

Figure 1 in Elamir and Seheult (2004)

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First of all load the library:

```
> library(nsRFA)
```

and generate the samples from the Normal distribution:

```
> Nsim=1000
```

```
> n=60
```

```
> campsimulati <- rnorm(n*Nsim)
```

```
> campsimulati <- matrix(campsimulati, ncol=n)
```

Then calculate l_3 and $SE(l_3)$:

```
> lmom <- t(apply(campsimulati, 1, Lmoments))
```

```
> vlmom <- t(apply(campsimulati, 1, varLmoments, matrix=FALSE))
```

```
> l3 <- lmom[, "lca"]*lmom[, "l2"]
```

```
> sl3 <- sqrt(vlmom[, "var.l3"])
```

```
> l3gaussian <- l3/sl3
```

and plot the results:

```
> qqnorm(l3gaussian, main="Normal Q-Q Plot for Gaussian samples")
```

```
> qqline(l3gaussian)
```

Repeat the same procedure for the Student distribution:

```
> campsimulati <- rt(n*Nsim, df=5)
```

```
> campsimulati <- matrix(campsimulati, ncol=n)
```

```
> lmom <- t(apply(campsimulati, 1, Lmoments))
```

```
> vlmom <- t(apply(campsimulati, 1, varLmoments, matrix=FALSE))
```

```
> l3 <- lmom[, "lca"]*lmom[, "l2"]
```

```
> sl3 <- sqrt(vlmom[, "var.l3"])
```

```
> l3student <- l3/sl3
```

the Cauchy distribution:

```
> campsimulati <- rcauchy(n*Nsim)
```

```
> campsimulati <- matrix(campsimulati, ncol=n)
```

```
> lmom <- t(apply(campsimulati, 1, Lmoments))
```

```
> vlmom <- t(apply(campsimulati, 1, varLmoments, matrix=FALSE))
```

```
> l3 <- lmom[, "lca"]*lmom[, "l2"]
```

```
> sl3 <- sqrt(vlmom[, "var.l3"])
```

```
> l3cauchy <- l3/sl3
```

and the Uniform distribution:

```

> campsimulati <- runif(n*Nsim)

> campsimulati <- matrix(campsimulati, ncol=n)
> lmom <- t(apply(campsimulati, 1, Lmoments))
> vlmom <- t(apply(campsimulati, 1, varLmoments, matrix=FALSE))
> l3 <- lmom[, "lca"]*lmom[, "l2"]
> sl3 <- sqrt(vlmom[, "var.l3"])

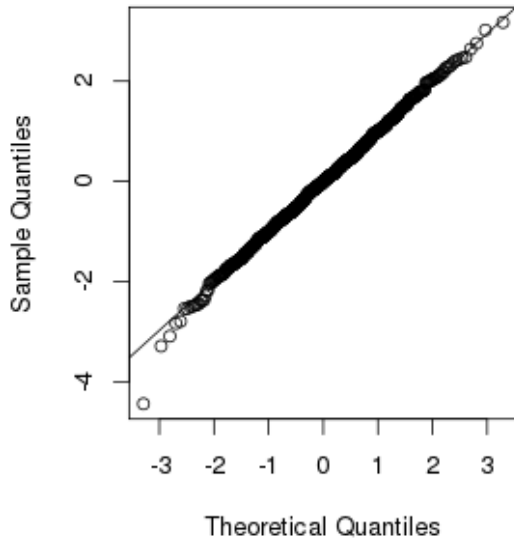
> l3unif <- l3/sl3

Plot the result:

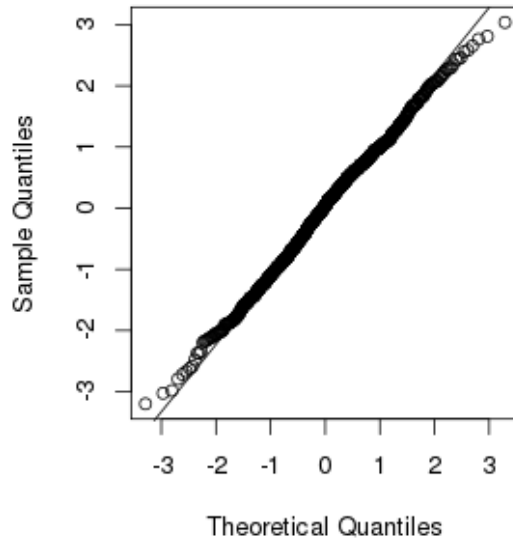
> layout(matrix(c(1,2,3,4), 2, 2, byrow = TRUE))
> qqnorm(l3gaussian, main="Normal Plot: Gaussian samples")
> qqline(l3gaussian)
> qqnorm(l3student, main="Normal Plot: Student (df=5) samples")
> qqline(l3student)
> qqnorm(l3cauchy, main="Normal Plot: Cauchy samples")
> qqline(l3cauchy)
> qqnorm(l3unif, main="Normal Plot: Uniform samples")
> qqline(l3unif)

```

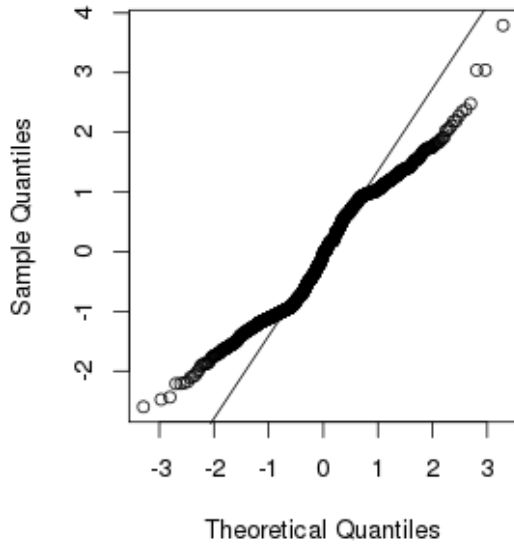
Normal Plot: Gaussian samples



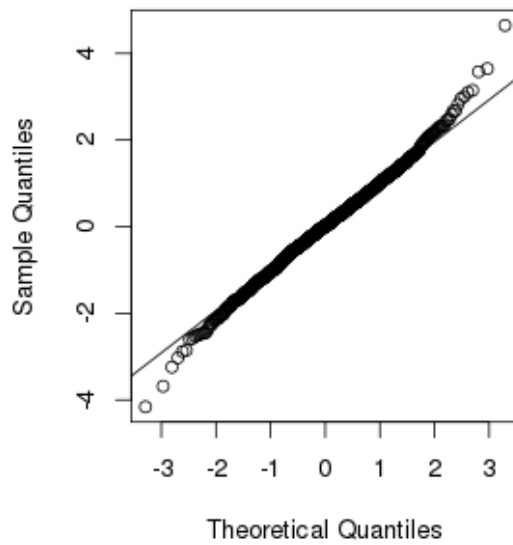
Normal Plot: Student (df=5) samples



Normal Plot: Cauchy samples



Normal Plot: Uniform samples



Normal quantile plots and added line for $N = 1000$ simulated values of $l_3/SE(l_3)$ from Gaussian, Student(5), Cauchy and Uniform samples of size $n = 60$.

References

Elamir, E.A.H., and Seheult, A.H. (2004). Exact variance structure of sample L-moments. *Journal of Statistical Planning and Inference*, 124:337–359.