

# Package ‘DBfit’

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**Type** Package

**Title** A Double Bootstrap Method for Analyzing Linear Models with Autoregressive Errors

**Version** 2.0

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**Author** Joseph W. McKean and Shaofeng Zhang

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**Description** Computes the double bootstrap as discussed in McKnight, McKean, and Huitema (2000) <[doi:10.1037/1082-989X.5.1.87](https://doi.org/10.1037/1082-989X.5.1.87)>.

The double bootstrap method provides a better fit for a linear model with autoregressive errors than ARIMA when the sample size is small.

**License** GPL (>= 2)

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## Description

Computes the double bootstrap as discussed in McKnight, McKean, and Huitema (2000) <doi:10.1037/1082-989X.5.1.87>. The double bootstrap method provides a better fit for a linear model with autoregressive errors than ARIMA when the sample size is small.

## Details

The DESCRIPTION file:

```

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Version:      2.0
Date:         2021-04-30
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```

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**Author(s)**

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**References**

McKnight, S. D., McKean, J. W., and Huitema, B. E. (2000). A double bootstrap method to analyze linear models with autoregressive error terms. *Psychological methods*, 5 (1), 87. Shaofeng Zhang (2017). Ph.D. Dissertation.

---

boot1

*First Bootstrap Procedure For parameter estimations*

---

**Description**

Function performing the first bootstrap procedure to yield the parameter estimates

**Usage**

boot1(y, phi1, arp, nbs, x, allb, method, scores)

**Arguments**

y	the response variable
phi1	the Durbin two-stage estimate of the autoregressive parameter rho
arp	the order of autoregressive errors
nbs	the bootstrap size
x	the original design matrix (including intercept), without centering
allb	all the Durbin two-stage estimates of the regression coefficients
method	If "OLS", uses the ordinary least square; If "RANK", uses the rank-based fit
scores	Default is Wilcoxon scores

**Value**

An estimate of the bias is returned

**Note**

This function is for internal use. The main function for users is `dbfit`.

---

boot2

*First Bootstrap Procedure For parameter estimations*


---

**Description**

Function performing the second bootstrap procedure to yield the inference of the regression coefficients

**Usage**

```
boot2(y, xcopy, phi1, beta, nbs, method, scores)
```

**Arguments**

y	the response variable
xcopy	the original design matrix (including intercept), without centering
phi1	the estimate of the autoregressive parameter rho from the first bootstrap procedure
beta	the estimates of the regression coefficients from the first bootstrap procedure
nbs	the bootstrap size
method	If "OLS", uses the ordinary least square; If "RANK", uses rank-based fit
scores	Default is Wilcoxon scores

**Value**

betacov	the estimate of var-cov matrix of betas
allbeta	the estimates of betas inside of the second bootstrap, not the final estimates of betas. The final estimates of betas are still from boot1.
rhostar	the estimates of rho inside of the second bootstrap, not the final estimates of rho. The final estimate(s) of rho are still from boot1.
MSEstar	MSE used inside of the second bootstrap.

**Note**

This function is for internal use. The main function for users is `dbfit`

---

dbfit

*The main function for the double bootstrap method*

---

**Description**

This function is used to implement the double bootstrap method. It is used to yield estimates of both regression coefficients and autoregressive parameters(rho), and also the inference of them.

**Usage**

```
## Default S3 method:
dbfit(x, y, arp, nbs = 500, nbscov = 500,
conf = 0.95, correction = TRUE, method = "OLS", scores, ...)
```

**Arguments**

x	the design matrix, including intercept, i.e. the first column being ones.
y	the response variable.
arp	the order of autoregressive errors.
nbs	the bootstrap size for the first bootstrap procedure. Default is 500.
nbscov	the bootstrap size for the second bootstrap procedure. Default is 500.
conf	the confidence level of CI for rho, default is 0.95.
correction	logical. Currently, ONLY works for order 1, i.e. for order > 1, this correction will not get involved. If TRUE, uses the correction for cases that the estimate of rho is 0.99. Default is TRUE.
method	the method to be used for fitting. If "OLS", uses the ordinary least square <code>lm</code> ; If "RANK", uses the rank-based fit <code>rfit</code> .
scores	Default is Wilcoxon scores
...	additional arguments to be passed to fitting routines

**Details**

Computes the double bootstrap as discussed in McKnight, McKean, and Huitema (2000). For details, see the references.

**Value**

coefficients	the estimates of regression coefficients based on the first bootstrap procedure
rho1	the Durbin two-stage estimate of the autoregressive parameter rho
adjar	the estimates of regression coefficients based on the first bootstrap procedure
mse	the mean square error
rho_CI_1	the first type of CI for rho, see the second reference for details.
rho_CI_2	the second type of CI for rho, see the second reference for details.
rho_CI_3	the third type of CI for rho, see the second reference for details.
betacov	the estimate of the variance-covariance matrix of betas
tabbeta	a table of point estimates, SE's, test statistics and p-values.
flag99	an indicator; if 1, it indicates the original fit yields an estimate of rho to be 0.99. When the correction is requested (default), the correction procedure kicks in, and the final estimates of rho is corrected. Only valid if order 1 is specified.
residuals	the residuals, that is response minus fitted values.
fitted.values	the fitted mean values.

**Author(s)**

Joseph W. McKean and Shaofeng Zhang

**References**

McKnight, S. D., McKean, J. W., and Huitema, B. E. (2000). A double bootstrap method to analyze linear models with autoregressive error terms. *Psychological methods*, 5 (1), 87.

Shaofeng Zhang (2017). Ph.D. Dissertation.

**See Also**

dbfit.formula

**Examples**

```
# make sure the dependent package Rfit is installed
# To save users time, we set both bootstrap sizes to be 100 in this example.
# Defaults are both 500.

# data(testdata)
# This data is generated by a two-phase design, with autoregressive order being one,
# autoregressive coefficient being 0.6 and all regression coefficients being 0.
# Both the first and second phase have 20 observations.
```

```

# y <- testdata[,5]
# x <- testdata[,1:4]
# fit1 <- dbfit(x,y,1, nbs = 100, nbscov = 100) # OLS fit, default
# summary(fit1)
# Note that the CI's of autoregressive coef are not shown in the summary.
# Instead, they are attributes of model fit.
# fit1$rho_CI_1

# fit2 <- dbfit(x,y,1, nbs = 100, nbscov = 100 ,method="RANK") # rank-based fit

# When fitting with autoregressive order 2,
# the estimate of the second order autoregressive coefficient should not be significant,
# since this data is generated with order 1.

# fit3 <- dbfit(x,y,2, nbs = 100, nbscov = 100)
# fit3$rho_CI_1 # The first row is lower bounds, and second row is upper bounds

```

---

durbin1fit

*Durbin stage 1 fit*


---

### Description

Function implements the Durbin stage 1 fit

### Usage

```
durbin1fit(y, x, arp, method, scores)
```

### Arguments

y	the response variable in stage 1, not the original response variable
x	the model matrix in stage 1, not the original design matrix
arp	the order of autoregressive errors.
method	the method to be used for fitting. If "OLS", uses the ordinary least square; If "RANK", uses the rank-based fit.
scores	Default is Wilcoxon scores

### Note

This function is for internal use. The main function for users is dbfit.

### References

McKnight, S. D., McKean, J. W., and Huitema, B. E. (2000). A double bootstrap method to analyze linear models with autoregressive error terms. *Psychological methods*, 5 (1), 87. Shaofeng Zhang (2017). Ph.D. Dissertation.

---

 durbin1xy

*Creating New X and Y for Durbin Stage 1*


---

### Description

Functions provides the transformed reponse variable and model matrix for Durbin stage 1 fit. For details of the transformation, see the reference.

### Usage

```
durbin1xy(y, x, arp)
```

### Arguments

y	the orginal response variable
x	the orginal design matrix with first column of all one's (corresponding to the intercept)
arp	the order of autoregressive errors.

### References

McKnight, S. D., McKean, J. W., and Huitema, B. E. (2000). A double bootstrap method to analyze linear models with autoregressive error terms. *Psychological methods*, 5 (1), 87. Shaofeng Zhang (2017). Ph.D. Dissertation.

---

 durbin2fit

*Durbin stage 2 fit*


---

### Description

Function implements the Durbin stage 1 fit

### Usage

```
durbin2fit(y, xc, adjphi, method, scores)
```

### Arguments

y	a transformed reponse variable
xc	a transformed design matrix
adjphi	the Durbin stage 1 estimate(s) of the autoregressive parameters rho
method	the method to be used for fitting. If "OLS", uses the ordinary least square; If "RANK", uses the rank-based fit.
scores	Default is Wilcoxon scores



**Value**

beta	the estimates of regression coefficients
sigma	the estimate of standard deviation of the white noise

**Note**

This function is for internal use. The main function for users is `dbfit`.

**References**

McKnight, S. D., McKean, J. W., and Huitema, B. E. (2000). A double bootstrap method to analyze linear models with autoregressive error terms. *Psychological methods*, 5 (1), 87. Shaofeng Zhang (2017). Ph.D. Dissertation.

---

fullr	<i>QR decomposition for non-full rank design matrix for Rfit.</i>
-------	---

---

**Description**

With Rfit recent update, it cannot return partial results with sigular design matrix (as opposed to `lm`). This function uses QR decomposition for Rfit to resolve this issue, so that `dbfit` can run robust version.

**Usage**

```
fullr(x, p1)
```

**Arguments**

x	design matrix, including intercept, i.e. the first column being ones.
p1	number of first few columns of x that are lineraly independent.

**Note**

This function is for internal use.

hmdesign2

*the Two-Phase Design Matrix*

---

**Description**

Returns the design matrix for a two-phase intervention model.

**Usage**

```
hmdesign2(n1, n2)
```

**Arguments**

n1	number of obs in phase 1
n2	number of obs in phase 2

**Details**

It returns a matrix of 4 columns. As discussed in Huitema, Mckean, & Mcknight (1999), in two-phase design: beta0 = intercept, beta1 = slope for Phase 1, beta2 = level change from Phase 1 to Phase 2, and beta3 slope change from Phase 1 to Phase 2.

**References**

Huitema, B. E., Mckean, J. W., & Mcknight, S. (1999). Autocorrelation effects on least-squares intervention analysis of short time series. *Educational and Psychological Measurement*, 59 (5), 767-786.

**Examples**

```
n1 <- 15
n2 <- 15
hmdesign2(n1, n2)
```

---

hmmat*K-Phase Design Matrix*

---

**Description**

Returns the design matrix for a general k-phase intervention model

**Usage**

```
hmmat(vecss, k)
```

**Arguments**

vecss	a vector of length k with each element being the number of observations in each phase
k	number of phases

**Details**

It returns a matrix of  $2*k$  columns. The design can be unbalanced, i.e. each phase has different observations.

**References**

Huitema, B. E., Mckean, J. W., & Mcknight, S. (1999). Autocorrelation effects on least- squares intervention analysis of short time series. *Educational and Psychological Measurement*, 59 (5), 767-786.

**See Also**

[hmdesign2](#)

**Examples**

```
# a three-phase design matrix
hmmat(c(10,10,10),3)
```

---

hypothmat

*General Linear Tests of the regression coefficients*

---

**Description**

Performs general linear tests of the regressio coefficients.

**Usage**

```
hypothmat(sfit, mmat, n, p)
```

**Arguments**

sfit	the result of a call to dbfit.
mmat	a full row rank $q*(p+1)$ matrix, where q is the row number of the matrix and p is number of independent variables.
n	total number of observations.
p	number of independent variables.

**Details**

This functions performs the general linear F-test of the form  $H_0: Mb = 0$  vs  $H_A: Mb \neq 0$ .

**Value**

tst                    the test statistic  
 pvf                    the p-value of the F-test

**References**

McKnight, S. D., McKean, J. W., and Huitema, B. E. (2000). A double bootstrap method to analyze linear models with autoregressive error terms. *Psychological methods*, 5 (1), 87. Shaofeng Zhang (2017). Ph.D. Dissertation.

**Examples**

```
# data(testdata)
# y<-testdata[,5]
# x<-testdata[,1:4]
# fit1<-dbfit(x,y,1) # OLS fit, default
# a test that H0: b1 = b3 vs HA: b1 != b3
# mat<-matrix(c(1,0,0,-1),nrow=1)
# hypothmat(sfit=fit1,mmat=mat,n=40,p=4)
```

---

 lagx

*Lag Functions*


---

**Description**

For preparing the transformed x and y in the Durbin stage 1 fit

**Usage**

```
lagx(x, s1, s2)
lagmat(x, p)
```

**Arguments**

x                    a vector or the design matrix, including intercept, i.e. the first column being ones.  
 s1                   starting index of the slice.  
 s2                   end index of the slice.  
 p                    the order of autoregressive errors.

**Note**

These function are for internal use.

---

 nurho

*Creating a new response variable for Durbin stage 2*


---

**Description**

It returns a new response variable (vector) for Durbin stage 2.

**Usage**

```
nurho(yc, adjphi)
```

**Arguments**

yc                    the centered response variable y  
 adjphi                (initial) estimate of rho in Durbin stage 1

**Details**

see reference.

**Note**

This function is for internal use. The main function for users is `dbfit`.

**References**

McKnight, S. D., McKean, J. W., and Huitema, B. E. (2000). A double bootstrap method to analyze linear models with autoregressive error terms. *Psychological methods*, 5 (1), 87. Shaofeng Zhang (2017). Ph.D. Dissertation.

---

 print.dbfit

*DBfit Internal Print Functions*


---

**Description**

These functions print the output in a user-friendly manner using the internal R function `print`.

**Usage**

```
## S3 method for class 'dbfit'
print(x, ...)
## S3 method for class 'summary.dbfit'
print(x, ...)
```

**Arguments**

x                    An object to be printed  
...                   additional arguments to be passed to print

**See Also**

[dbfit](#), [summary.dbfit](#)

---

rhoci2

*A fisher type CI of the autoregressive parameter rho*

---

**Description**

This function returns a Fisher type CI for rho, which is then used to correct the .99 cases.

**Usage**

```
rhoci2(n, rho, cv)
```

**Arguments**

n                    total number of observations  
rho                  final estimate of rho, usually .99.  
cv                   critical value for CI

**Details**

see reference.

**Note**

This function is for internal use.

**References**

Shaofeng Zhang (2017). Ph.D. Dissertation. Rao, C. R. (1952). Advanced statistical methods in biometric research. p. 231

---

`simpgen1hm2`*Simulation Data Generating Function*

---

**Description**

Generates the simulation data for a two-phase intervention model.

**Usage**

```
simpgen1hm2(n1, n2, rho, beta = c(0, 0, 0, 0))
```

**Arguments**

n1	number of obs in phase 1
n2	number of obs in phase 2
rho	pre-defined autoregressive parameter(s)
beta	pre-defined regression coefficients

**Details**

This function is used for simulations when developing the package. With pre-defined sample sizes in both phases and parameters, it returns a simulated data.

**Value**

mat	a matrix containing the simulation data. The last column is the response variable. All other columns make up the design matrix.
-----	---

**See Also**

[hmdesign2](#)

**Examples**

```
n1 <- 15
n2 <- 15
rho <- 0.6
beta <- c(0,0,0,0)
dat <- simpgen1hm2(n1, n2, rho, beta)
dat
```

---

simula

*Work Horse Function to implement the Double Bootstrap method*

---

### Description

simula is the original work horse function to implement the DB method. However, when this function returns an estimate of rho to be .99, another work horse function simulacorrection kicks in.

### Usage

```
simula(x, y, arp, nbs, nbscov, conf, method, scores)
```

### Arguments

x	the design matrix, including intercept, i.e. the first column being ones.
y	the response variable.
arp	the order of autoregressive errors.
nbs	the bootstrap size for the first bootstrap procedure. Default is 500.
nbscov	the bootstrap size for the second bootstrap procedure. Default is 500.
conf	the confidence level of CI for rho, default is 0.95.
method	the method to be used for fitting. If "OLS", uses the ordinary least square <code>lm</code> ; If "RANK", uses the rank-based fit <code>rfit</code> .
scores	Default is Wilcoxon scores

### Details

see [dbfit](#).

### Note

Users should use `dbfit` to perform the analysis.

### References

McKnight, S. D., McKean, J. W., and Huitema, B. E. (2000). A double bootstrap method to analyze linear models with autoregressive error terms. *Psychological methods*, 5 (1), 87. Shaofeng Zhang (2017). Ph.D. Dissertation.

### See Also

[dbfit](#).



---

simulacorrection	<i>Work Horse Function to Implement the Double Bootstrap Method For .99 Cases</i>
------------------	---

---

### Description

When function `simula` returns an estimate of  $\rho$  to be `.99`, this function kicks in and outputs a corrected estimate of  $\rho$ . Currently, this only works for order 1, i.e. for order  $> 1$ , this correction will not get involved.

### Usage

```
simulacorrection(x, y, arp, nbs, nbscov, method, scores)
```

### Arguments

<code>x</code>	the design matrix, including intercept, i.e. the first column being ones.
<code>y</code>	the response variable.
<code>arp</code>	the order of autoregressive errors.
<code>nbs</code>	the bootstrap size for the first bootstrap procedure. Default is 500.
<code>nbscov</code>	the bootstrap size for the second bootstrap procedure. Default is 500.
<code>method</code>	the method to be used for fitting. If "OLS", uses the ordinary least square <code>lm</code> ; If "RANK", uses the rank-based fit <code>rfit</code> .
<code>scores</code>	Default is Wilcoxon scores

### Details

If 0.99 problem is detected, then construct Fisher CI for both initial estimate (in Durbin stage 1) and first bias-corrected estimate (perform only one bootstrap, instead of a loop); if the midpoint of latter is smaller than 0.95, then this midpoint is the final estimate for  $\rho$ ; otherwise the midpoint of the former CI is the final estimate.

By default, when function `simula` returns an estimate of  $\rho$  to be `.99`, this function kicks in and outputs a corrected estimate of  $\rho$ . However, users can turn the auto correction off by setting `correction="FALSE"` in `dbfit`. Users are encouraged to investigate why the stationarity assumption is violated based on their experience of time series analysis and knowledge of the data.

### Note

Users should use `dbfit` to perform the analysis.

### References

Shaofeng Zhang (2017). Ph.D. Dissertation.

### See Also

[dbfit](#).

---

summary.dbfit	<i>Summarize the double bootstrap (DB) fit</i>
---------------	--

---

### Description

It summarizes the DB fit in a way that is similar to OLS lm.

### Usage

```
## S3 method for class 'dbfit'
summary(object, ...)
```

### Arguments

object	a result of the call to rfit
...	additional arguments to be passed

### Value

call	the call to rfit
tab	a table of point estimates, standard errors, t-ratios and p-values
rho1	the Durbin two-stage estimate of rho
adjar	the DB (final) estimate of rho
flag99	an indicator; if 1, it indicates the original fit yields an estimate of rho to be 0.99. Only valid if order 1 is specified.

### Examples

```
# data(testdata)
# y<-testdata[,5]
# x<-testdata[,1:4]
# fit1<-dbfit(x,y,1) # OLS fit, default
# summary(fit1)
```

---

testdata	<i>testdata</i>
----------	-----------------

---

### Description

This data serves as a test data.

### Usage

```
data("testdata")
```

**Format**

A data frame with 40 observations. First 4 columns make up the design matrix, while the last column is the response variable. This data is generated by a two-phase design, with autoregressive order being one, autoregressive coefficient being 0.6 and all regression coefficients being 0. Both the first and second phase have 20 observations.

**Examples**

```
data(testdata)
```

---

wrho

*Creating a new design matrix for Durbin stage 2*

---

**Description**

It returns a new design matrix for Durbin stage 2.

**Usage**

```
wrho(xc, adjphi)
```

**Arguments**

xc	centered design matrix, no column of ones
adjphi	(initial) estimate of rho in Durbin stage 1

**Details**

see reference.

**Note**

This function is for internal use. The main function for users is `dbfit`.

**References**

McKnight, S. D., McKean, J. W., and Huitema, B. E. (2000). A double bootstrap method to analyze linear models with autoregressive error terms. *Psychological methods*, 5 (1), 87. Shaofeng Zhang (2017). Ph.D. Dissertation.

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