the canonical pairs U and V.
corr.UV	Matrix of the correlation of the canonical pairs U and V.
coef.X	Matrix of the canonical coefficients of the group X.
coef.Y	Matrix of the canonical coefficients of the group Y.
corr.X	Matrix of the correlations between canonical variables and the original variables of the group X.
corr.Y	Matrix of the correlations between the canonical variables and the original variables of the group Y.
score.X	Matrix with the scores of the group X.
score.Y	Matrix with the scores of the group Y.
sigtest	Returns the significance test of the relationship between group X and Y: "Bartlett" (default) or "Rao".

Author(s)

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References

- Mingoti, S. A. *Análise de dados através de métodos de estatística multivariada: uma abordagem aplicada*. Belo Horizonte: UFMG, 2005. 297 p.
- Ferreira, D. F. *Estatística Multivariada*. 2a ed. revisada e ampliada. Lavras: Editora UFLA, 2011. 676 p.
- Rencher, A. C. *Methods of multivariate analysis*. 2th. ed. New York: J.Wiley, 2002. 708 p.
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See Also[Plot.CCA](#)**Examples**

```
data(DataMix) # data set

data <- DataMix[,2:ncol(DataMix)]

rownames(data) <- DataMix[,1]

X <- data[,1:2]

Y <- data[,5:6]

res <- CCA(X, Y, type = 2, test = "Bartlett", sign = 0.05)

print("Matrix with eigenvalues (variances) of the canonical pairs U and V:"); round(res$var.UV,3)

print("Matrix of the correlation of the canonical pairs U and V:"); round(res$corr.UV,3)

print("Matrix of the canonical coefficients of the group X:"); round(res$coef.X,3)

print("Matrix of the canonical coefficients of the group Y:"); round(res$coef.Y,3)

print("Matrix of the correlations between the canonical
      variables and the original variables of the group X:"); round(res$corr.X,3)

print("Matrix of the correlations between the canonical
      variables and the original variables of the group Y:"); round(res$corr.Y,3)

print("Matrix with the scores of the group X:"); round(res$score.X,3)

print("Matrix with the scores of the group Y:"); round(res$score.Y,3)

print("test of significance of the canonical pairs:"); res$sigtest
```

Cluster

Cluster Analysis.

Description

Performs hierarchical and non-hierarchical cluster analysis in a data set.

Usage

```
Cluster(data, titles = NA, hierarquic = TRUE, analysis = "Obs",
        cor.abs = FALSE, normalize = FALSE, distance = "euclidean",
        method = "complete", horizontal = FALSE, num.groups = 0,
```

```
lambda = 2, savptc = FALSE, width = 3236, height = 2000,
res = 300, casc = TRUE)
```

Arguments

<code>data</code>	Data to be analyzed.
<code>titles</code>	Titles of the graphics, if not set, assumes the default text.
<code>hierarquic</code>	Hierarchical groupings (default = TRUE), for non-hierarchical groupings (method K-Means), only for case 'analysis' = "Obs".
<code>analysis</code>	"Obs" for analysis on observations (default), "Var" for analysis on variables.
<code>cor.abs</code>	Matrix of absolute correlation case 'analysis' = "Var" (default = FALSE).
<code>normalize</code>	Normalize the data only for case 'analysis' = "Obs" (default = FALSE).
<code>distance</code>	Metric of the distances in case of hierarchical groupings: "euclidean" (default), "maximum", "manhattan", "canberra", "binary" or "minkowski". Case Analysis = "Var" the metric will be the correlation matrix, according to cor.abs.
<code>method</code>	Method for analyzing hierarchical groupings: "complete" (default), "ward.D", "ward.D2", "single", "average", "mcquitty", "median" or "centroid".
<code>horizontal</code>	Horizontal dendrogram (default = FALSE).
<code>num.groups</code>	Number of groups to be formed.
<code>lambda</code>	Value used in the minkowski distance.
<code>savptc</code>	Saves graphics images to files (default = FALSE).
<code>width</code>	Graphics images width when savptc = TRUE (default = 3236).
<code>height</code>	Graphics images height when savptc = TRUE (default = 2000).
<code>res</code>	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
<code>casc</code>	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Several graphics.

<code>tab.res</code>	Table with similarities and distances of the groups formed.
<code>groups</code>	Original data with groups formed.
<code>res.groups</code>	Results of the groups formed.
<code>R.sqt</code>	Result of the R squared.
<code>sum.sqt</code>	Total sum of squares.
<code>mtx.dist</code>	Matrix of the distances.

Author(s)

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References

- Rencher, A. C. *Methods of multivariate analysis*. 2th. ed. New York: J.Wiley, 2002. 708 p.
- Mingoti, S. A. *analysis de dados atraves de metodos de estatistica multivariada: uma abordagem aplicada*. Belo Horizonte: UFMG, 2005. 297 p.
- Ferreira, D. F. *Estatistica Multivariada*. 2a ed. revisada e ampliada. Lavras: Editora UFPA, 2011. 676 p.

Examples

```
data(DataQuan) # set of quantitative data

data <- DataQuan[,2:8]

rownames(data) <- DataQuan[1:nrow(DataQuan),1]

res <- Cluster(data, titles = NA, hierarquic = TRUE, analysis = "Obs",
              cor.abs = FALSE, normalize = FALSE, distance = "euclidean",
              method = "ward.D", horizontal = FALSE, num.groups = 2,
              savptc = FALSE, width = 3236, height = 2000, res = 300,
              casc = FALSE)

print("R squared:"); res$R.sqt
# print("Total sum of squares:"); res$sum.sqt
print("Groups formed:"); res$groups
# print("Table with similarities and distances:"); res$tab.res
# print("Table with the results of the groups:"); res$res.groups
# print("Distance Matrix:"); res$mtx.dist

write.table(file=file.path(tempdir(),"SimilarityTable.csv"), res$tab.res, sep=";",
            dec=".",row.names = FALSE)
write.table(file=file.path(tempdir(),"GroupData.csv"), res$groups, sep=";",
            dec=".",row.names = TRUE)
write.table(file=file.path(tempdir(),"GroupResults.csv"), res$res.groups, sep=";",
            dec=".",row.names = TRUE)
```

CoefVar

Coefficient of variation of the data.

Description

Find the coefficient of variation of the data, either overall or per column.

Usage

```
CoefVar(data, type = 1)
```

Arguments

data	Data to be analyzed.
type	1 Coefficient of overall variation (default), 2 Coefficient of variation per column.

Value

Coefficient of variation, either overall or per column.

Author(s)

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References

Ferreira, D. F.; *Estatística Basica*. 2 ed. rev. Lavras: UFLA, 2009. 664 p.

Examples

```
data(DataQuan) # data set  
  
data <- DataQuan[,2:8]  
  
res <- CoefVar(data, type = 1) # Coefficient of overall variation  
round(res,2)  
  
res <- CoefVar(data, type = 2) # Coefficient of variation per column  
round(res,2)
```

DA

Linear (LDA) and quadratic discriminant analysis (QDA).

Description

Perform linear and quadratic discriminant analysis.

Usage

```
DA(data, class = NA, type = "lda", validation = "learning",  
method = "moment", prior = NA, testing = NA)
```

Arguments

data	Data to be classified.
class	Vector with data classes names.
type	"lda": linear discriminant analysis (default), or "qda": quadratic discriminant analysis.
validation	Type of validation: "learning" - data training (default), or "testing" - classifies the data of the vector "testing".
method	Classification method: "mle" to MLEs, "mve" to use cov.mv, "moment" (default) for standard mean and variance estimators, or "t" for robust estimates based on the t distribution.
prior	Probabilities of occurrence of classes. If not specified, it will take the proportions of the classes. If specified, probabilities must follow the order of factor levels.
testing	Vector with indices that will be used in data as test. For validation = "learning", one has testing = NA.

Value

confusion	Confusion table.
error.rate	Overall error ratio.
prior	Probability of classes.
type	Type of discriminant analysis.
validation	Type of validation.
num.class	Number of classes.
class.names	Class names.
method	Classification method.
num.correct	Number of correct observations.
results	Matrix with comparative classification results.

Author(s)

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References

- Ferreira, D. F. *Estatística Multivariada*. 2a ed. revisada e ampliada. Lavras: Editora UFLA, 2011. 676 p.
- Mingoti, S. A. *Análise de dados através de métodos de estatística multivariada: uma abordagem aplicada*. Belo Horizonte: UFMG, 2005. 297 p.

Rencher, A. C. *Methods of multivariate analysis*. 2th. ed. New York: J.Wiley, 2002. 708 p.
 Ripley, B. D. *Pattern Recognition and Neural Networks*. Cambridge University Press, 1996.
 Venables, W. N.; Ripley, B. D. *Modern Applied Statistics with S*. Fourth edition. Springer, 2002.

Examples

```

data(iris) # data set

data = iris[,1:4] # data to be classified
class = iris[,5] # data class
prior = c(1,1,1)/3 # a priori probability of the classes

res <- DA(data, class, type = "lda", validation = "learning",
          method = "mle", prior = prior, testing = NA)

print("confusion table:"); res$confusion
print("Overall hit ratio:"); 1 - res$error.rate
print("Probability of classes:"); res$prior
print("classification method:"); res$method
print("type of discriminant analysis:"); res$type
print("class names:"); res$class.names
print("Number of classes:"); res$num.class
print("type of validation:"); res$validation
print("Number of correct observations:"); res$num.correct
print("Matrix with comparative classification results:"); res$results

### cross-validation ###
amostra = sample(2, nrow(data), replace = TRUE, prob = c(0.7,0.3))
datatrain = data[amostra == 1,] # training data
datatest = data[amostra == 2,] # test data

dim(datatrain) # training data dimension
dim(datatest) # test data dimension

testing = as.integer(rownames(datatest)) # test data index

res <- DA(data, class, type = "qda", validation = "testing",
          method = "moment", prior = NA, testing = testing)

print("confusion table:"); res$confusion
print("Overall hit ratio:"); 1 - res$error.rate
print("Number of correct observations:"); res$num.correct
print("Matrix with comparative classification results:"); res$results

```


Description

Set of data categorized by coffees, on sensorial abilities in the consumption of special coffees.

Usage

```
data(DataCoffee)
```

Format

Data set of a research done with the purpose of evaluating the concordance between the responses of different groups of consumers with different sensorial abilities. The experiment relates the sensorial analysis of special coffees defined by (A) Yellow Bourbon, cultivated at altitudes greater than 1200 m; (D) idem to (A) differing only in the preparation of the samples; (B) Acaia cultivated at an altitude of less than 1,100 m; (C) identical to (B) but differentiating the sample preparation. Here the data are categorized by coffees. The example given demonstrates the results found in OSSANI et al. (2017).

References

Ossani, P. C.; Cirillo, M. A.; Borem, F. M.; Ribeiro, D. E.; Cortez, R. M.. Quality of specialty coffees: a sensory evaluation by consumers using the MFACT technique. *Revista Ciencia Agronomica (UFC. Online)*, v. 48, p. 92-100, 2017.

Ossani, P. C. *Qualidade de cafes especiais e nao especiais por meio da analise de multiplos fatores para tabelas de contingencias*. 2015. 107 p. Dissertacao (Mestrado em Estatistica e Experimentacao Agropecuaria) - Universidade Federal de Lavras, Lavras, 2015.

Examples

```
data(DataCoffee) # categorized data set

data <- DataCoffee[,2:ncol(DataCoffee)]

rownames(data) <- as.character(t(DataCoffee[1:nrow(DataCoffee),1]))

group.names = c("Coffee A", "Coffee B", "Coffee C", "Coffee D")

mf <- MFA(data, c(16,16,16,16), c(rep("f",4)), group.names)

print("Principal components variances:"); round(mf$mtxA,2)

print("Matrix of the Partial Inertia / Score of the Variables:"); round(mf$mtxEV,2)

tit <- c("Scree-plot", "Individuals", "Individuals / Types coffees", "Inercias Groups")

Plot.MFA(mf, titles = tit, xlabel = NA, ylabel = NA,
         posleg = 2, boxleg = FALSE, color = TRUE,
         namarr = FALSE, linlab = NA, casc = FALSE) # plotting several graphs on the screen
```

DataFreq *Frequency data set.*

Description

Simulated data set with the weekly frequency of the number of coffee cups consumed weekly in some world capitals.

Usage

```
data(DataFreq)
```

Format

Set of data with 6 rows and 9 columns. There are 6 observations described by 9 variables: Group by sex and age, Sao Paulo - Cafe Bourbon, London - Cafe Bourbon, Athens - Cafe Bourbon, London - Cafe Acaia, Athens - Cafe Catuai, Sao Paulo - Cafe Catuai, Athens - Cafe Catuai.

Author(s)

Paulo Cesar Ossani
Marcelo Angelo Cirillo

Examples

```
data(DataFreq)  
DataFreq
```

DataInd *Frequency data set.*

Description

Set of data categorized by coffees, on sensorial abilities in the consumption of special coffees.

Usage

```
data(DataInd)
```

Format

Data set of a research done with the purpose of evaluating the concordance between the responses of different groups of consumers with different sensorial abilities. The experiment relates the sensorial analysis of special coffees defined by (A) Yellow Bourbon, cultivated at altitudes greater than 1200 m; (D) idem to (A) differing only in the preparation of the samples; (B) Acaia cultivated at an altitude of less than 1,100 m; (C) identical to (B) but differentiating the sample preparation. Here the data are categorized by coffees. The example given demonstrates the results found in OSSANI et al. (2017).

References

Ossani, P. C.; Cirillo, M. A.; Borem, F. M.; Ribeiro, D. E.; Cortez, R. M.. Quality of specialty coffees: a sensory evaluation by consumers using the MFACT technique. *Revista Ciencia Agronomica (UFC. Online)*, v. 48, p. 92-100, 2017.

Ossani, P. C. *Qualidade de cafes especiais e nao especiais por meio da analise de multiplos fatores para tabelas de contingencias*. 2015. 107 p. Dissertacao (Mestrado em Estatistica e Experimentacao Agropecuaria) - Universidade Federal de Lavras, Lavras, 2015.

Examples

```
data(DataInd) # categorized data set

data <- DataInd[,2:ncol(DataInd)]

rownames(data) <- as.character(t(DataInd[1:nrow(DataInd),1]))

group.names = c("Group 1", "Group 2", "Group 3", "Group 4")

mf <- MFA(data, c(16,16,16,16), c(rep("f",4)), group.names)

print("Principal components variances:"); round(mf$mtxA,2)

print("Matrix of the Partial Inertia / Score of the Variables:"); round(mf$mtxEV,2)

tit <- c("Scree-plot", "Individuals", "Individuals / Types coffees", "Inercias Groups")

Plot.MFA(mf, titles = tit, xlabel = NA, ylabel = NA,
         posleg = 2, boxleg = FALSE, color = TRUE,
         namarr = FALSE, linlab = NA, casc = FALSE) # plotting several graphs on the screen
```

DataMix

Mixed data set.

Description

Simulated set of mixed data on consumption of coffee.

Usage

```
data(DataMix)
```

Format

Data set with 10 rows and 7 columns. Being 10 observations described by 7 variables: Cooperatives/Tasters, Average grades given to analyzed coffees, Years of work as a taster, Taster with technical training, Taster exclusively dedicated, Average frequency of the coffees Classified as special, Average frequency of the coffees as commercial.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

Examples

```
data(DataMix)  
DataMix
```

DataQuali

Qualitative data set

Description

Set simulated of qualitative data on consumption of coffee.

Usage

```
data(DataQuali)
```

Format

Data set simulated with 12 rows and 6 columns. Being 12 observations described by 6 variables: Sex, Age, Smoker, Marital status, Sportsman, Study.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

Examples

```
data(DataQuali)  
DataQuali
```

DataQuan	<i>Quantitative data set</i>
----------	------------------------------

Description

Set simulated of quantitative data on grades given to some sensory characteristics of coffees.

Usage

```
data(DataQuan)
```

Format

Data set with 6 rows and 11 columns. Being 6 observations described by 11 variables: Coffee, Chocolate, Caramelised, Ripe, Sweet, Delicate, Nutty, Caramelised, Chocolate, Spicy, Caramelised.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

Examples

```
data(DataQuan)  
DataQuan
```

FA	<i>Factor Analysis (FA).</i>
----	------------------------------

Description

Performs factorial analysis (FA) in a data set.

Usage

```
FA(data, method = "PC", type = 2, nfactor = 1, rotation = "None",  
  scoresobs = "Bartlett", converg = 1e-5, iteracao = 1000,  
  testfit = TRUE)
```

Arguments

data	Data to be analyzed.
method	Method of analysis: "PC" - Principal Components (default), "PF" - Principal Factor, "ML" - Maximum Likelihood.
type	1 for analysis using the covariance matrix, 2 for analysis using the correlation matrix (default).
rotation	Type of rotation: "None" (default), "Varimax" and "Promax".
nfactor	Number of factors (default = 1).
scoresobs	Type of scores for the observations: "Bartlett" (default) or "Regression".
converg	Limit value for convergence to sum of the squares of the residuals for Maximum likelihood method (default = 1e-5).
iteracao	Maximum number of iterations for Maximum Likelihood method (default = 1000).
testfit	Tests the model fit to the method of Maximum Likelihood (default = TRUE).

Value

mtxMC	Matrix of correlation / covariance.
mtxAutv1r	Matrix of eigenvalues.
mtxAutvec	Matrix of eigenvectors.
mtxvar	Matrix of variances and proportions.
mtxcarga	Matrix of factor loadings.
mtxvaresp	Matrix of specific variances.
mtxcomuna	Matrix of commonalities.
mtxresidue	Matrix of residues.
v1rsqrs	Upper limit value for sum of squares of the residues.
v1rsqr	Sum of squares of the residues.
mtxresult	Matrix with all associated results.
mtxscores	Matrix with scores of the observations.
coefscores	Matrix with the scores of the coefficients of the factors.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

Mingot, S. A. *Análise de dados através de métodos de estatística multivariada: uma abordagem aplicada*. Belo Horizonte: UFMG, 2005. 297 p.

Kaiser, H. F. *The varimax criterion for analytic rotation in factor analysis*. Psychometrika 23, 187-200, 1958.

Rencher, A. C. *Methods of multivariate analysis*. 2th. ed. New York: J.Wiley, 2002. 708 p.

Ferreira, D. F. *Estatística Multivariada*. 2a ed. revisada e ampliada. Lavras: Editora UFLA, 2011. 676 p.

See Also

[Plot.FA](#)

Examples

```
data(DataQuan) # data set

data <- DataQuan[,2:ncol(DataQuan)]

rownames(data) <- DataQuan[,1]

res <- FA(data, method = "PC", type = 2, nfactor = 3, rotation = "None",
          scoresobs = "Bartlett", converg = 1e-5, iteracao = 1000,
          testfit = TRUE)

print("Matrix with all associated results:"); round(res$mtxresult,3)

print("Sum of squares of the residues:"); round(res$vlrsqr,3)

print("Matrix of the factor loadings.:"); round(res$mtxcarga,3)

print("Matrix with scores of the observations:"); round(res$mtxscores,3)

print("Matrix with the scores of the coefficients of the factors:"); round(res$coefscores,3)
```

Description

Performs the exploration of the data through the technique of animation Grand Tour.

Usage

```
GrandTour(data, method = "Interpolation", title = NA, xlabel = NA,
          ylabel = NA, size = 1.1, grid = TRUE, color = TRUE, linlab = NA,
          class = NA, classcolor = NA, posleg = 2, boxleg = TRUE,
          axesvar = TRUE, axes = TRUE, numrot = 200, choicerot = NA,
          savptc = FALSE, width = 3236, height = 2000, res = 300)
```

Arguments

<code>data</code>	Numerical data set.
<code>method</code>	Method used for rotations: "Interpolation" - Interpolation method (default), "Torus" - Torus method, "Pseudo" - Pseudo Grand Tour method.
<code>title</code>	Titles of the graphics, if not set, assumes the default text.
<code>xlabel</code>	Names the X axis, if not set, assumes the default text.
<code>ylabel</code>	Names the Y axis, if not set, assumes the default text.
<code>size</code>	Size of the points in the graphs.
<code>grid</code>	Put grid on graphs (default = TRUE).
<code>color</code>	Colored graphics (default = TRUE).
<code>linlab</code>	Vector with the labels for the observations.
<code>class</code>	Vector with names of data classes.
<code>classcolor</code>	Vector with the colors of the classes.
<code>posleg</code>	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
<code>boxleg</code>	Puts the frame in the caption (default = TRUE).
<code>axesvar</code>	Puts axes of rotation of the variables (default = TRUE).
<code>axes</code>	Plots the X and Y axes (default = TRUE).
<code>numrot</code>	Number of rotations (default = 200). If method = "Interpolation", numrot represents the angle of rotation.
<code>choicerot</code>	Choose specific rotation and display on the screen, or save the image if savptc = TRUE.
<code>savptc</code>	Saves graphics images to files (default = FALSE).
<code>width</code>	Graphics images width when savptc = TRUE (default = 3236).
<code>height</code>	Graphics images height when savptc = TRUE (default = 2000).
<code>res</code>	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).

Value

Graphs with rotations.

proj.data	Projected data.
vector.opt	Vector projection.
method	method used on Grand Tour.

Author(s)

Paulo Cesar Ossani
 Marcelo Angelo Cirillo

References

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Examples

```
data(iris) # database

res <- GrandTour(iris[,1:4], method = "Torus", title = NA, xlabel = NA, ylabel = NA,
  color = TRUE, linlab = NA, class = NA, posleg = 2, boxleg = TRUE,
  axesvar = TRUE, axes = FALSE, numrot = 10, choicerot = NA,
  savptc = FALSE, width = 3236, height = 2000, res = 300)

print("Projected data:"); res$proj.data
print("Projection vectors:"); res$vector.opt
print("Grand Tour projection method:"); res$method
```

```

res <- GrandTour(iris[,1:4], method = "Interpolation", title = NA, xlabel = NA, ylabel = NA,
  color = TRUE, linlab = NA, posleg = 2, boxleg = FALSE, axesvar = FALSE,
  axes = FALSE, numrot = 10, choicerot = NA, class = iris[,5],
  classcolor = c("goldenrod3", "gray53", "red"), savptc = FALSE,
  width = 3236, height = 2000, res = 300)

print("Projected data:"); res$proj.data
print("Projection vectors:"); res$vector.opt
print("Grand Tour projection method:"); res$method

```

GSVD

Generalized Singular Value Decomposition (GSVD).

Description

Given the matrix A of order $n \times m$, the generalized singular value decomposition (GSVD) involves the use of two sets of positive square matrices of order $n \times n$ and $m \times m$ respectively. These two matrices express constraints imposed, respectively, on the lines and columns of A .

Usage

```
GSVD(data, plin = NULL, pcol = NULL)
```

Arguments

<code>data</code>	Matrix used for decomposition.
<code>plin</code>	Weight for rows.
<code>pcol</code>	Weight for columns

Details

If `plin` or `pcol` is not used, it will be calculated as the usual singular value decomposition.

Value

<code>d</code>	Eigenvalues, that is, line vector with singular values of the decomposition.
<code>u</code>	Eigenvectors referring rows.
<code>v</code>	Eigenvectors referring columns.

Author(s)

Paulo Cesar Ossani
Marcelo Angelo Cirillo

References

Abdi, H. Singular Value Decomposition (SVD) and Generalized Singular Value Decomposition (GSVD). In: SALKIND, N. J. (Ed.). *Encyclopedia of measurement and statistics*. Thousand Oaks: Sage, 2007. p. 907-912.

Examples

```
data <- matrix(c(1,2,3,4,5,6,7,8,9,10,11,12), nrow = 4, ncol = 3)

svd(data) # Usual Singular Value Decomposition

GSVD(data) # GSVD with the same previous results

# GSVD with weights for rows and columns
GSVD(data, plin = c(0.1,0.5,2,1.5), pcol = c(1.3,2,0.8))
```

IM *Indicator matrix.*

Description

In the indicator matrix the elements are arranged in the form of *dummy* variables, in other words, 1 for a category chosen as a response variable and 0 for the other categories of the same variable.

Usage

```
IM(data, names = TRUE)
```

Arguments

data	Categorical data.
names	Include the names of the variables in the levels of the Indicator Matrix (default = TRUE).

Value

mtxIndc	Returns converted data in the indicator matrix.
---------	---

Author(s)

Paulo Cesar Ossani
Marcelo Angelo Cirillo

References

Rencher, A. C. *Methods of multivariate analysis*. 2th. ed. New York: J.Wiley, 2002. 708 p.

Examples

```
data <- matrix(c("S","S","N","N",1,2,3,4,"N","S","T","N"), nrow = 4, ncol = 3)

IM(data, names = FALSE)

data(DataQuali) # qualitative data set

IM(DataQuali, names = TRUE)
```

LocLab

Function for better position of the labels in the graphs.

Description

Function for better position of the labels in the graphs.

Usage

```
LocLab(x, y = NULL, labels = seq(along = x), cex = 1,
       method = c("SANN", "GA"), allowSmallOverlap = FALSE,
       trace = FALSE, shadotext = FALSE,
       doPlot = TRUE, ...)
```

Arguments

x	Coordinate x
y	Coordinate y
labels	The labels
cex	cex
method	Not used
allowSmallOverlap	Boolean
trace	Boolean
shadotext	Boolean
doPlot	Boolean
...	Other arguments passed to or from other methods

Value

See the text of the function.

Description

Performs Multidimensional Scaling (MDS) on a data set.

Usage

```
MDS(data, distance = "euclidean", title = NA, xlabel = NA,
     ylabel = NA, posleg = 2, boxleg = TRUE, axes = TRUE,
     size = 1.1, grid = TRUE, color = TRUE, linlab = NA,
     class = NA, classcolor = NA, savptc = FALSE, width = 3236,
     height = 2000, res = 300)
```

Arguments

data	Data to be analyzed.
distance	Metric of the distance: "euclidean" (default), "maximum", "manhattan", "canberra", "binary" or "minkowski".
title	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
posleg	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
boxleg	Puts the frame in the caption (default = TRUE).
axes	Plot the X and Y axes (default = TRUE).
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
linlab	Vector with the labels for the observations.
class	Vector with names of data classes.
classcolor	Vector with the colors of the classes.
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (default = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).

Value

Multidimensional Scaling.

mtxD Matrix of the distances.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

Mingoti, S. A. *Analise de dados atraves de metodos de estatistica multivariada: uma abordagem aplicada*. Belo Horizonte: UFMG, 2005. 297 p.

Rencher, A. C. *Methods of multivariate analysis*. 2th. ed. New York: J.Wiley, 2002. 708 p.

Examples

```
data(iris) # data set

data <- iris[,1:4]

cls <- iris[,5] # data class

md <- MDS(data = data, distance = "euclidean", title = NA, xlabel = NA,
          ylabel = NA, posleg = 2, boxleg = TRUE, axes = TRUE, color = TRUE,
          linlab = NA, class = cls, classcolor = c("goldenrod3", "gray53", "red"),
          savptc = FALSE, width = 3236, height = 2000, res = 300)

print("Matrix of the distances:"); md$mtxD
```

MFA

Multiple Factor Analysis (MFA).

Description

Perform Multiple Factor Analysis (MFA) on groups of variables. The groups of variables can be quantitative, qualitative, frequency (MFACT) data, or mixed data.

Usage

```
MFA(data, groups, typegroups = rep("n",length(groups)), namegroups = NULL)
```

Arguments

data	Data to be analyzed.
groups	Number of columns for each group in order following the order of data in 'data'.
typegroups	Type of group: "n" for numerical data (default), "c" for categorical data, "f" for frequency data.
namegroups	Names for each group.

Value

vtrG	Vector with the sizes of each group.
vtrNG	Vector with the names of each group.
vtrplin	Vector with the values used to balance the lines of the Z matrix.
vtrpcol	Vector with the values used to balance the columns of the Z matrix.
mtxZ	Matrix concatenated and balanced.
mtxA	Matrix of the eigenvalues (variances) with the proportions and proportions accumulated.
mtxU	Matrix U of the singular decomposition of the matrix Z.
mtxV	Matrix V of the singular decomposition of the matrix Z.
mtxF	Matrix global factor scores where the lines are the observations and the columns the components.
mtxEFG	Matrix of the factor scores by group.
mtxCCP	Matrix of the correlation of the principal components with original variables.
mtxEV	Matrix of the partial inertias / scores of the variables

Author(s)

Paulo Cesar Ossani
Marcelo Angelo Cirillo

References

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- Ossani, P. C.; Cirillo, M. A.; Borem, F. M.; Ribeiro, D. E.; Cortez, R. M. Quality of specialty coffees: a sensory evaluation by consumers using the MFACT technique. *Revista Ciencia Agronomica (UFC. Online)*, v. 48, p. 92-100, 2017.
- Pages, J. Analyse factorielle multiple appliquee aux variables qualitatives et aux donnees mixtes. *Revue de Statistique Appliquee*, Paris, v. 50, n. 4, p. 5-37, 2002.
- Pages, J.. Multiple factor analysis: main features and application to sensory data. *Revista Colombiana de Estadistica*, Bogota, v. 27, n. 1, p. 1-26, 2004.

See Also

[Plot.MFA](#)

Examples

```
data(DataMix) # mixed dataset

data <- DataMix[,2:ncol(DataMix)]

rownames(data) <- DataMix[1:nrow(DataMix),1]
```



```
group.names = c("Grade Cafes/Work", "Formation/Dedication", "Coffees")
mf <- MFA(data = data, c(2,2,2), typegroups = c("n","c","f"), group.names) # performs MFA
print("Principal Component Variances:"); round(mf$mtxA,2)
print("Matrix of the Partial Inertia / Score of the Variables:"); round(mf$mtxEV,2)
```

NormData

Normalizes the data.

Description

Function that normalizes the data globally, or by column.

Usage

```
NormData(data, type = 1)
```

Arguments

data	Data to be analyzed.
type	1 normalizes overall (default), 2 normalizes per column.

Value

dataNorm	Normalized data.
----------	------------------

Author(s)

Paulo Cesar Ossani
Marcelo Angelo Cirillo

Examples

```
data(DataQuan) # set of quantitative data
data <- DataQuan[,2:8]
res <- NormData(data, type = 1) # normalizes the data globally
res # Globally standardized data
sd(res) # overall standard deviation
mean(res) # overall mean
```

```
res <- NormData(data, type = 2) # normalizes the data per column
res # standardized data per column
apply(res, 2, sd) # standard deviation per column
colMeans(res) # column averages
```

NormTest	<i>Test of normality of the data.</i>
----------	---------------------------------------

Description

Check the normality of the data, based on the asymmetry coefficient test.

Usage

```
NormTest(data, sign = 0.05)
```

Arguments

data	Data to be analyzed.
sign	Test significance level (default 5%).

Value

statistic	Observed Chi-square value, that is, the test statistic.
chisquare	Chi-square value calculated.
gl	Degree of freedom.
p.value	p-value.

Author(s)

Paulo Cesar Ossani
Marcelo Angelo Cirillo

References

Mingoti, S. A. *Análise de dados através de métodos de estatística multivariada: uma abordagem aplicada*. Belo Horizonte: UFMG, 2005. 297 p.

Rencher, A. C. *Methods of Multivariate Analysis*. 2th. ed. New York: J.Wiley, 2002. 708 p.

Ferreira, D. F. *Estatística Multivariada*. 2a ed. revisada e ampliada. Lavras: Editora UFLA, 2011. 676 p.

Examples

```
data <- cbind(rnorm(100,2,3), rnorm(100,1,2))
```

```
NormTest(data)
```

```
plot(density(data))
```

```
data <- cbind(rexp(200,3), rexp(200,3))
```

```
NormTest(data, sign = 0.01)
```

```
plot(density(data))
```

PCA

Principal Components Analysis (PCA).

Description

Performs principal component analysis (PCA) in a data set.

Usage

```
PCA(data, type = 1)
```

Arguments

data	Data to be analyzed.
type	1 for analysis using the covariance matrix (default), 2 for analysis using the correlation matrix.

Value

mtxC	Matrix of covariance or correlation according to "type".
mtxAutv1r	Matrix of eigenvalues (variances) with the proportions and proportions accumulated.
mtxAutvec	Matrix of eigenvectors - principal components.
mtxVCP	Matrix of covariance of the principal components with the original variables.
mtxCCP	Matrix of correlation of the principal components with the original variables.
mtxscores	Matrix with scores of the principal components.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

Hotelling, H. Analysis of a complex of statistical variables into principal components. *Journal of Educational Psychology*, Arlington, v. 24, p. 417-441, Sept. 1933.

Mingoti, S. A. *Análise de dados através de métodos de estatística multivariada: uma abordagem aplicada*. Belo Horizonte: UFMG, 2005. 297 p.

Ferreira, D. F. *Estatística Multivariada*. 2a ed. revisada e ampliada. Lavras: Editora UFLA, 2011. 676 p.

Rencher, A. C. *Methods of multivariate analysis*. 2th. ed. New York: J.Wiley, 2002. 708 p.

See Also

[Plot.PCA](#)

Examples

```
data(DataQuan) # set of quantitative data

data <- DataQuan[,2:8]

rownames(data) <- DataQuan[1:nrow(DataQuan),1]

pc <- PCA(data, 2) # performs the PCA

print("Covariance matrix / Correlation:"); round(pc$mtxC,2)

print("Principal Components:"); round(pc$mtxAutvec,2)

print("Principal Component Variances:"); round(pc$mtxAutv1r,2)

print("Covariance of the Principal Components:"); round(pc$mtxVCP,2)

print("Correlation of the Principal Components:"); round(pc$mtxCCP,2)

print("Scores of the Principal Components:"); round(pc$mtxscores,2)
```

Plot.CA

Graphs of the simple (CA) and multiple correspondence analysis (MCA).

Description

Graphs of the simple (CA) and multiple correspondence analysis (MCA).

Usage

```
Plot.CA(CA, titles = NA, xlabel = NA, ylabel = NA, size = 1.1,
        grid = TRUE, color = TRUE, linlab = NA, axes = TRUE,
        savptc = FALSE, width = 3236, height = 2000, res = 300,
        casc = TRUE)
```

Arguments

CA	Data of the CA function.
titles	Titles of the graphics, if not set, assumes the default text..
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
linlab	Vector with the labels for the observations.
axes	Plots the X and Y axes (default = TRUE).
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (default = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
casc	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Returns several graphs.

Author(s)

Paulo Cesar Ossani
Marcelo Angelo Cirillo

See Also

[CA](#)

Examples

```
data(DataFreq) # frequency data set

data <- DataFreq[,2:ncol(DataFreq)]

rownames(data) <- DataFreq[1:nrow(DataFreq),1]

res <- CA(data, "f") # performs CA

tit <- c("Scree-plot", "Observations", "Variables", "Observations / Variables")

Plot.CA(res, titles = tit, xlabel = NA, ylabel = NA, axes = TRUE,
        color = TRUE, linlab = rownames(data), savptc = FALSE,
        width = 3236, height = 2000, res = 300, casc = FALSE)
```

```

data(DataQuali) # qualitative data set

data <- DataQuali[,2:ncol(DataQuali)]

res <- CA(data, "c", "b") # performs CA

tit <- c("", "", "Graph of the variables")

Plot.CA(res, titles = tit, xlabel = NA, ylabel = NA,
        color = TRUE, linlab = NA, savptc = FALSE,
        width = 3236, height = 2000, res = 300,
        axes = TRUE, casc = FALSE)

```

Plot.CCA

Graphs of the Canonical Correlation Analysis (CCA).

Description

Graphs of the Canonical Correlation Analysis (CCA).

Usage

```

Plot.CCA(CCA, titles = NA, xlabel = NA, ylabel = NA, size = 1.1,
        grid = TRUE, color = TRUE, axes = TRUE, savptc = FALSE,
        width = 3236, height = 2000, res = 300, casc = TRUE)

```

Arguments

CCA	Data of the CCA function.
titles	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
axes	Plots the X and Y axes (default = TRUE).
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (default = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
casc	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Returns several graphs.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

See Also

[CCA](#)

Examples

```
data(DataMix) # database

data <- DataMix[,2:ncol(DataMix)]

rownames(data) <- DataMix[,1]

X <- data[,1:2]

Y <- data[,5:6]

res <- CCA(X, Y, type = 2, test = "Bartlett", sign = 0.05) # performs CCA

tit <- c("Scree-plot", "Correlations", "Scores of the group X", "Scores of the group Y")

Plot.CCA(res, titles = tit, xlabel = NA, ylabel = NA,
         color = TRUE, savptc = FALSE, width = 3236,
         height = 2000, res = 300, axes = TRUE,
         casc = FALSE)
```

Plot.Cor

Plot of correlations between variables.

Description

It performs the correlations between the variables of a database and presents it in graph form.

Usage

```
Plot.Cor(data, title = NA, grid = TRUE, leg = TRUE, boxleg = FALSE,
         text = FALSE, arrow = TRUE, color = TRUE, namesvar = NA,
         savptc = FALSE, width = 3236, height = 2000, res = 300)
```

Arguments

<code>data</code>	Numeric data set.
<code>title</code>	Title for the plot, if not defined it assumes standard text.
<code>grid</code>	Puts grid on plot (default = TRUE).
<code>leg</code>	Put the legend on the plot (default = TRUE)
<code>boxleg</code>	Put frame in the legend (default = FALSE).
<code>text</code>	Puts correlation values in circles (default = FALSE).
<code>arrow</code>	Positive (up) and negative (down) correlation arrows (default = TRUE).
<code>color</code>	Colorful plot (default = TRUE).
<code>namesvar</code>	Vector with the variable names, if omitted it assumes the names in 'date'.
<code>savptc</code>	Saves graphics images to files (default = FALSE).
<code>width</code>	Graphics images width when savptc = TRUE (default = 3236).
<code>height</code>	Graphics images height when savptc = TRUE (default = 2000).
<code>res</code>	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).

Value

Plot with the correlations between the variables in 'date'.

Author(s)

Paulo Cesar Ossani

Examples

```
data(iris) # data set
```

```
Plot.Cor(data = iris[,1:4], title = NA, grid = TRUE, leg = TRUE, boxleg = FALSE,  
text = FALSE, arrow = TRUE, color = TRUE, namesvar = NA, savptc = FALSE,  
width = 3236, height = 2000, res = 300)
```

```
Plot.Cor(data = iris[,1:4], title = NA, grid = TRUE, leg = TRUE, boxleg = FALSE,  
text = TRUE, arrow = TRUE, color = TRUE, namesvar = c("A1", "B2", "C3", "D4"),  
savptc = FALSE, width = 3236, height = 2000, res = 300)
```

Plot.FA *Graphs of the Factorial Analysis (FA).*

Description

Graphs of the Factorial Analysis (FA).

Usage

```
Plot.FA(FA, titles = NA, xlabel = NA, ylabel = NA, size = 1.1,
        grid = TRUE, color = TRUE, linlab = NA, axes = TRUE, class = NA,
        classcolor = NA, posleg = 2, boxleg = TRUE, savptc = FALSE,
        width = 3236, height = 2000, res = 300, casc = TRUE)
```

Arguments

FA	Data of the FA function.
titles	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
linlab	Vector with the labels for the observations.
axes	Plots the X and Y axes (default = TRUE).
class	Vector with names of data classes.
classcolor	Vector with the colors of the classes.
posleg	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
boxleg	Puts the frame in the caption (default = TRUE).
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (default = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
casc	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Returns several graphs.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

See Also[FA](#)**Examples**

```
data(iris) # conjunto de dados

data <- iris[,1:4]

cls <- iris[,5] # classe dos dados

res <- FA(data, method = "PC", type = 2, nfactor = 3)

tit <- c("Scree-plot", "Scores of the Observations", "Factorial Loadings", "Biplot")

cls <- as.character(iris[,5])

Plot.FA(FA = res, titles = tit, xlabel = NA, ylabel = NA,
        color = TRUE, linlab = NA, savptc = FALSE, size = 1.1,
        posleg = 1, boxleg = FALSE, class = cls, axes = TRUE,
        classcolor = c("blue3", "red", "goldenrod3"),
        width = 3236, height = 2000, res = 300, casc = FALSE)
```

Plot.MFA

Graphics of the Multiple Factor Analysis (MFA).

Description

Graphics of the Multiple Factor Analysis (MFA).

Usage

```
Plot.MFA(MFA, titles = NA, xlabel = NA, ylabel = NA,
         posleg = 2, boxleg = TRUE, size = 1.1, grid = TRUE,
         color = TRUE, groupcolor = NA, namarr = FALSE,
         linlab = NA, savptc = FALSE, width = 3236,
         height = 2000, res = 300, casc = TRUE)
```

Arguments

MFA	Data of the MFA function.
titles	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
posleg	1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
boxleg	Puts frame in legend (default = TRUE).
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
groupscolor	Vector with the colors of the groups.
namarr	Puts the points names in the cloud around the centroid in the graph corresponding to the global analysis of the Individuals and Variables (default = FALSE).
linlab	Vector with the labels for the observations, if not set, assumes the default text.
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (default = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
casc	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Returns several graphs.

Author(s)

Paulo Cesar Ossani
Marcelo Angelo Cirillo

See Also

[MFA](#)

Examples

```
data(DataMix) # set of mixed data

data <- DataMix[,2:ncol(DataMix)]

rownames(data) <- DataMix[1:nrow(DataMix),1]
```

```

group.names = c("Grade Cafes/Work", "Formation/Dedication", "Coffees")

mf <- MFA(data, c(2,2,2), typegroups = c("n","c","f"), group.names) # performs MFA

tit <- c("Scree-Plot","Observations","Observations/Variables",
        "Correlation Circle","Inertia of the Variable Groups")

Plot.MFA(MFA = mf, titles = tit, xlabel = NA, ylabel = NA,
         posleg = 2, boxleg = FALSE, color = TRUE,
         groupscolor = c("blue3","red","goldenrod3"),
         namarr = FALSE, linlab = NA, savptc = FALSE,
         width = 3236, height = 2000, res = 300,
         casc = TRUE) # plotting several graphs on the screen

Plot.MFA(MFA = mf, titles = tit, xlabel = NA, ylabel = NA,
         posleg = 2, boxleg = FALSE, color = TRUE,
         namarr = FALSE, linlab = rep("A?",10),
         savptc = FALSE, width = 3236, height = 2000,
         res = 300, casc = TRUE) # plotting several graphs on the screen

```

Plot.PCA

Graphs of the Principal Components Analysis (PCA).

Description

Graphs of the Principal Components Analysis (PCA).

Usage

```

Plot.PCA(PC, titles = NA, xlabel = NA, ylabel = NA, size = 1.1,
         grid = TRUE, color = TRUE, linlab = NA, axes = TRUE, class = NA,
         classcolor = NA, posleg = 2, boxleg = TRUE, savptc = FALSE,
         width = 3236, height = 2000, res = 300, casc = TRUE)

```

Arguments

PC	Data of the PCA function.
titles	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
linlab	Vector with the labels for the observations.
axes	Plots the X and Y axes (default = TRUE).

<code>class</code>	Vector with names of data classes.
<code>classcolor</code>	Vector with the colors of the classes.
<code>posleg</code>	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
<code>boxleg</code>	Puts the frame in the caption (default = TRUE).
<code>savptc</code>	Saves graphics images to files (default = FALSE).
<code>width</code>	Graphics images width when <code>savptc = TRUE</code> (default = 3236).
<code>height</code>	Graphics images height when <code>savptc = TRUE</code> (default = 2000).
<code>res</code>	Nominal resolution in ppi of the graphics images when <code>savptc = TRUE</code> (default = 300).
<code>cas</code>	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Returns several graphs.

Author(s)

Paulo Cesar Ossani
Marcelo Angelo Cirillo

See Also

[PCA](#)

Examples

```
data(iris) # data set

data <- iris[,1:4]

cls <- iris[,5] # data class

pc <- PCA(data, 2)

tit <- c("Scree-plot", "Observations", "Correlations")

cls <- as.character(iris[,5])

Plot.PCA(PC = pc, titles = tit, xlabel = NA, ylabel = NA,
         color = TRUE, linlab = NA, savptc = FALSE, size = 1.1,
         posleg = 2, boxleg = FALSE, class = cls, axes = TRUE,
         classcolor = c("blue3", "red", "goldenrod3"),
         width = 3236, height = 2000, res = 300, cas = FALSE)
```

Plot.PP

*Graphics of the Projection Pursuit (PP).***Description**

Graphics of the Projection Pursuit (PP).

Usage

```
Plot.PP(PP, titles = NA, xlabel = NA, ylabel = NA, posleg = 2, boxleg = TRUE,
        size = 1.1, grid = TRUE, color = TRUE, classcolor = NA, linlab = NA,
        axesvar = TRUE, axes = TRUE, savptc = FALSE, width = 3236, height = 2000,
        res = 300, casc = TRUE)
```

Arguments

PP	Data of the PP_Optimizer function.
titles	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
posleg	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
boxleg	Puts the frame in the caption (default = TRUE).
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
classcolor	Vector with the colors of the classes.
linlab	Vector with the labels for the observations.
axesvar	Puts axes of rotation of the variables, only when dimproj > 1 (default = TRUE).
axes	Plots the X and Y axes (default = TRUE).
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (default = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
casc	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Graph of the evolution of the indices, and graphs whose data were reduced in two dimensions.

Author(s)

Paulo Cesar Ossani
Marcelo Angelo Cirillo

See Also

[PP_Optimizer](#) and [PP_Index](#)

Examples

```
data(iris) # dataset

# Example 1 - Without the classes in the data
data <- iris[,1:4]

findex <- "kurtosismax" # index function

dim <- 1 # dimension of data projection

sphere <- TRUE # spherical data

res <- PP_Optimizer(data = data, class = NA, findex = findex,
                    optmethod = "GTSA", dimproj = dim, sphere = sphere,
                    weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                    eps = 1e-3, maxiter = 500, half = 30)

Plot.PP(res, titles = NA, posleg = 1, boxleg = FALSE, color = TRUE,
         linlab = NA, axesvar = TRUE, axes = TRUE, savptc = FALSE,
         width = 3236, height = 2000, res = 300, casc = FALSE)

# Example 2 - With the classes in the data
class <- iris[,5] # data class

res <- PP_Optimizer(data = data, class = class, findex = findex,
                    optmethod = "GTSA", dimproj = dim, sphere = sphere,
                    weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                    eps = 1e-3, maxiter = 500, half = 30)

tit <- c(NA,"Graph example") # titles for the graphics

Plot.PP(res, titles = tit, posleg = 1, boxleg = FALSE, color = TRUE,
         classcolor = c("blue3","red","goldenrod3"), linlab = NA,
         axesvar = TRUE, axes = TRUE, savptc = FALSE, width = 3236,
         height = 2000, res = 300, casc = FALSE)

# Example 3 - Without the classes in the data, but informing
#             the classes in the plot function
res <- PP_Optimizer(data = data, class = NA, findex = "Moment",
                    optmethod = "GTSA", dimproj = 2, sphere = sphere,
                    weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
```

```

        eps = 1e-3, maxiter = 500, half = 30)

lin <- c(rep("a",50),rep("b",50),rep("c",50)) # data class

Plot.PP(res, titles = NA, posleg = 1, boxleg = FALSE, color = TRUE,
        linlab = lin, axesvar = TRUE, axes = TRUE, savptc = FALSE,
        width = 3236, height = 2000, res = 300, casc = FALSE)

# Example 4 - With the classes in the data, but not informed in plot function
class <- iris[,5] # data class

dim <- 2 # dimension of data projection

findex <- "lda" # index function

res <- PP_Optimizer(data = data, class = class, findex = findex,
                   optmethod = "GTSA", dimproj = dim, sphere = sphere,
                   weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                   eps = 1e-3, maxiter = 500, half = 30)

tit <- c("",NA) # titles for the graphics

Plot.PP(res, titles = tit, posleg = 1, boxleg = FALSE, color = TRUE,
        linlab = NA, axesvar = TRUE, axes = TRUE, savptc = FALSE,
        width = 3236, height = 2000, res = 300, casc = FALSE)

```

Plot.Regr

Graphs of the linear regression results.

Description

Graphs of the linear regression results.

Usage

```

Plot.Regr(Reg, typegraf = "Scatterplot", title = NA, xlabel = NA,
          ylabel = NA, namevary = NA, namevarx = NA, size = 1.1,
          grid = TRUE, color = TRUE, intconf = TRUE, intprev = TRUE,
          savptc = FALSE, width = 3236, height = 2000, res = 300,
          casc = TRUE)

```

Arguments

Reg	Regression function data.
typegraf	Type of graphic: "Scatterplot" - Scatterplot 2 to 2, "Regression" - Graph of the linear regression,

	"QQPlot" - Graph of the normal probability of the residues, "Histogram" - Histogram of the residues, "Fits" - Graph of the adjusted values versus residuals, "Order" - Graph of the order of the observations versus the residuals.
title	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
namevary	Variable name Y, if not set, assumes the default text.
namevarx	Name of the variable X, or variables X, if not set, assumes the default text.
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
intconf	Case typegraf = "Regression". Graphics with confidence interval (default = TRUE).
intprev	Case typegraf = "Regression". Graphics with predictive interval (default = TRUE).
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (default = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
cas	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Returns several graphs.

Author(s)

Paulo Cesar Ossani

See Also

[Regr](#)

Examples

```
data(DataMix)

Y <- DataMix[,2]

X <- DataMix[,7]

name.y <- "Medium grade"

name.x <- "Commercial coffees"
```

```

res <- Reqr(Y, X, namevarx = name.x , intercept = TRUE, sigf = 0.05)

tit <- c("Scatterplot")
Plot.Reqr(res, typegraf = "Scatterplot", title = tit,
          namevary = name.y, namevarx = name.x, color = TRUE,
          savptc = FALSE, width = 3236, height = 2000, res = 300)

tit <- c("Scatterplot with the adjusted line")
Plot.Reqr(res, typegraf = "Regression", title = tit,
          xlabel = name.x, ylabel = name.y, color = TRUE,
          intconf = TRUE, intprev = TRUE, savptc = FALSE,
          width = 3236, height = 2000, res = 300)

dev.new() # necessary to not overlap the following graphs to the previous graph

par(mfrow = c(2,2))

Plot.Reqr(res, typegraf = "QQPlot", casc = FALSE)
Plot.Reqr(res, typegraf = "Histogram", casc = FALSE)
Plot.Reqr(res, typegraf = "Fits", casc = FALSE)
Plot.Reqr(res, typegraf = "Order", casc = FALSE)

```

 PP_Index

Function to find the Projection Pursuit indexes (PP).

Description

Function used to find Projection Pursuit indexes (PP).

Usage

```

PP_Index(data, class = NA, vector.proj = NA,
         findex = "HOLES", dimproj = 2, weight = TRUE,
         lambda = 0.1, r = 1, ck = NA)

```

Arguments

data	Numeric dataset without class information.
class	Vector with names of data classes.
vector.proj	Vector projection.
findex	Projection index function to be used: "lda" - LDA index, "pda" - PDA index, "lr" - Lr index, "holes" - Holes index (default), "cm" - Central Mass index, "pca" - PCA index, "friedmantukey" - Friedman Tukey index,

	"entropy" - Entropy index,
	"legendre" - Legendre index,
	"laguerrefourier" - Laguerre Fourier index,
	"hermite" - Hermite index,
	"naturalhermite" - Natural Hermite index,
	"kurtosismax" - Maximum kurtosis index,
	"kurtosimin" - Minimum kurtosis index,
	"moment" - Moment index,
	"mf" - MF index,
	"chi" - Chi-square index.
dimproj	Dimension of data projection (default = 2).
weight	Used in index LDA, PDA and Lr to weight the calculations for the number of elements in each class (default = TRUE).
lambda	Used in the PDA index (default = 0.1).
r	Used in the Lr index (default = 1).
ck	Internal use of the CHI index function.

Value

num.class	Number of classes.
class.names	Class names.
findex	Projection index function used.
vector.proj	Projection vectors found.
index	Projection index found in the process.

Author(s)

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 Marcelo Angelo Cirillo

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See Also

[PP_Optimizer](#) and [Plot.PP](#)

Examples

```
data(iris) # data set

data <- iris[,1:4]

# Example 1 - Without the classes in the data
ind <- PP_Index(data = data, class = NA, vector.proj = NA,
               findex = "moment", dimproj = 2, weight = TRUE,
               lambda = 0.1, r = 1)

print("Number of classes:"); ind$num.class
print("class Names:"); ind$class.names
print("Projection index function:"); ind$findex
print("Projection vectors:"); ind$vector.proj
print("Projection index:"); ind$index

# Example 2 - With the classes in the data
class <- iris[,5] # data class

findex <- "pda" # index function

sphere <- TRUE # spherical data
```

```

res <- PP_Optimizer(data = data, class = class, findex = findex,
                  optmethod = "SA", dimproj = 2, sphere = sphere,
                  weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                  eps = 1e-3, maxiter = 1000, half = 30)

# Comparing the result obtained
if (match(toupper(findex),c("LDA", "PDA", "LR"), nomatch = 0) > 0) {
  if (sphere) {
    data <- apply(predict(prcomp(data)), 2, scale) # spherical data
  }
} else data <- as.matrix(res$proj.data[,1:Dim])

ind <- PP_Index(data = data, class = class, vector.proj = res$vector.opt,
               findex = findex, dimproj = 2, weight = TRUE, lambda = 0.1,
               r = 1)

print("Number of classes:"); ind$num.class
print("class Names:"); ind$class.names
print("Projection index function:"); ind$findex
print("Projection vectors:"); ind$vector.proj
print("Projection index:"); ind$index
print("Optimized Projection index:"); res$index[length(res$index)]

```

 PP_Optimizer

Optimization function of the Projection Pursuit index (PP).

Description

Optimization function of the Projection Pursuit index (PP).

Usage

```

PP_Optimizer(data, class = NA, findex = "HOLES",
             dimproj = 2, sphere = TRUE, optmethod = "GTSA",
             weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
             eps = 1e-3, maxiter = 3000, half = 30)

```

Arguments

data	Numeric dataset without class information.
class	Vector with names of data classes.
findex	Projection index function to be used: "lda" - LDA index, "pda" - PDA index, "lr" - Lr index, "holes" - Holes index (default), "cm" - Central Mass index,

	"pca" - PCA index, "friedmantukey" - Friedman Tukey index, "entropy" - Entropy index, "legendre" - Legendre index, "laguerrefourier" - Laguerre Fourier index, "hermite" - Hermite index, "naturalhermite" - Natural Hermite index, "kurtosismax" - Maximum kurtosis index, "kurtosismin" - Minimum kurtosis index, "moment" - Moment index, "mf" - MF index, "chi" - Chi-square index.
dimproj	Dimension of the data projection (default = 2).
sphere	Spherical data (default = TRUE).
optmethod	Optimization method GTSA - Grand Tour Simulated Annealing or SA - Simulated Annealing (default = "GTSA").
weight	Used in index LDA, PDA and Lr to weight the calculations for the number of elements in each class (default = TRUE).
lambda	Used in the PDA index (default = 0.1).
r	Used in the Lr index (default = 1).
cooling	Cooling rate (default = 0.9).
eps	Approximation accuracy for cooling (default = 1e-3).
maxiter	Maximum number of iterations of the algorithm (default = 3000).
half	Number of steps without incrementing the index, then decreasing the cooling value (default = 30).

Value

num.class	Number of classes.
class.names	Class names.
proj.data	Projected data.
vector.opt	Projection vectors found.
index	Vector with the projection indices found in the process, converging to the maximum, or the minimum.
findex	Projection index function used.

Author(s)

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Marcelo Angelo Cirillo

References

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Lee, E.; Cook, D.; Klinke, S.; Lumley, T. Projection pursuit for exploratory supervised classification. *Journal of Computational and Graphical Statistics*, 14(4):831-846, 2005.

See Also

[Plot.PP](#) and [PP_Index](#)

Examples

```
data(iris) # data set

# Example 1 - Without the classes in the data
data <- iris[,1:4]

class <- NA # data class

findex <- "kurtosismax" # index function

dim <- 1 # dimension of data projection

sphere <- TRUE # spherical data

res <- PP_Optimizer(data = data, class = class, findex = findex,
                   optmethod = "GTSA", dimproj = dim, sphere = sphere,
                   weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                   eps = 1e-3, maxiter = 1000, half = 30)

print("Number of classes:"); res$num.class
print("class Names:"); res$class.names
print("Projection index function:"); res$findex
print("Projected data:"); res$proj.data
print("Projection vectors:"); res$vector.opt
print("Projection index:"); res$index

# Example 2 - With the classes in the data
class <- iris[,5] # classe dos dados

res <- PP_Optimizer(data = data, class = class, findex = findex,
                   optmethod = "GTSA", dimproj = dim, sphere = sphere,
                   weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                   eps = 1e-3, maxiter = 1000, half = 30)

print("Number of classes:"); res$num.class
print("class Names:"); res$class.names
print("Projection index function:"); res$findex
```

```
print("Projected data:"); res$proj.data
print("Projection vectors:"); res$vector.opt
print("Projection index:"); res$index
```

 Repr

Linear regression.

Description

Performs linear regression on a data set.

Usage

```
Regr(Y, X, namevarx = NA, intercept = TRUE, sigf = 0.05)
```

Arguments

Y	Variable response.
X	Regression variables.
namevarx	Name of the variable, or variables X, if not set, assumes the default text.
intercept	Consider the intercept in the regression (default = TRUE).
sigf	Level of significance of residue tests(default = 5%).

Value

Betas	Regression coefficients.
CovBetas	Covariance matrix of the regression coefficients.
ICc	Confidence interval of the regression coefficients.
hip.test	Hypothesis test of the regression coefficients.
ANOVA	Regression analysis of the variance.
R	Determination coefficient.
Rc	Corrected coefficient of determination.
Ra	Adjusted coefficient of determination.
QME	Variance of the residues.
ICQME	Confidence interval of the residue variance.
prev	Prediction of the regression fit.
IPp	Predictions interval
ICp	Interval of prediction confidence
error	Residuals of the regression fit.
error.test	It returns to 5% of significance the test of independence, normality and homogeneity of the variance of the residues.

Author(s)

Paulo Cesar Ossani

References

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Rencher, A. C. *Methods of multivariate analysis*. 2th. ed. New York: J.Wiley, 2002. 708 p.

See Also

[Plot.Regr](#)

Examples

```
data(DataMix)

Y <- DataMix[,2]

X <- DataMix[,6:7]

name.x <- c("Special Coffees", "Commercial Coffees")

res <- Repr(Y, X, namevarx = name.x , intercept = TRUE, sigf = 0.05)

print("Regression Coefficients:"); round(res$Betas,4)
print("Analysis of Variance:"); res$ANOVA
print("Hypothesis test of regression coefficients:"); round(res$hip.test,4)
print("Determination coefficient:"); round(res$R,4)
print("Corrected coefficient of determination:"); round(res$Rc,4)
print("Adjusted coefficient of determination:"); round(res$Ra,4)
print("Tests of the residues"); res$error.test
```

Scatter

Scatter plot.

Description

Performs the scatter plot.

Usage

```
Scatter(data, ellipse = TRUE, ellipse.level = 0.95, rectangle = FALSE,
        title = NA, xlabel = NA, ylabel = NA, posleg = 2, boxleg = TRUE,
        axes = TRUE, size = 1.1, grid = TRUE, color = TRUE, linlab = NA,
        class = NA, classcolor = NA, savptc = FALSE, width = 3236,
        height = 2000, res = 300)
```

Arguments

data	Data with x and y coordinates.
ellipse	Place an ellipse around the classes (default = TRUE).
ellipse.level	Significance level of the ellipse (default = 0.95).
rectangle	Place rectangle to differentiate classes (default = FALSE).
title	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
posleg	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
boxleg	Puts the frame in the caption (default = TRUE).
axes	Plots the X and Y axes (default = TRUE).
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
linlab	Vector with the labels for the observations.
class	Vector with names of data classes.
classcolor	Vector with the colors of the classes.
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (default = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).

Value

Scatter plot.

Author(s)

Paulo Cesar Ossani

References

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- Anton, H.; Rorres, C. *Elementary linear algebra: applications version*. 10th ed. New Jersey: John Wiley & Sons, 2010. 768 p.

Examples

```
data(iris) # data set

data <- iris[,3:4]

cls <- iris[,5] # data class

Scatter(data, ellipse = TRUE, ellipse.level = 0.95, rectangle = FALSE,
        title = NA, xlabel = NA, ylabel = NA, posleg = 1, boxleg = FALSE,
        axes = FALSE, size = 1.1, grid = TRUE, color = TRUE, linlab = NA,
        class = cls, classcolor = c("goldenrod3", "blue", "red"),
        savptc = FALSE, width = 3236, height = 2000, res = 300)

Scatter(data, ellipse = FALSE, ellipse.level = 0.95, rectangle = TRUE,
        title = NA, xlabel = NA, ylabel = NA, posleg = 1, boxleg = TRUE,
        axes = FALSE, size = 1.1, grid = TRUE, color = TRUE, linlab = NA,
        class = cls, classcolor = c("goldenrod3", "blue", "red"),
        savptc = FALSE, width = 3236, height = 2000, res = 300)
```

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