

Package ‘BLOQ’

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Title Methods to Impute and Analyze Data with BLOQ Observations

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Description Provides methods for estimating the area under the concentration versus time curve (AUC) and its standard error in the presence of Below the Limit of Quantification (BLOQ) observations. Two approaches are implemented: direct estimation using censored maximum likelihood, and a two-step approach that first imputes BLOQ values using various methods and then computes the AUC using the imputed data. Technical details are described in Barnett et al. (2020), “Methods for Non-Compartmental Pharmacokinetic Analysis With Observations Below the Limit of Quantification,” *Statistics in Biopharmaceutical Research*. <doi:10.1080/19466315.2019.1701546>.

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estimateAUCandStdErr *Estimate AUC and its standard error*

Description

function to estimate AUC and compute standard error of this estimate

Usage

```
estimateAUCandStdErr(
  imputedData,
  timePoints,
  isMultiplicative = FALSE,
  na.rm = FALSE
)
```

Arguments

| | |
|------------------|---|
| imputedData | numeric matrix or data frame of size n by J (n the sample size and J the number of time points) |
| timePoints | vector of time points |
| isMultiplicative | logical variable indicating whether an additive error model (FALSE) or a multiplicative error model (TRUE) should be used |
| na.rm | logical variable indicating whether the rows with missing values should be ignored or not. |

Value

vector of length 2 with estimated AUC and its standard error

Author(s)

Vahid Nassiri, Helen Yvette Barnett

Examples

```
# generate data from Beal model with only fixed effects
set.seed(111)
genDataFixedEffects <- simulateBealModelFixedEffects(10, 0.693,
+ 1, 1, seq(0.5,3,0.5))
# Impute the data with BLOQ's with one of the provided methods,
# for example, here we use ROS
imputedDataROS <- imputeROS(genDataFixedEffects, 0.1)
# estimate AUC and its standard error
estimateAUCandStdErr(imputedDataROS,seq(0.5,3,0.5))
```

```
estimateAUCwithCMLperTimePoint
```

estimate AUC with censored maximum likelihood per time point

Description

function to estimate mean and standard error of each column of data with BLOQ's using a censored maximum likelihood (CML) approach, then use these estimates for estimating AUC and its standard error

Usage

```
estimateAUCwithCMLperTimePoint(
  inputData,
  LOQ,
  timePoints,
  isMultiplicative = FALSE,
  onlyFitCML = FALSE,
  printCMLmessage = TRUE,
  optimizationMethod = NULL,
  CMLcontrol = NULL
)
```

Arguments

| | |
|------------------|---|
| inputData | numeric matrix or data frame of the size n by J (n the sample size and J the number of time points) the input dataset |
| LOQ | scalar, limit of quantification value |
| timePoints | vector of time points |
| isMultiplicative | logical variable indicating whether an additive error model (FALSE) or a multiplicative error model (TRUE) should be used |
| onlyFitCML | logical variable with FALSE as default, if TRUE only the censored maximum likelihood estimates will be calculated |

| | |
|--------------------|---|
| printCMLmessage | logical variable with TRUE as default, if TRUE then messages regarding the convergence status of censored log-likelihood maximization will be printed. |
| optimizationMethod | single string specifying the method to be used for optimizing the log-likelihood, the default is NULL that allows the function to decide about the best method. Otherwise, one can select among choices available via R package maxLik: "NR" (for Newton-Raphson), "BFGS" (for Broyden-Fletcher-Goldfarb-Shanno), "BFGSR" (for the BFGS algorithm implemented in R), "BHHH" (for Berndt-Hall-Hausman), "SANN" (for Simulated ANNealing), "CG" (for Conjugate Gradients), or "NM" (for Nelder-Mead). Lower-case letters (such as "nr" for Newton-Raphson) are allowed. |
| CMLcontrol | list of arguments to control convergence of maximization algorithm. It is the same argument as control in the function maxLik in the R package maxLik |

Value

a list with three components: output of maxLik function, estimated parameters for each column using censored maximum likelihood, and estimated AUC and its standard error.

Author(s)

Vahid Nassiri, Helen Yvette Barnett

See Also

[maxLik](#)

Examples

```
# generate data from Beal model with only fixed effects
set.seed(111)
genDataFixedEffects <- simulateBealModelFixedEffects(10, 0.693,
  1, 1, seq(0.5,3,0.5))
# Multiplicative error model
estimateAUCwithCMLperTimePoint(genDataFixedEffects, 0.1, seq(0.5,3,0.5), TRUE)
```

estimateAUCwithFullCML

estimate AUC with Full censored maximum likelihood

Description

function to estimate mean and covariance matrix of censored data using a full censored maximum likelihood approach (with a special structure for the covariance matrix which only allows correlations between successive time points), then use these estimates for estimating AUC and its standard error

Usage

```
estimateAUCwithFullCML(
  inputData,
  LOQ,
  timePoints,
  isMultiplicative = FALSE,
  onlyFitCML = FALSE,
  printCMLmessage = TRUE,
  optimizationMethod = NULL,
  CMLcontrol = NULL,
  na.rm = TRUE
)
```

Arguments

| | |
|---------------------------------|--|
| <code>inputData</code> | numeric matrix or data frame of the size n by J (n the sample size and J the number of time points) the input dataset |
| <code>LOQ</code> | scalar, limit of quantification value |
| <code>timePoints</code> | vector of time points |
| <code>isMultiplicative</code> | logical variable indicating whether an additive error model (FALSE) or a multiplicative error model (TRUE) should be used |
| <code>onlyFitCML</code> | logical variable with FALSE as default, if TRUE only the censored maximum likelihood estimates will be calculated |
| <code>printCMLmessage</code> | logical variable with TRUE as default, if TRUE then messages regarding the convergence status of censored log-likelihood maximization will be printed. |
| <code>optimizationMethod</code> | single string specifying the method to be used for optimizing the log-likelihood, the default is NULL that allows the function to decide about the best method. Otherwise, one can select among choices available via R package <code>maxLik</code> : "NR" (for Newton-Raphson), "BFGS" (for Broyden-Fletcher-Goldfarb-Shanno), "BFGSR" (for the BFGS algorithm implemented in R), "BHHH" (for Berndt-Hall-Hall-Hausman), "SANN" (for Simulated ANNealing), "CG" (for Conjugate Gradients), or "NM" (for Nelder-Mead). Lower-case letters (such as "nr" for Newton-Raphson) are allowed. |
| <code>CMLcontrol</code> | list of arguments to control convergence of maximization algorithm. It is the same argument as <code>control</code> in the function <code>maxLik</code> in the R package <code>maxLik</code> |
| <code>na.rm</code> | logical variable indicating whether the lines with missing values should be ignored (TRUE, default) or not (FALSE). |

Value

a list with three components: output of `maxLik` function, estimated parameters (mean vector and the covariance matrix) using censored maximum likelihood, and estimated AUC and its standard error.

Author(s)

Vahid Nassiri, Helen Yvette Barnett

See Also

[maxLik](#)

Examples

```
#' # generate data from Beal model with only fixed effects
set.seed(123)
genDataFixedEffects <- simulateBealModelFixedEffects(10, 0.693,
1, 1, seq(0.5,3,1.5))
estimateAUCwithFullCML(genDataFixedEffects, 0.15, seq(0.5,3,1.5))
```

estimateAUCwithMVNCML *estimate AUC with multivariate normal censored maximum likelihood*

Description

function to estimate mean and covariance matrix of censored data using a full censored maximum likelihood approach (with a special structure for the covariance matrix which only allows correlations between successive time points), then use these estimates for estimating AUC and its standard error

Usage

```
estimateAUCwithMVNCML(
  inputData,
  LOQ,
  timePoints,
  isMultiplicative = FALSE,
  onlyFitCML = FALSE,
  printCMLmessage = TRUE,
  optimizationMethod = NULL,
  CMLcontrol = NULL,
  na.rm = TRUE,
  isPairwise = FALSE
)
```

Arguments

| | |
|------------|---|
| inputData | numeric matrix or data frame of the size n by J (n the sample size and J the number of time points) the input dataset |
| LOQ | scalar, limit of quantification value |
| timePoints | vector of time points |

| | |
|---------------------------------|--|
| <code>isMultiplicative</code> | logical variable indicating whether an additive error model (FALSE) or a multiplicative error model (TRUE) should be used |
| <code>onlyFitCML</code> | logical variable with FALSE as default, if TRUE only the censored maximum likelihood estimates will be calculated |
| <code>printCMLmessage</code> | logical variable with TRUE as default, if TRUE then messages regarding the convergence status of censored log-likelihood maximization will be printed. |
| <code>optimizationMethod</code> | single string specifying the method to be used for optimizing the log-likelihood, the default is NULL that allows the function to decide about the best method. Otherwise, one can select among choices available via R package <code>maxLik</code> : "NR" (for Newton-Raphson), "BFGS" (for Broyden-Fletcher-Goldfarb-Shanno), "BFGSR" (for the BFGS algorithm implemented in R), "BHHH" (for Berndt-Hall-Hall-Hausman), "SANN" (for Simulated ANNealing), "CG" (for Conjugate Gradients), or "NM" (for Nelder-Mead). Lower-case letters (such as "nr" for Newton-Raphson) are allowed. |
| <code>CMLcontrol</code> | list of arguments to control convergence of maximization algorithm. It is the same argument as <code>control</code> in the function <code>maxLik</code> in the R package <code>maxLik</code> |
| <code>na.rm</code> | logical variable indicating whether the lines with missing values should be ignored (TRUE, default) or not (FALSE). |
| <code>isPairwise</code> | logical variable, if TRUE the unstructured covariance matrix will be estimated using pairwise approach, otherwise (FALSE, default) the full maximum likelihood will be used with a special structure imposed on the covariance matrix. |

Value

a list with three components: output of `maxLik` function, estimated parameters (mean vector and the covariance matrix) using censored maximum likelihood, and estimated AUC and its standard error.

Author(s)

Vahid Nassiri, Helen Yvette Barnett

See Also

[maxLik](#)

Examples

```
# generate data from Beal model with only fixed effects
set.seed(111)
genDataFixedEffects <- simulateBealModelFixedEffects(10, 0.693,
1, 1, seq(0.5,3,1.5))
estimateAUCwithMVNCML(genDataFixedEffects, 0.1, seq(0.5,3,1.5))
estimateAUCwithMVNCML(genDataFixedEffects, 0.1, seq(0.5,3,1.5),
isPairwise = TRUE)
```

```
estimateAUCwithPairwiseCML
```

estimate AUC with pairwise censored maximum likelihood

Description

function to estimate mean and covariance matrix of censored data using a full censored maximum likelihood approach via fitting all possible pairs, then use these estimates for estimating AUC and its standard error

Usage

```
estimateAUCwithPairwiseCML(
  inputData,
  LOQ,
  timePoints,
  isMultiplicative = FALSE,
  onlyFitCML = FALSE,
  optimizationMethod = NULL,
  CMLcontrol = NULL,
  na.rm = TRUE
)
```

Arguments

| | |
|---------------------------------|--|
| <code>inputData</code> | numeric matrix or data frame of the size n by J (n the sample size and J the number of time points) the input dataset |
| <code>LOQ</code> | scalar, limit of quantification value |
| <code>timePoints</code> | vector of time points |
| <code>isMultiplicative</code> | logical variable indicating whether an additive error model (FALSE) or a multiplicative error model (TRUE) should be used |
| <code>onlyFitCML</code> | logical variable with FALSE as default, if TRUE only the censored maximum likelihood estimates will be calculated. |
| <code>optimizationMethod</code> | single string specifying the method to be used for optimizing the log-likelihood, the default is NULL that allows the function to decide about the best method. Otherwise, one can select among choices available via R package <code>maxLik</code> : "NR" (for Newton-Raphson), "BFGS" (for Broyden-Fletcher-Goldfarb-Shanno), "BFGSR" (for the BFGS algorithm implemented in R), "BHHH" (for Berndt-Hall-Hall-Hausman), "SANN" (for Simulated ANNealing), "CG" (for Conjugate Gradients), or "NM" (for Nelder-Mead). Lower-case letters (such as "nr" for Newton-Raphson) are allowed. |
| <code>CMLcontrol</code> | list of arguments to control convergence of maximization algorithm. It is the same argument as <code>control</code> in the function <code>maxLik</code> in the R package <code>maxLik</code> |

`na.rm` logical variable indicating whether the lines with missing values should be ignored (TRUE, default) or not (FALSE). Note that, it will be applied for the sub-datasets regarding each pair.

Value

a list with three components: output of `maxLik` function, estimated parameters (mean vector and the covariance matrix) using censored maximum likelihood, and estimated AUC and its standard error.

Author(s)

Vahid Nassiri, Helen Yvette Barnett

See Also

[maxLik](#)

Examples

```
# generate data from Beal model with only fixed effects
set.seed(111)
genDataFixedEffects <- simulateBealModelFixedEffects(10, 0.693,
1, 1, seq(0.5,3,1.5))
estimateAUCwithPairwiseCML(genDataFixedEffects, 0.1, seq(0.5,3,1.5))
```

imputeBLOQ

impute BLOQ's with various methods

Description

function to impute BLOQ's. The user can define column-specific methods to impute the BLOQ's.

Usage

```
imputeBLOQ(inputData, LOQ, imputationMethod, progressPrint = FALSE, ...)
```

Arguments

`inputData` numeric matrix or data frame of the size n by J (n the sample size and J the number of time points) the input dataset

`LOQ` scalar, limit of quantification value

`imputationMethod`

could be a single string or a vector of strings with the same length as the number of time points (`ncol(inputData)`). If it is left blank, then the imputation is done using kernel density estimation method for the columns with at least one non-BLOQ component. For all the rest (only BLOQ) the constant imputation is used. The allowed values are "constant", "ros", "kernel", "cml" corresponding to

constant imputation, imputing using regression on order statistics, imputing using kernel density estimator, and imputing using censored maximum likelihood, respectively.

`progressPrint` logical variable indicating whether the imputation progress should be printed or not.

... any other argument which should be changed according to the input arguments regarding the functions corresponding to different imputation methods.

Value

a list with two components: imputed dataset, and the methods used to impute each column.

Author(s)

Vahid Nassiri, Helen Yvette Barnett

Examples

```
set.seed(111)
inputData <- simulateBealModelFixedEffects(10, 0.693, 1, 1, seq(0.5, 3, 0.5))
LOQ = 0.125
imputeBLOQ(inputData, LOQ,
  imputationMethod = c("cml", "ros", "kernel", "constant", "constant", "constant"),
  maxIter = 500, isMultiplicative = TRUE, constantValue = LOQ)
imputeBLOQ(inputData, LOQ, maxIter = 500, isMultiplicative = TRUE,
  constantValue = LOQ/5, epsilon = 1e-04)
```

imputeCML

imputing BLOQ's using censored maximum likelihood

Description

function to impute BLOQ's using quantiles of a normal distribution with mean and standard error estimates using censored maximum likelihood

Usage

```
imputeCML(
  inputData,
  LOQ,
  isMultiplicative = FALSE,
  useSeed = runif(1),
  printCMLmessage = TRUE,
  CMLcontrol = NULL
)
```

Arguments

| | |
|------------------|--|
| inputData | numeric matrix or data frame of the size n by J (n the sample size and J the number of time points) the input dataset |
| LOQ | scalar, limit of quantification value |
| isMultiplicative | logical variable indicating whether an additive error model (FALSE) or a multiplicative error model (TRUE) should be used |
| useSeed | scalar, set a seed to make the results reproducible, default is runif(1), it is used to randomly order the first imputed column (if the first column has any BLOQ's) |
| printCMLmessage | logical variable with TRUE as default, if TRUE then messages regarding the convergence status of censored log-likelihood maximization will be printed. |
| CMLcontrol | list of arguments to control convergence of maximization algorithm. It is the same argument as control in the function maxLik in the R package maxLik |

Value

the imputed dataset: a numeric matrix or data frame of the size n by J (n the sample size and J the number of time points)

Author(s)

Vahid Nassiri, Helen Yvette Barnett

See Also

[maxLik](#)

Examples

```
# generate data from Beal model with only fixed effects
set.seed(111)
genDataFixedEffects <- simulateBealModelFixedEffects(10, 0.693,
+ 1, 1, seq(0.5,3,0.5))
imputeCML(genDataFixedEffects, 0.1, FALSE, 1)
```

| | |
|----------------|--|
| imputeConstant | <i>imputing BLOQ's with a constant value</i> |
|----------------|--|

Description

function to impute BLOQ observations by replacing them with a constant value.

Usage

```
imputeConstant(inputData, LOQ, constantValue)
```

Arguments

`inputData` numeric matrix or data frame of the size n by J (n the sample size and J the number of time points) the input dataset

`LOQ` scalar, limit of quantification value

`constantValue` scalar, the constant value which replaces all BLOQ's, default is $LOQ/2$

Value

the imputed dataset: a numeric matrix or data frame of the size n by J (n the sample size and J the number of time points)

Author(s)

Vahid Nassiri, Helen Yvette Barnett

Examples

```
# generate data from Beal model with only fixed effects
set.seed(111)
genDataFixedEffects <- simulateBealModelFixedEffects(10, 0.693,
+ 1, 1, seq(0.5,3,0.5))
# replacing BLOQ's with LOQ/2
imputeConstant(genDataFixedEffects, 0.1, 0.1/2)
```

`imputeKernelDensityEstimation`

imputing BLOQ's using kernel density estimation

Description

function to impute BLOQ observations using kernel density estimation.

Usage

```
imputeKernelDensityEstimation(
  inputData,
  LOQ,
  epsilon = 1e-07,
  maxIter = 1000,
  useSeed = runif(1)
)
```

Arguments

| | |
|-----------|--|
| inputData | numeric matrix or data frame of the size n by J (n the sample size and J the number of time points) the input dataset |
| LOQ | scalar, limit of quantification value |
| epsilon | scalar with 1e-07 as default, the difference between two iterations which achieving it would stop the procedure (convergence). |
| maxIter | scalar, the maximum number of iterations with 1000 as default. |
| useSeed | scalar, set a seed to make the results reproducible, default is runif(1), it is used to randomly order the first imputed column (if the first column has any BLOQ's) |

Value

the imputed dataset: a numeric matrix or data frame of the size n by J (n the sample size and J the number of time points)

Author(s)

Vahid Nassiri, Helen Yvette Barnett

Examples

```
# generate data from Beal model with only fixed effects
set.seed(111)
genDataFixedEffects <- simulateBealModelFixedEffects(10, 0.693,
+ 1, 1, seq(0.5,3,0.5))
imputeKernelDensityEstimation(genDataFixedEffects, 0.1, epsilon = 1e-05)
```

imputeROS

imputing BLOQ's using regression on order statistics

Description

function to impute BLOQ's with regression on order statistics (ROS) approach.

Usage

```
imputeROS(inputData, LOQ, isMultiplicative = FALSE, useSeed = runif(1))
```

Arguments

| | |
|------------------|--|
| inputData | numeric matrix or data frame of the size n by J (n the sample size and J the number of time points) the input dataset |
| LOQ | scalar limit of quantification value |
| isMultiplicative | logical variable indicating whether an additive error model (FALSE) or a multiplicative model (TRUE) should be used |
| useSeed | scalar, set a seed to make the results reproducible, default is runif(1), it is used to randomly order the first imputed column (if the first column has any BLOQ's) |

Value

the imputed dataset: a numeric matrix or data frame of the size n by J (n the sample size and J the number of time points)

Author(s)

Vahid Nassiri, Helen Yvette Barnett

Examples

```
# generate data from Beal model with only fixed effects
set.seed(111)
genDataFixedEffects <- simulateBealModelFixedEffects(10, 0.693,
+ 1, 1, seq(0.5,3,0.5))
imputeROS(genDataFixedEffects, 0.1)
```

simulateBealModelFixedEffects

simulate data from Beal model with fixed effects

Description

function to generate data from a Beal model with fixed effects

Usage

```
simulateBealModelFixedEffects(
  numSubjects,
  clearance,
  volumeOfDistribution,
  dose,
  timePoints
)
```

Arguments

| | |
|----------------------|---|
| numSubjects | scalar, number of subject which should be generated |
| clearance | scalar, clearance |
| volumeOfDistribution | scalar, volume of distribution |
| dose | scalar, dose |
| timePoints | vector of time points |

Details

The model used to generate data at time t is as follows

$$y(t) = C(t) \exp(e(t)),$$

where $C(t)$, the PK-model, is defined as follows:

$$C(t) = \frac{\text{dose}}{V_d} \exp(-CL \cdot t),$$

with V_d the volume of distribution and CL as clearance. The error model is considered as $e(t) \sim N(0, h(t))$, with:

$$h(t) = 0.03 + 0.165 \frac{C(t)^{-1}}{C(1.5)^{-1} + C(t)^{-1}}$$

Value

generated sample with numSubjects as the number of rows and length of timePoints as the number of columns

Author(s)

Vahid Nassiri, Helen Yvette Barnett

See Also

Beal S. L., Ways to fit a PK model with some data below the quantification limit, Journal of Pharmacokinetics and Pharmacodynamics, 2001;28(5):481–504.

Examples

```
set.seed(111)
simulateBealModelFixedEffects(10, 0.693,
+ 1, 1, seq(0.5, 3, 0.5))
```

```
simulateBealModelMixedEffects
```

simulate data from Beal model with fixed and random effects

Description

function to generate data from a Beal model with fixed effects

Usage

```
simulateBealModelMixedEffects(
  numSubjects,
  clearance,
  volumeOfDistribution,
  dose,
  varCompClearance,
  varCompVolumeOfDistribution,
  timePoints
)
```

Arguments

numSubjects scalar, number of subject which should be generated

clearance scalar, clearance

volumeOfDistribution
 scalar, volume of distribution

dose scalar, dose

varCompClearance
 scalar, standard error of the normal distribution generating clearance

varCompVolumeOfDistribution
 scalar, standard error of the normal distribution generating volume of distribu-
 tion

timePoints vector of time points

Details

The model used to generate data at time t is as follows

$$y(t) = C(t) \exp(e(t)),$$

where $C(t)$, the PK-model, is defined as follows:

$$C(t) = \frac{\text{dose}}{V_d} \exp(CL \cdot t),$$

with V_d the volume of distribution and CL as clearance. The error model is considered as $e(t) \sim N(0, h(t))$, with:

$$h(t) = 0.03 + 0.165 \frac{C(t)^{-1}}{C(1.5)^{-1} + C(t)^{-1}}.$$

For the mixed effects model, $CL = \widetilde{CL} \exp(\eta_1)$, and $V_d = \widetilde{V}_d \exp(\eta_2)$, where $\eta_1 \sim N(0, w_1^2)$ and $\eta_2 \sim N(0, w_2^2)$. Note that w_1 and w_2 are specified by *varCompClearance*, and *varCompVolumeOfDistribution* in the arguments, respectively.

Value

generated sample with numSubjects as the number of rows and length of timePoints as the number of columns

Author(s)

Vahid Nassiri, Helen Yvette Barnett

See Also

Beal S. L., Ways to fit a PK model with some data below the quantification limit, *Journal of Pharmacokinetics and Pharmacodynamics*, 2001;28(5):481–504.

Examples

```
set.seed(111)
simulateBealModelMixedEffects(10, 0.693,
+ 1, 1, 0.2,0.2, seq(0.5,3,0.5))
```

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